<table>
<thead>
<tr>
<th>Title</th>
<th>A singing voices synthesis system to characterize vocal registers using ARX-LF model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Author(s)</td>
<td>Motoda, Hiroki; Akagi, Masato</td>
</tr>
<tr>
<td>Citation</td>
<td>2013 International Workshop on Nonlinear Circuits, Communications and Signal Processing (NCSP'13): 93-96</td>
</tr>
<tr>
<td>Issue Date</td>
<td>2013-03</td>
</tr>
<tr>
<td>Type</td>
<td>Conference Paper</td>
</tr>
<tr>
<td>URL</td>
<td><a href="http://hdl.handle.net/10119/11510">http://hdl.handle.net/10119/11510</a></td>
</tr>
<tr>
<td>Rights</td>
<td>This material is posted here with permission of the Research Institute of Signal Processing Japan. Hiroki Motoda and Masato Akagi, 2013 International Workshop on Nonlinear Circuits, Communications and Signal Processing (NCSP'13), 2013, pp.93-96.</td>
</tr>
</tbody>
</table>
A singing voices synthesis system to characterize vocal registers using ARX-LF model

Hiroki Motoda and Masato Akagi

School of Information Science, Japan Advanced Institute of Science and Technology
1-1 Asahidai, Nomi, Ishikawa, 923-1292 Japan
Phone/FAX:+81-761-51-1391/+81-761-51-1149
Email: {H.Motoda, akagi}@jaist.ac.jp

Abstract
This paper proposes a singing voices synthesis system to synthesize singing voices having characteristics of vocal registers, such as modal, falsetto and falsetto. Human can sing songs naturally in wide range of frequency by training how to use vocal fold vibrations to represent vocal registers. However, even state-of-the-art singing voices synthesis systems cannot produce vocal registers appropriately. Naturalness of the synthesized singing voices using these systems is reduced in low and high frequency ranges. One of the methods for improving naturalness is adding characteristics of glottal sources for each vocal register. This paper considers a model that can represent glottal sources with characteristics of vocal registers for an advanced singing voice synthesis system. This paper proposes a singing voice synthesis system with the ARX-LF model that can describe glottal sources for each vocal register by simulating glottal production mechanisms. A model for controlling ARX-LF parameters corresponding to glottal sources was constructed, and acoustic features corresponding to naturalness of singing voice were added. Singing voice data of each vocal register were analyzed by the ARX-LF model, and ARX-LF parameter values corresponding to glottal source of each vocal register were obtained. The control model was constructed using the results of the analysis. Singing voices were synthesized by the control model, and quality of the synthesized voices was evaluated. As the results, almost the same impressions were obtained from the synthesized singing voices as those from actual singing voices in each vocal register. Results revealed effectiveness of the proposed system for synthesizing singing voices to characterize vocal registers.

1. Introduction
Vocal register is a particular series of tones in the human voice that are produced by one particular vibratory pattern of the vocal folds and therefore possess a common quality. Human can sing songs naturally in wide range of frequency by training how to use vocal fold vibrations to represent vocal registers. Many researchers investigated relationships between vocal registers and characteristics of glottal sources [1][2][3].

However, even state-of-the-art singing voices synthesis systems cannot produce vocal registers appropriately. Naturalness of the synthesized singing voices using these systems is reduced in low and high frequency ranges. Characteristics of vocal registers in VOCALOID [4] depends on materials of stored singing data. Although SingBySpeaking [5] can synthesize natural singing voice in mid tone range using STRAIGHT [6], controlling of vocal quality corresponding to glottal sources is difficult in STRAIGHT. Thus, SingBySpeaking cannot produce vocal registers in high and low tone ranges appropriately. One of the methods for improving naturalness is adding characteristics of glottal sources for each vocal register. This paper considers a model that can represent glottal sources with characteristics of vocal registers for an advanced singing voice synthesis system. This paper proposes a singing voice synthesis system with the ARX-LF model [7] that can describe glottal sources for each vocal register by simulating human voice production mechanisms. A model for controlling ARX-LF parameters corresponding to characteristics of glottal sources was constructed. Singing voices were synthesized using the control model, and quality of the synthesized voices were evaluated.

2. Overview of the proposed system
2.1 ARX-LF model
Production mechanisms of human voices is simulated by an ARX-LF model as equation 1.

$$s(n) + \sum_{i=1}^{p} a_i(n)s(n-i) = b_0(n)u(n) + \varepsilon(n)$$

(1)

where $s(n)$ and $u(n)$ are observed speech signal and glottal source signal at time $n$, where $u(n)$ is approximated by LF glottal source model [8]. $a_i(n)$ and $b_0(n)$ are time-varying coefficients and $\varepsilon(n)$ is residual. By applying the Z-transform onto the equation (assuming time invariance), one gets the following equation,

$$S(z) = \frac{1}{A(z)} \cdot U(z) + \frac{1}{A(z)} \cdot E(z)$$

(2)

where $U(z)$, $E(z)$ and $S(z)$ are Z-transform of glottal source, residual and voice. The shape of $u(n)$ is represented by fundamental period $T_0$, and four waveshape parameters $T_p$, $T_o$, $T_{oa}$ and $E_v$ as shown Figure 1. $E_v$ is calculated by $b_0$. In order to simplify controlling the shape of $u(n)$, three parameters $O_q$, $\alpha_m$, and $Q_a$ are chosen as ARX-LF
parameters. \( O_q = \frac{T_e}{T_0} \) corresponds to the open quotient, \( \alpha_m = \frac{T_p}{T_e} \) to the asymmetry coefficient, and \( Q_a = \frac{T_a}{(1 - O_q)T_0} \) to the return phase quotient.


Although literatures revealed relationships between vocal registers and vocal tract filter, for example [3], this paper focuses on characteristics of glottal sources only. Vocal tract filter is not modified.

3. Model for controlling ARX-LF parameters

In this section, a model for controlling ARX-LF parameter values was proposed to represent characteristics of glottal sources for each vocal register. ARX-LF parameter values of each register were obtained by ARX-LF analysis, and the control model was constructed using the results of the analysis.

3.1 Analysis condition

Singing voice data were selected from the database “Nihongowo uta uta utau”. Vowel /a/ was chosen from voiced sounds. In this study, three vocal registers, vocal fry, modal, and falsetto were targeted. In order to obtain ARX-LF parameter values corresponding to glottal source of each vocal register, typical singing voices belonging to each register were selected. In this study, two parameters \( V_b \) and \( F_b \) are set to determine the boundaries of vocal registers voluntarily. \( V_b \) denotes the boundary between vocal fry and modal, and \( F_b \) denotes the boundary between modal and falsetto. \( V_b \) and \( F_b \) are set to 90 (Hz), 400 (Hz), respectively. Five samples of vocal fry and ten samples for each of modal and falsetto were chosen as the typical ones. Sampling frequency was 12 kHz.

3.2 Analysis results

Relationships between ARX-LF parameter values and characteristics of glottal sources for each vocal register were considered. Mean values of ARX-LF parameter values for each vocal register were shown in Table 1. It is known that the open quotient is larger in falsetto and smaller in vocal fry and typical \( O_q \) values were obtained; \( \alpha_m \) is small in falsetto, because partial vibration of vocal fold in falsetto leads this result; and \( Q_a \) is large in falsetto, because turbulent flow generated by incomplete closure of vocal fold in falsetto produces this result. These results revealed that characteristics of glottal source for each vocal register can be represented by ARX-LF parameters.

Table 1: Mean parameter values of ARX-LF analysis of each vocal register

<table>
<thead>
<tr>
<th>Vocal Register</th>
<th>( O_q )</th>
<th>( \alpha_m )</th>
<th>( Q_a )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vocal Fry</td>
<td>0.226</td>
<td>0.826</td>
<td>0.015</td>
</tr>
<tr>
<td>Modal</td>
<td>0.434</td>
<td>0.824</td>
<td>0.025</td>
</tr>
<tr>
<td>Falsetto</td>
<td>0.824</td>
<td>0.773</td>
<td>0.116</td>
</tr>
</tbody>
</table>
3.3 Model for controlling each ARX-LF parameter

Models for controlling ARX-LF parameters are proposed to synthesize singing voices having characteristics of vocal registers. Each ARX-LF parameter is modified in accordance with \( F_0 \) of music score \( F_{0_{\text{syn}}} \). In order to preserve speaker individuality, \( F_0 \) of speaking data \( F_{0_{\text{ori}}} \) and each ARX-LF parameter obtained by ARX-LF analysis \( O_{q_{\text{ori}}} \), \( \alpha_{m_{\text{ori}}} \) and \( Q_{a_{\text{ori}}} \) are used. ARX-LF parameters for each vocal register are interpolated in a linear manner. Scattered maps of parameter values are shown in Figures 3 to 5.

- **Control model for \( O_q \)**

\( O_q \) is widely varied among vocal registers as shown in Figure 3. In addition, there is a slight tilt for each vocal register. In order to represent tilt, regression line of each vocal register were calculated by a least-squares method, as shown in Table 2. An \( O_q \) control model is constructed based on the regression line. A modified parameter value \( O_{q_{\text{syn}}} \) is calculated by the following equations.

\[
O_{q_{\text{syn}}} = O_{q_{\text{ori}}} + y_{oq}(F_{0_{\text{syn}}}) - y_{oq}(F_{0_{\text{ori}}})
\]

where \( a_{oq}, b_{oq} \) are decided by \( x, V_b \) and \( F_b \) value. If \( x < V_b \), values of vocal fry is chosen, in Table 2. If \( V_b \leq x < F_b \), values of modal is chosen. If \( F_b \leq x \), values of falsetto is chosen.

\[
y_{oq}(x) = a_{oq} \cdot \log_2 x - b_{oq}
\]

![Figure 3: Distribution map of \( O_q \) of each data](image)

<table>
<thead>
<tr>
<th>( x )</th>
<th>( F_{0_{\text{ori}}} )</th>
<th>( F_{0_{\text{syn}}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>vocal fry</td>
<td>0.119</td>
<td>-0.529</td>
</tr>
<tr>
<td>modal</td>
<td>0.050</td>
<td>0.047</td>
</tr>
<tr>
<td>falsetto</td>
<td>0.207</td>
<td>-1.001</td>
</tr>
</tbody>
</table>

- **Control model for \( \alpha_m \)**

In order to represent partial vibration of vocal fold in falsetto, the following control model for \( \alpha_m \) is constructed. \( \alpha_m \) is modified if \( F_{0_{\text{syn}}} \) is high. \( \alpha_m \) is widely varied in falsetto as shown in Figure 4. Parameter \( \alpha_r \) is set up to decide rate of change voluntarily. A modified parameter value \( \alpha_{m_{\text{ori}}} \) is calculated by the following equations.

\[
\alpha_{m_{\text{syn}}} = \begin{cases} 
\alpha_{m_{\text{ori}}} \cdot \alpha_r & (F_b \leq F_{0_{\text{syn}}}) \\
\alpha_{m_{\text{ori}}} & (F_{0_{\text{syn}}} < F_b)
\end{cases}
\]

![Figure 4: Distribution map of \( \alpha_m \) of each data](image)

- **Control model for \( Q_a \)**

In order to represent turbulent flows generated by incomplete closure of the vocal fold, a control model for \( Q_a \) is constructed. \( Q_a \) is large in falsetto as shown by Figure 5. In addition, there is a slight tilt in each of vocal register. As the same as \( O_q \), the regression line of each vocal register was calculated, as shown in Table 3. A modified parameter value \( Q_{a_{\text{syn}}} \) is calculated by the following equations.

\[
Q_{a_{\text{syn}}} = Q_{a_{\text{ori}}} + y_{qa}(F_{0_{\text{syn}}}) - y_{qa}(F_{0_{\text{ori}}})
\]

where \( a_{qa}, b_{qa} \) are decided by \( x, V_b \) and \( F_b \) value. If \( x < V_b \), values of vocal fry is chosen, in Table 3. If \( V_b \leq x < F_b \), values of modal is chosen. If \( F_b \leq x \), values of falsetto is chosen.

![Figure 5: Distribution map of \( Q_a \) of each data](image)

<table>
<thead>
<tr>
<th>( x )</th>
<th>( F_{0_{\text{ori}}} )</th>
<th>( F_{0_{\text{syn}}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>vocal fry</td>
<td>0.038</td>
<td>-0.232</td>
</tr>
<tr>
<td>modal</td>
<td>0.009</td>
<td>-0.004</td>
</tr>
<tr>
<td>falsetto</td>
<td>0.015</td>
<td>0.035</td>
</tr>
</tbody>
</table>
4. Evaluation of synthesized singing voice

In this section, quality of the synthesized singing voices in wide frequency ranges was evaluated. In order to evaluate reproducibility of falsetto and vocal fry, Experiment I and Experiment II were carried out.

Experiment I: synthesized singing voices in modal and falsetto registers were compared.

Experiment II: synthesized singing voices in modal and vocal fry registers were compared.

4.1 Synthesized singing voice

Six singing voices were synthesized for each experiment. In Experiment I, singing voices in modal register as Mf1, Mf2, Mf3 and those in falsetto register as F1, F2, F3 were synthesized. F0s were set to 247 Hz (B3), 277 Hz (C4), 294 Hz (D4), 330 Hz (E4), 370 Hz (F4), 440 Hz (A4), respectively. In Experiment II, singing voices in modal as Mv1, Mv2, Mv3 and those in vocal fry as V1, V2, V3 were synthesized. F0s were set to 130 Hz (C3), 123 Hz (B2), 110 Hz (A2), 87 Hz (F2), 82 Hz (E2), 73 Hz (D2), respectively, and $\alpha_r = 0.9$, $V_b = 100$, and $F_b = 310$.

4.2 Experimental condition

The procedure for the Experiments was the Scheffe’s Paired Comparison. Seven male listeners were participated in the experiments. The number of trials was 30 (=6 x 5) in each experiment. Degrees of “Breathy” that is typical impression of falsetto was evaluated in Experiment I. Degrees of “Rough” that is typical impression of vocal fry was evaluated in Experiment II. In order to simplify the decision task, “Breathy” voices and “Rough” voices were learned using actual singing voices in advance.

4.3 Results and Discussions

Population parameter $\sigma$ was estimated from results of each Experiment using Ura Variation. $\sigma$ of Experiment I is shown in Table 4. If $\sigma$ is large positive value, singing voice was perceived as “Breathier”. $\sigma$ is widely varied between modal and falsetto. This result ensured that characteristics of falsetto can be represented by the proposed system. In addition, $\sigma$ is larger if tone ranges are higher. This indicates that adding characteristics of glottal sources for each vocal register is important in wide tone ranges.

In Experiment II, similar results are obtained. $\sigma$ of Experiment II is shown in Table 5. If $\sigma$ is larger positive value, the singing voice was perceived as “Rougher”. This result suggested that characteristics of vocal fry can be represented by the proposed system. As the results, reproducibility of vocal registers by the proposed system were ensured.

| Table 4: Results of Experiment 1 |
|---|---|---|---|---|---|
| $\sigma$ | Mf1 | Mf2 | Mf3 | F1 | F2 | F3 |
| -1.35 | -1.29 | -1.01 | 0.88 | 1.09 | 1.67 |

| Table 5: Results of Experiment 2 |
|---|---|---|---|---|---|
| $\sigma$ | Mv1 | Mv2 | Mv3 | V1 | V2 | V3 |
| -1.51 | -1.41 | -1.05 | 0.76 | 1.36 | 1.86 |

5. Conclusions

This paper proposed a singing voices synthesis system with the ARX-LF model to synthesize singing voices having characteristics of vocal registers. A model for controlling ARX-LF parameters was constructed to represent characteristics of glottal sources for each vocal register. Quality of the synthesized singing voices in wide frequency ranges was evaluated. Results revealed that characteristics of vocal registers can be represented appropriately by the proposed system.

In this study, boundaries of vocal registers were not analyzed, and vocal tract filter was not modified. In the future work, we investigate transitions of ARX-LF parameters boundaries of vocal registers, and construct a model for controlling vocal tract filter.

References