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Doctoral Dissertation

An Interactive Theorem Proving Framework for Declarative Cloud Orchestration

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Abstract

An interactive theorem proving framework for verifying declarative cloud orchestration is proposed.

Recent rapid progress of cloud computing accelerates the whole life cycle of system usage and requires much flexible automation of system operations. Automation of cloud system operations is called cloud orchestration and correctness of cloud orchestration becomes much crucial for many activities in the human society. However, correctness of automated cloud system operations cannot depend on testing-based quality control because a cloud system is a kind of distributed systems and it is not possible to exhaustively test all of its behavior which may occur at various situations in the production environment. Formal approaches are expected to provide systematic ways to guarantee correctness of cloud orchestration.

Formal approaches are mainly classified into two categories, model checking and theorem proving. As opposed to model checking, theorem proving can verify models of arbitrary many number of states and so suitable for proving absence of counter examples. However, when applying to practical problems it requires many human efforts to develop proofs.

This dissertation proposes a framework of interactive proof development for a kind of liveness properties, leads-to property, of cloud orchestration. We say "framework" to mean something like an application framework of software development which brings high productivity by minimizing development efforts and high maintainability by consistent structure of application software.

The proposed framework provides (1) a general way to formalize specifications of different kinds of cloud orchestration tools and (2) a procedure for how to verifying a kind of liveness properties, as well as invariant properties, of formalized specifications. It also provides (3) general templates and libraries of formal descriptions for specifying orchestration of cloud systems and (4) proved lemmas for general predicates of the libraries to be used for verification.

The framework has been applied to the verification of specifications of AWS CloudFormation and also of OASIS TOSCA, and is demonstrated to be effective for reducing generic routine work and making a verification engineer concentrate on the work specific to each individual system. The case study of OASIS TOSCA shows that the framework can be used to specify, represent, and verify the behavior models of TOSCA where the standard has not yet provided any ways to do so. It also shows a general way to manage dependencies of cloud resources which is a smarter one than that of the most popular tool, CloudFormation.

The major contributions of this dissertation are that (1) it introduces the idea of frameworks from software development to proof development which results in high productivity and high maintainability of proofs and (2) it shows that the framework can be effectively applied to a non-trivial problem, that is, to specify, represent, and verify the behavior models of the standard specification language of cloud orchestration.

Key Words: Cloud Orchestration, System Specification/Verification, Theorem Proving, Framework, Proof Scores, CafeOBJ

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Chapter 1

Introduction

Cloud computing has recently emerged as an important infrastructure supporting many aspects of human activities. In former days, it took several months to make system infrastructure resources (computer, network, storage, etc.) available, while in these days, it takes only several minutes to do so. This situation accelerates the whole life cycle of system usage where much flexible automation is required for system operations such as setting up, scaling, patching, and so on. The total automation of system operations is sometimes called "Infrastructure as Code" (IaC).

1.1 Correctness of Automated Operations of Cloud Systems

A system on cloud consists of many "parts," such as virtual machines (VMs), storages, and network services as well as software packages, configuration files, and user accounts in VMs. These parts are called *resources* and the automated management of cloud resources is called *resource orchestration*, or *cloud orchestration*.

The most popular cloud orchestration tool is *CloudFormation* [3] provided as a service by Amazon Web Services (AWS) and a compatible open source tool is being developed as *Open-Stack Heat* [31]. CloudFormation can manage resources provided by IaaS platform of AWS, such as VMs (EC2), block storages (EBS), load balancers (ELB), and so on. CloudFormation automatically sets up these resources according to declaratively defined dependencies of resources. However, CloudFormation does not directly manage resources inside VMs and instead it allows to specify any types of scripts for initially setting up VMs, such as installing Httpd package, creating configuration files, copying contents, and activating an Httpd component. Shell command scripts were commonly used for this layer of management and recently several open source tools become popular such as *Puppet* [24], *Chef* [6], and *Ansible* [25]. Currently operation engineers have to learn and use these several kinds of tools in actual situations, which results in much elaboration to guarantee correctness of automated operations. In an actual commercial experience of the author, more than 50% of troubles are caused by defects in those dependency definitions and scripts.

Correctness of cloud orchestration is much more crucial than that of the former systems because cloud systems serve to much more people in much longer time than the former systems used mainly inside of companies. Although cloud computing enables to easily, cheaply, and repeatedly prepare testing environments for cloud systems, test-based quality control is not sufficient for automated system operations because a cloud system is a kind of distributed systems and it is not possible to exhaustively test all of its behavior which may occur at various situations in the production environment. In practice, typical and problematic defects of automated system operations often occur at unusual situations, for example, when activation of some component is much delayed because of unexpected heavy accesses to file/database systems or when accidental termination of some component occurs and it returns no responses. In order to test operations at unusual situations, Netflix, an American video on demand company, has been using a resiliency tool, named *Chaos Monkey* [20], which intentionally and randomly terminates some components of their system in the production environment. Chaos is controlled to occur during business hours of weekdays so that operation engineers can solve the problems and learn from them when automated operations fail to deal with the situations. Reinhold, E. [26], an engineer of Uber, the most famous online transportation network company, reported that they are using a similar resiliency tools, named *uDestroy*, to unleash controlled chaos on their services.

1.2 Theorem Proving Framework for Cloud Orchestration

We believe formal approaches will provide more systematic ways to guarantee correctness of cloud orchestration because they have theoretical bases to exhaustively test all possible behavior of cloud systems. Formal approaches have a long research history of more than half a century and many theories and techniques together with the remarkable evolution of computing power enable to apply them to various domains, such as automotive software, mobile IC chip firmware, financial and military applications, and so on.

However, it is difficult, as ever, to apply formal approaches to practical scale problems because they require distinctive knowledge and skills and there are not enough number of engineers who have acquired such knowledge and skills. In the computer company, the author is working for, there have been many trial projects applying various formal approaches, several selected engineers were trained for each project, and most of the trials were reported as succeeded. But none of them was expanded to apply to practical projects after trained engineers dispersed.

The shortage of competent engineers is a very common problem when a new technology is applied to practical scale problems. For example, about twenty years ago we had to shift our software development methods from structured models to object oriented models. Many projects suffered from lack of competent object oriented architects and Java programmers, which is a major reason why some of the projects lost several million dollars. However, object orientation becomes a matured technology nowadays and many large-scale applications are developed using object oriented architectures. It is not because the shortage of competent engineers is fully resolved. Instead, now we successfully make use of high reusability of object oriented designs and programs especially as *application frameworks*.

For example, Ruby on Rails (RoR) [14] is one of the most popular application frameworks. RoR defines an MVC architecture of web applications, provides super classes and utility classes to implement the architecture, and gives developers a guide for how to design and code web applications. RoR brings high productivity by minimizing development efforts and high maintainability by consistent structure of applications. In general, an application framework focuses on a specific application domain and provides (1) a general application model which defines structure and behavior of applications in the domain, (2) abstract reusable entities, i.e. super classes and utility classes, which can be instantiated to implement the application model, and (3) procedures which define how the developers design, program, and configure their own applications. Using an application framework is a very popular approach to raise the skill level of novice engineers and to enable a large number of engineers to efficiently develop a practical scale application with the consistent structure and behavior.

This dissertation proposes a "framework" of interactive proof development for a kind of liveness properties, *leads-to* property, of cloud orchestration. The most important property of an automated system operation, which we want to guarantee, is that the operation surely brings a cloud system to a desired state. We say "surely" to mean that the system always reaches some final state from any initial states, which is formalized as (*init* leads-to *final*). There are two major difficulties to verify the reachability of cloud orchestration. One is to find sufficient conditions for the reachability. The framework assists proof developers how to construct the sufficient conditions for their own problem. Another difficulty is to manage acyclicness of resource dependency. In a cloud system, dependency among resources should not become cyclic in order to reach a desired state. The framework provides how to formalize and prove the invariant property of the acyclicness.

Similarly to application frameworks in software development, the theorem proving framework provides a general formalization of cloud orchestration specifications of different kinds of tools and provides a procedure for how to verify leads-to properties, and also invariant properties, of the specifications. It also provides logic templates and predicate libraries which are defined in a general level of abstraction and can be instantiated as problem specific descriptions, predicates, and lemmas. Using them, the verification procedure assists developers to systematically think and develop proofs of leads-to properties. The theorem proving framework is expected to raise the skill level of proof developers and to enable a number of engineers to efficiently develop practical scale proofs of cloud orchestration with a consistent structure.

1.3 Formal Verification of System Behavior

One major approach of formal verification of system behavior is *model checking* which is based on exhaustive analysis of states of transition systems and can automatically find counter examples included in the specified models. However, the sizes of models are limited and thus absence of counter examples cannot be proved.

Model checking has been used for verification of software behavior since 1990's. For example, Magee, J., et al. [17] used model checking to verify safety and liveness properties of software architecture. Cornejo, M. A., et al. [8] specified an existing (and commonly used) dynamic reconfiguration protocol in LOTOS (Language Of Temporal Ordering Specification) and verified several temporal properties, such as "every reconfiguration command is eventually followed by an acknowledgment", using model checking techniques of the CADP tool set. Vassev, E., et al. [34] applied model checking to autonomic computing in the NASA Voyager mission. They show that liveness properties, such as "a picture taken by the Voyager will eventually be result in sending a message to antennas on Earth", specified by ASSL (Autonomic System Specification Language), can be verified. Song, J., et al. [30] used the SPIN model checker to verify two invariant properties of a self-configuration procedure for autonomous networks of cellular base stations. Recently, Salaün, G., et al. [9, 27, 28] designed a system setup protocol in the cloud and demonstrated to verify a liveness property of the protocol using their model checking method.

The framework proposed in this dissertation supports another approach, namely *interactive theorem proving*, which can verify models of arbitrary many number of states and so suitable for proving absence of counter examples. It requires thinking through meanings of the specified

models, which is very important aspect of developing trusted systems. However, when applying to practical problems, it requires many human efforts to develop proofs for splitting the cases, establishing lemmas, and proving them in the course of verification.

There also exist several researches to apply the theorem proving approach to practical problems. Klein, G. et al. [16] used the Isabelle/HOL theorem prover to verify functional correctness of OS Kernel. They wrote 4900 lines of the abstract specification, 5700 lines of the Haskell prototype which is automatically converted to the executable specification, and 8700 lines of the C program which is converted to the implementation specification. They proved two step refinements (from abstract to executable and from executable to implementation level) using the forward simulation method and wrote about 200-kilo proof steps. Since they focused functional correctness, they did not ensure correctness of the abstract specification.

The German Verisoft project [12] researches verification of a whole software stack from verified hardware to verified application programs. In the project, Alkassar, E., et al. [2] used the Isabelle/HOL theorem prover to verify functional correctness of their page-fault handler in which program properties are specified by the Hoare logic, transferred or mapped to several lower stack layers, and finally implemented by a hardware instruction set. They proved more than twelve thousands of lemmas and wrote more than 244-kilo proof steps. They found some difficulty to keep a consistent style of proof development in such scale of problem, which they described as follows:

"The theories were developed by various people from different sites with different backgrounds and Isabelle offers its users quite some opportunity to develop an individual proof style. Some prefer rather small steps others try to push automation as far as possible. Some prefer the 'apply' style, which often leads a large number of intermediate lemmas, others structure their proofs with Isar."

None of the existing researches described above did not consider reuse of proofs which our framework provides for its users. As far as we know, reuse of proofs is discussed only in Event-B community as the generic instantiation approach proposed by Abrial, J. and Hallerstede, S. [1]. The idea of the generic instantiation is that it is sufficient to prove instantiated axioms in order to reuse proofs of a generic machine and its refined machines.

Silva, R. and Butler, M. J. [29] proposed to use theorem proving to ensure the sufficient condition of the generic instantiation. Using the renaming and composing plug-ins for the Rodin platform (a tool set for Event-B), they defined a way of instantiating generic machines and generating the sufficient condition as a theorem of the concrete machine whose proof obligation will be ensured by Rodin's theorem prover. Tikhonova, U., et al. [32] applied this idea to verify LACE DSL programs of controlling lithography machines. However, the generated theorems are too large for the automatic provers of Rodin to discharge. They say that they do not expect their average user to prove these theorems using interactive provers, as it requires knowledge of propositional calculus and understanding of proof strategies. Instead of theorem proving, they employed evaluation of structural properties predicates in the animation plug-in of Rodin.

The existing researches of applying theorem proving to practical scale problems commonly reported that it requires much human efforts and the shortage of competent proof engineer is a remained problem, which is the main concern of this dissertation.

One of the major contributions of this dissertation is to introduce the idea of frameworks from software development to proof development, which has a unique set of features as follows:

• The framework supports verification of leads-to properties as well as invariant properties of practical scale problems using interactive theorem proving.

- It provides a general way to formalize specifications in a specific domain, i.e. cloud orchestration.
- It provides abstract entities and proved lemmas to be reused to specify and verify concrete problems with high productivity.
- It also provides a procedure to guide novice proof engineers which results in consistent proofs with high maintainability.

Although the above features of this dissertation are, in principle, not dependent on the theorem proving system to be implemented, the following functionalities of CafeOBJ, described in Chapter 3, contribute to realizing the effective framework.

- **Transition search predicates** enable to prove the reachability of state transition systems together with equations in a unified manner of predicate logic.
- **Template modules** enable to define general entities and to reuse them by instantiating and renaming which brings high productivity.
- **Constructor-based inductive theorem prover** enables users to easily follow the provided procedure and develop consistent structure of models and proofs which brings high maintainability.

1.4 Standard Specification Language of Cloud Orchestration

The second major contribution of this dissertation is to show that the idea of theorem proving framework can be effectively applied to a non-trivial problem, that is, to specify, represent, and verify the behavior models of the standard specification language of cloud orchestration where the standard has not yet provided any ways to do so.

While orchestration tools are specialized into two management layers, on IaaS and inside VMs, there is a unified standard specification language, *OASIS TOSCA* [21] that can be used to describe the structure of both types of resources. The resource structure is called a *topology* and a TOSCA tool is expected to automate system operations based on resource dependencies declaratively defined by topologies.

TOSCA assumes two main engineering roles, namely a type architect and an application architect. In a typical scenario, type architects define and provide several types of resources and an application architect uses them to define a topology of a cloud system. The type architect also defines *operations*¹ of resource types, such as creating, starting, stopping, or deleting resources. A system operation of a cloud system is implemented as an invocation sequence of the type operations, which can be decided in two kinds of manners. One is an imperative manner in which the application architect uses a process modeling language to define a plan that explicitly invokes these type operations. Another is a declarative one in which the application architect only defines a topology and a TOSCA tool will automatically invoke appropriate type operations based on the defined topology. Naturally, the declarative manner is a main target of OASIS TOSCA because it promotes more abstract and reusable descriptions of topologies.

Currently there are no practical implementations of the declarative manner of TOSCA and one of the reasons is that no standard set of type operations are defined and there is no way for type architects to define behavior of their own types. In Section 7.2, we will describe how to

¹In this dissertation, we say *a type operation* as an operation of a type whereas TOSCA calls it *a lifecycle operation*.

use our framework to define behavior of TOSCA types and to verify that a specified topology can correctly automate to set up the cloud system.

The rest of this dissertation is organized as follows. Chapter 2 introduces several cloud orchestration tools. Chapter 3 introduces functionalities of CafeOBJ language in which we represent formal specifications of cloud systems. Chapter 4 describes a general model of cloud orchestration. Chapter 5 describes general logic templates and predicate libraries. Chapter 6 presents the procedure for verification of leads-to properties using a simple example specification of CloudFormation. Chapter 7 explains how the framework is applied to verification of OASIS TOSCA specifications. Chapter 8 explains related work and future issues.

Chapter 2

Cloud Orchestration

Cloud computing is a model for providing computational resources that allows on-demand accesses via the internet to shared pools of configurable resources such as networks, computers, storage, middleware, development tools, applications, etc.

Cloud computing services are classified into three categories by the type of computing resources to provide. IaaS (Infrastructure as a Service) is one of the service categories which mainly provides hardware facilities via the internet. Such as servers, storages, and networks are typically provided and called as virtual machines(VMs), virtual storages, and virtual networks. PaaS (Platform as a Service) is another category which mainly provides middleware (software components for constructing applications) via the internet, such as application servers, databases, and messaging queues, and so on. SaaS (Software as a Service) is the last category in which applications are provided via the internet.

Recent rapid progress of cloud computing accelerates the whole life cycle of system usage and requires much flexible automation of system operations, such as set-up, scale-out, scalein, or shutdown of cloud systems. Automation of cloud system operations is called *resource orchestration*, or *cloud orchestration* and there are many cloud orchestration tools used in practical situations. This chapter introduces several popular cloud orchestration tools and describes differences of their ways to specify automated system operations.

2.1 AWS CloudFormation

The most popular cloud orchestration tool is *CloudFormation* [3] provided as a service by Amazon Web Services (AWS). CloudFormation can manage *resources* provided by IaaS platform of AWS, such as VMs (EC2), block storages (EBS), and load balancers (ELB). CloudFormation automatically sets up these resources according to a *template* that declaratively defines dependencies of resources. A template is a set of resources and a resource has an identifier and a type and includes several *properties* which may depend on other resources.

Fig. 2.1 is part of a very simple CloudFormation template written in JSON format [15]. This template specifies the dependency of the resources in a simple cloud system on the AWS IaaS platform shown in lower part of Fig. 2.1. There are two resources; one has the identifier MyInstance and the type AWS::EC2::Instance, another has the identifier MyEIP and the type AWS::EC2::EIP. Note that an Elastic Compute Cloud instance (EC2 instance) is a virtual machine on AWS IaaS platform and an Elastic IP (EIP) provides a static IP address for an EC2 instance which is dynamically created and activated. MyEIP has a property whose type is InstanceID. The property refers MyInstance which makes resource MyEIP depend

```
{ "Resources" : {
    "MyInstance" : {
    "Type" : "AWS::EC2::Instance",
    "MyEIP" : {
        "Type" : "AWS::EC2::EIP",
        "Properties" : {
            "InstanceId" : { "Ref" : "MyInstance" }
}}}}

MyEIP
[AWS::EC2::EIP]
InstanceID
[AWS::EC2::EIP]
```

Figure 2.1: A Very Simple CloudFormation Template

on MyInstance. Thus, CloudFormation firstly activates MyInstance and then activates MyEIP with a parameter of the instance ID of MyInstance.

2.2 Puppet, Chef, and Ansible

Puppet, Chef, and Ansible are not cloud orchestration tools but *deployment tools* (also called *configuration tools*) which are used by cloud orchestration tools to set up resources inside VMs.

Puppet [24] provides a domain specific language (DSL) to describe executable Ruby [18] scripts for setting up resources inside VMs. A Ruby script of Puppet is called a manifest and executed in a VM. Fig. 2.2 is a simple manifest written in Puppet DSL to set up an httpd service. A manifest is a list of declarations each of which declares the desired state of a resource. Each declaration specifies a type, a title, and attributes of a resource. For example, the first four lines of the manifest shown in Fig. 2.2 specifies that a *package* type resource named httpd is desired to be installed to the target VM. A package means an installable package of a middleware which is the Apache HTTP server in this case. The second declaration of the example manifest means that an httpd service is desired to be running and it requires the httpd package resource above is in the specified state. The third one means that the specified directory is desired to exist. The fourth means that a file is desired to be copied from the Puppet server to the specified file path whose owner is root, group is root, and mode is 644, which requires the directory declared above is in the specified state. The fifth one also means that a file is desired to be copied and this resource should be checked whenever the state of the specified service resource is changed. A manifest is not necessarily executed from top to bottom; the order is decided by require and subscribe attributes. A manifest is idempotent which means the result of its execution is always the same because nothing is done when a specified resource is already in the desired state.

Chef [6] also provides a Ruby-based DSL to describe executable scripts for setting up resources inside VMs. A script is called a *recipe* and executed in a VM. A collection of related recipes and auxiliary files is called a *cookbook*. Fig. 2.3 is a simple recipe written in Chef DSL to set up an httpd service. A recipe is a list of declarations each of which declares the desired state of a resource. Each declaration specifies a type, a name, attributes, and actions of a resource. For example, the first three lines of the recipe shown in Fig. 2.3 specifies that a package type resource named httpd is desired to be installed to the target VM and the action to do

```
package { "httpd":
  name => "httpd",
  ensure => "installed"
}
service { "httpd":
  name => "httpd",
  enable => "true",
  ensure => running,
  require => Package["httpd"]
}
file { "/var/www/html/sample":
  ensure => directory,
  owner => "apache",
  group => "apache",
  mode => "755",
  require => Package["httpd"]
}
file { "/var/www/html/sample/sample.html":
  source => "puppet:///files/sample.html",
  owner => "root",
  group => "root",
  mode => "644",
  require => File["/var/www/html/sample"]
}
file { "/etc/httpd/conf/httpd.conf":
  source => "puppet:///files/httpd.conf",
  mode => "644",
  owner => "root"
  group => "root"
  subscribe => Service["httpd"]
}
```



```
package "httpd" do
  action :install
end
cookbook_file "/etc/httpd/conf/httpd.conf" do
  source "httpd.conf"
  owner 'root'
  group 'root'
  mode 00644
end
directory "/var/www/html/sample" do
  owner 'apache'
  group 'apache'
  mode 00755
  action :create
end
cookbook_file "/var/www/html/sample/sample.html" do
  source "sample.html"
  owner 'root'
  group 'root'
  mode 00644
end
service "httpd" do
  supports :status => true, :restart => true, :reload => true
  action [:enable,:start]
end
```

Figure 2.3: A Simple Chef Recipe for Setting up an HTTPD Server

A: one B: - C: two D: three - E: four F: five G: six

Figure 2.4: An Example YMAL Document

so is :install. The second declaration of the example recipe means that a file httpd.conf included in the cookbook of this recipe is desired to be copied to the specified file path whose owner is root, group is root, and mode is 00644. The third one means that the specified directory is desired to exist and the fifth one means that an httpd service is desired to be running. As opposed to a Puppet manifest, a Chef recipe is executed from top to bottom and so the order of resources is critical; the fourth and fifth resources should not be inverted because the directory should exist before the file is copied into it. A recipe is idempotent similarly as a Puppet manifest. Since actions to achieve the desired states (e.g. :install) are abstracted and implemented for many kinds of operating systems, a recipe is independent from the difference of them.

What corresponds to a manifest of Puppet or a recipe of Chef is called a *playbook* in Ansible [25]. Although Ansible is implemented by Python [33], a playbook is not an executable script in Python but a YAML format file [7] which is interpreted and executed by ansible-playbook command. Before showing an example playbook, we will briefly explain the YAML format. A YAML document represents nesting key-value lists and arrays. A key and its value are separated by a colon (:). Keys with the same indentation composes a list. In Fig. 2.4, the top level list has three key-value pairs whose keys are A, B, and G. An array is represented by minus signs (-) with the same indentation. In the figure, the value of key B is an array with two elements each of which is a key-value list with two pairs. Let us write a key-value list as $\{(k1, v1), (k2, v2), \ldots\}$ and an array as $[e1, e2, \ldots]$, then the data structure represented by the YAML document in Fig. 2.4 is the following list:

{(A, one), (B, [{(C, two), (D, three)}, {(E, four), (F, five)}]), (G, six)}

A playbook represents an array of *plays* which are a sports analogy; many plays are required to set up a cloud system. Fig. 2.5 is a simple example playbook to set up an httpd service which represents only one play. A play is a key-value list including keys of hosts, tasks, and so on. Key hosts specifies machines to which the play is applied. Key tasks specifies an array of *tasks* which are executed in order. In the example, the task array includes five tasks. A task is a key-value list and typically begins with the pair of name key and its value which serves as a comment. The second pair of a task specifies a *module* and the parameters to invoke it. A module is a command provided by Ansible which can be remotely executed on the specified VMs. In the example, module yum will install the package resource named httpd, module file will create the specified file or directory, and service will start the httpd service to be running. Similarly as a Chef recipe, tasks in an Ansible playbook are executed from top to bottom and so the order of tasks is critical. A playbook is idempotent similarly as a Puppet manifest and a Chef recipe. Since modules to achieve the desired states are abstracted and implemented for many kinds of operating systems, a playbook is independent from the difference of them.

Although there are several differences among Puppet, Chef, and Ansible which are omitted to explain here, they share several common features in comparison with shell command scripts

```
- hosts: webservers
 tasks:
   - name: be sure httpd is installed
     yum: name=httpd state=installed
   - name: be sure httpd.conf exists
     file: src=/file/httpd.conf
           path=/etc/httpd/conf/httpd.conf
           state=file
           owner=root
           group=root
           mode=0644
   - name: be sure springboot root directory exists
     file: path=/var/www/html/sample
           state=directory
           owner=apache
           group=apache
           mode=0755
   - name: be sure sample.html exists
     file: src=/file/sample.html
           path=/var/www/html/sample/sample.html
           state=file
           owner=root
           group=root
           mode=0644
   - name: be sure httpd is running and enabled
```

Figure 2.5: A Simple Ansible Playbook for Setting up an HTTPD Server

service: name=httpd state=running enabled=yes

provided by operating systems of VMs. They provide domain specific languages to describe the desired states of resources. The descriptions in the DSLs are idempotent and abstracted to be independent from the difference of operation systems.

However, people have to learn and use at least two different kinds of tools (orchestration tools and configuration tools) with different styles of specifications and functionalities, which results in much elaboration to guarantee the correctness of automated system operations.

2.3 OASIS TOSCA

OASIS TOSCA[21] is a standard specification language to describe automation of a cloud system consisting of service components and their relationships using a *service template*. It provides interoperable deployments of cloud systems across different cloud environments and their management throughout the complete lifecycle (e.g. setting up, scaling, patching, monitoring, etc.). A service template consists of a *topology template* and optionally a set of *plans*. A topology template defines the resource structure of a cloud system. Note that a topology template can be parameterized to give actual environment parameters such as IP addresses, which is the reason why named as "template" and in this dissertation we simply say "a topology" for the sake of brevity. A plan is an imperative definition of a system operation of the cloud system, such as a setup plan, written by a standard process modeling language, such as BPMN [23].

In TOSCA, a resource is called a *node* that has several *capabilities* and *requirements*. A topology consists of a set of nodes and a set of *relationships* of nodes. A capability is a function that the node provides to another node, while a requirement is a function that the node needs to be provided by another node. A relationship relates a requirement of a source node to a capability of a target node. Note that nodes and relationships in a topology template can also be parameterized, thus the exact terms of TOSCA are node templates and relationship templates. Fig. 2.6 shows a typical example of topology that consists of nine nodes and nine relationships. White circles represent capabilities and black ones are requirements.

The current version of TOSCA is an XML-based language¹. Fig 2.7 is part of the topology template of Fig. 2.6. In this example, there are two nodes (VMApache and OSApache) and one relationship. VMApacheOS is a capability of VMApache and OSApacheContainer is a requirement of OSApache. Each node, relationship, capability, and requirement has a *type*, such as VirtualMachine, HostedOn, and so on. Types are main functionalities of TOSCA that enable reusability of topology descriptions.

TOSCA assumes two main technical roles, namely a type architect and an application architect. In a typical scenario, type architects define and provide several types of those elements and an application architect uses them to define a topology of a cloud system. The type architect also defines *operations* of node types, such as creating, starting, stopping, or deleting nodes, and of relationship types, such as attaching relationships. A system operation of a cloud system is implemented as an invocation sequence of the type operations, which can be decided in two kinds of manners. One is an imperative manner in which the application architect uses a process modeling language to define a plan that explicitly invokes these type operations. Another is a declarative one in which the application architect only defines a topology and a TOSCA tool will automatically invoke appropriate type operations based on the defined topology. Naturally, the declarative manner is a main target of OASIS TOSCA because it promotes more abstract and reusable descriptions of topologies.

¹OASIS TOSCA TC has published the committee draft of a simple profile for a YAML-based language. [22]



Figure 2.6: An Example of TOSCA topology

```
<TopologyTemplate>
  <NodeTemplate id="VMApache" name="VM for Apache"
                type="VirtualMachine">
    <Capabilities>
      <Capability id="VMApacheOS" name="OS"
                  type="OperatingSystemContainerCapability"/>
    </Capabilities> </NodeTemplate>
  <NodeTemplate id="OSApache" name="OS for Apache"
                type="OperatingSystem">
    <Requirements>
      <Requirement id="OSApacheContainer" name="Container"
                   type="OperatingSystemContainerRequirement"/>
    </Requirements>
    <Capabilities>
      <Capability id="OsApacheSoftware" name="Software"
                  type="SoftwareContainerCapability"/>
    </Capabilities> </NodeTemplate>
  <RelationshipTemplate id="OSApacheHostedOnVMApache"
                        name="hosted on" type="HostedOn">
    <SourceElement ref="OSApacheContainer"/>
    <TargetElement ref="VMApacheOS"/>
  </RelationshipTemplate>
. . .
</TopologyTemplate>
```

Figure 2.7: A Topology Template of TOSCA

In this dissertation, *behavior of topologies* means when and which type operations should be invoked in automation. It is important to notice that behavior of a topology is decided by types of included nodes and relationships. We also say *behavior of a type* to mean that the conditions and results of invoking its type operations, which is defined by a type architect. Usually, different types of nodes are provided by different vendors and so specified by different type architects. An application architect is responsible for behavior of a topology whereas type architects are responsible for behavior of their defined types.

Chapter 3

Preliminaries of CafeOBJ

CafeOBJ [4] is a formal specification language that is one of the state-of-the-art algebraic specification languages and a member of the OBJ [13] language family, such as Maude [19]. CafeOBJ specifications are executable by regarding equations and transition rules in them as left-to-right rewrite rules, and this executability can be used for interactive theorem proving.

3.1 Modules and Equations

Basic units of specifications in CafeOBJ are *modules*. A module¹ consists of declarations of *module importations, sorts, sub-sort relations, operators, variables, equations* and *transition rules*, some of which may be omitted. Conventionally, names of modules, sorts, and variables are capitalized while names of operators including constants start with lower case letters or use punctuation symbols.

Modules may have *parameters* and are called parameterized modules if so. An example of parameterized modules is as follows ²:

```
module! SET(X :: TRIV) {
    -- Module Importation
    protecting(NAT)
    -- Sorts, Sub-sort Relations
    [Elt.X < Set]
    -- Operators
    op empty : -> Set {constr}
    op _ _ : Set Set -> Set {constr assoc comm idem id: empty}
    op #_ : Set -> Nat
    op _U_ : Set Set -> Set
    pred _\in_ : Elt.X Set
    op _A_ : Set Set -> Set
    op _\\_ : Set Set -> Set
```

¹CafeOBJ modules can be classified into tight modules and loose modules. Roughly speaking, a tight module denotes a unique model, while a loose module denotes a class of modules. Those are declared with module! and module* respectively.

²In CafeOBJ, a comment starts with -- or ** to the end of the line.

```
pred subset : Set Set
  -- Variables
  vars S S1 S2 : Set
  vars E E1 : Elt.X
  -- Equations
  -- for =
  eq ((E S1) = (E S2)) = (S1 = S2).
  -- for empty
  eq ((E S) = empty) = false.
  -- for #_
  eq \# empty = \emptyset .
  eq # (E S) = 1 + (# S).
  -- for _U_
  eq S1 U S2 = S1 S2.
  -- for _\in_
  eq E \ in empty = false.
  eq E \setminus in (E S) = true .
  ceq E in (E1 S) = E in S if not(E = E1).
  -- for _A_
  eq empty A S2 = empty.
  eq (E S1) A (E S2) = E (S1 A S2).
  ceq (E S1) A S2 = S1 A S2 if not(E \setminus in S2).
  -- for _\\_
  eq empty \setminus E = empty.
  eq (E S) \setminus E = S.
  ceq (E1 S) \setminus E = (E1 (S \setminus E)) if not (E = E1).
  -- for subset
  eq subset(empty,S) = true .
  eq subset((E S1),S2) = E \setminus in S2 and subset(S1,S2).
}
```

This module specifies generic sets and has one parameter **X** constrained by the built-in module TRIV in which one sort Elt is only declared as follows:

```
module* TRIV {
   [Elt]
}
```

The sort is referred by Elt.X and used for elements in SET. The built-in module NAT in which natural numbers are specified is imported with protecting. Modules also can be imported with extending and using; protecting means that elements of the imported modules should not be added nor collapsed; extending means that they can only be added but not be collapsed; and using means they can be added and collapsed.

One sort Set is declared and it is also declared that Elt.X is a sub-sort of Set. This is why an element is also a singleton set that only consists of the element. An operator without arguments is a *constant* and an operator which is not defined by any equations is a *constructor*. The operator empty is a constant of Set and the juxtaposition operator $_$ is a constructor of Set, where an underscore is the place where an argument is put. It is also specified that the juxtaposition operator is associative, commutative, and idempotent and has empty as its identity. Operators are defined with equations. The first equation specifies that # empty equals 0, and the second one specifies that # (E S) equals 1 + (# S). Those two equations define operator $\#_{-}$ that counts the number of the elements in a given set. Operators $_U_{-}$, $__\in_{-}$, A_{-} , $__\in_{-}$, and subset are defined which mean union(\cup), membership(\in), intersection(\cap), difference(\setminus), and inclusion(\subseteq) of sets respectively. Note that "pred Op : Sort1 Sort2" is an abbreviation for "op Op : Sort1 Sort2 -> Bool."

Parameterized modules can be instantiated together with modules as actual parameters through views. Let us consider the following module as an actual parameter of Set:

```
module! SERVICE {
  protecting(NAT)
  [LocalState Service]
  ops closed open ready : -> LocalState {constr}
  op sv : Nat LocalState -> Service {constr}
}
```

in which two sorts are declared. A term of sort LocalState represents a local state of a service and there are three constants of local states (closed, open, and ready). A term of sort Service represents a service which has a form sv(n,lst) where n is some natural number as an identifier and lst is one of local states. SET can be instantiated as SV-SET as follows:

```
module! SV-SET {
  protecting(
    SET(SERVICE{sort Elt -> Service})
    * {sort Set -> SvSet,
        op empty -> empSvSet})
}
```

What follows SERVICE, namely {sort Elt -> Service}, is a *view* used here saying that Elt is replaced with Service in the instantiation of SET with SERVICE. What follows * is renaming. Set and empty are renamed as SvSet and empSvSet, respectively. Other operators are used without renaming. The instantiated SET with SERVICE in which Set and empty are renamed as mentioned is imported with protecting in SV-SET. In this case, SET is called a *template module* and TRIV is called a *parameter module*. Note that a template module is not always a parameterized module. Template modules with no parameters will be explained in Section 5.1.

Command open make a given module, SV-SET in this case, available.

```
open SV-SET .
reduce #(sv(1,closed) sv(2,open)) . -- to 2.
op svs : -> SvSet .
reduce #(sv(1,closed) svs) = # svs + 1 . -- to true.
close
```

In SV-SET, (sv(1,closed) sv(2,open)) is a term of sort SvSet and represents a set of services consists of two elements. Thereby, #(sv(1,closed) sv(2,open)) is a term of Nat which reduces to 2 using equations of SET as left-to-right rewrite rules. When svs is a term of sort SvSet, (sv(1,closed) svs) is also a term of sort SvSet which represents a set of services including at least one closed service where svs represents the rest of the set. Thus, #(sv(1,closed) svs) reduces to # svs + 1.

3.2 Transition Rules

Let us consider the following module:

```
module! UPDATE {
  using(SV-SET)
  [State]
  op < _ > : SvSet -> State {constr}
  var SVS : SvSet
  var N : Nat
  trans [c2o]:
    < sv(N,closed) SVS > => < sv(N,open) SVS > .
  ctrans [o2r]:
    < sv(N,open) SVS > => < sv(N,ready) SVS >
    if # SVS > 0 .
}
```

Module UPDATE specifies a *state machine*. We say a "global state" as a state of the state machine in order to avoid the confusion with local states of services. A ground term of sort State represents a global state consisting of a set of services, where the set { < svs > | svs is a ground term of SvSet} represents the state space. Two transition rules, labeled by c2o and o2r, define the state transition over the global states. Transition rule c2o specifies that a closed service appearing in a global state is changed to open, and o2r specifies that an open service is changed to ready if there is at least one other service, where ctrans means "conditional trans".

Command select is similar to open except that it does not allow to declare new sorts, operators, equations, and so on. Command execute makes CafeOBJ try to apply transition rules until no one can be applied.

```
select UPDATE .
execute < sv(1,closed) sv(2,open) > .
    -- to < sv(1,ready) sv(2,ready) > .
execute < sv(1,closed) > .
    -- to < sv(1,open) > .
```

Rule c2o makes state < sv(1,closed) sv(2,open) > transit to < sv(1,open) sv(2,open) > then rule o2r makes transit it to < <math>sv(1,ready) sv(2,open) > and successively makes it transit to < <math>sv(1,open) sv(2,open) > . On the other hand, only rule c2o can be applied to global state < sv(1,closed) > because it has only one element.

3.2.1 Formalization of State Machines in CafeOBJ

This section summarizes the formal definitions of state machines in CafeOBJ. Please refer to [10] for detailed definitions.

Definition 1 [transition rule] Let State be a sort of global states, l and r terms of sort State, and let c be a term of sort Bool, then a triple R = [l, r, c] is called a <u>transition rule</u> and represented as "ctrans $l \Rightarrow r$ if c." (or "trans $l \Rightarrow r$." when c is true).

Definition 2 [transition] Let *St* be a set of global states (i.e. ground terms of sort State), and let *Rule* be a set of transition rules, then a pair of global states $(S, S') \in Tr \subseteq St \times St$ is called a transition specified by *Rule* iff there exists a transition rule $R = [l, r, c] \in Rule$ and some ground substitution σ such that $S = l\sigma$, $S' = r\sigma$, and $c\sigma$ reduces to *true*. We also say *R* can be applied to *S* and say *S'* is a <u>next state</u> of *S*.

Definition 3 [state machine] Let *Rule* be a set of transition rules, then a <u>state machine</u> is a triple (St, Tr, In) where *St* is a set of global state, $Tr \subseteq St \times St$ is a set of transitions specified by *Rule*, and $In \subseteq St$. An element of *In* is called an <u>initial state</u>.

Definition 4 [transition sequence] Let (St, Tr, In) be a state machine, then a transition sequence is a sequence of global states (S_0, S_1, \ldots, S_n) where each adjacent pair $(S_i, S_{i+1}) \in Tr$.

Notation 1 $[S\alpha, \alpha S, \alpha\beta]$ Let *S* be a global state, and let $\alpha = (S_0, S_1, \dots, S_n)$ be a transition sequence, then $\underline{S\alpha}$ is the transition sequence such that $S\alpha = (S, S_0, S_1, \dots, S_n)$. $\underline{\alpha S}$ is the transition sequence such that $\alpha S = (S_0, S_1, \dots, S_n, S)$. Let $\alpha = (S_0, S_1, \dots, S_n)$ and $\beta = (S_{n+1}, S_{n+2}, \dots, S_{n+m})$ be transition sequences, then $\underline{\alpha\beta}$ is the transition sequence such that $\alpha\beta = (S_0, S_1, \dots, S_n, S_{n+1}, S_{n+2}, \dots, S_{n+m})$.

Definition 5 [reachable] Let (St, Tr, In) be a state machine, then a global state $S \in St$ is reachable iff there exists a transition sequence $(S_0, S_1, ..., S_n)$ where $S_0 \in In$ and $S = S_n$. Note that $S_0 \in In$ is reachable because (S_0) is a transition sequence with n = 0.

Definition 6 [invariant] Let (St, Tr, In) be a state machine, then a global state predicate p is an invariant iff p(S) = true holds for any reachable global state S.

3.3 Search Predicates

What is called *search predicates* can be used to conduct reachability analysis for such state machines specified in CafeOBJ :

```
pred _=(*,1)=>+_ : State State
pred _=(*,1)=>+_if_suchThat_{_} : State State Bool Bool Info
```

Let us consider the following code fragment:

```
select UPDATE .
reduce < sv(1,closed) sv(2,open) > =(*,1)=>+ < SVS > . -- to true.
reduce < sv(3,closed) sv(4,ready) > =(*,1)=>+ < SVS > . -- to true.
reduce < sv(5,open) > =(*,1)=>+ < SVS > . -- to false.
```

By reducing the term in the code fragment, CafeOBJ finds any next states of the given global state, such as $< sv(1, open) >^3$. The first reduction returns true because both transition rules are applicable. The second one also returns true but only rule c2o is applicable. The third one returns false.

CafeOBJ can find next states of a given global state such that some conditions hold in those next states. Let us consider the following code fragment⁴:

³*, 1, and + specify the range of search. If 2 is used instead of *, CafeOBJ tries to find at most two next states. If 3 is used instead of 1, CafeOBJ finds all of the global states reachable from the given global state with at most three state transitions. If * is used instead of +, CafeOBJ also includes the given global state as a search target. Only = (*, 1) =>+ is used in this dissertation.

⁴Since the final part of the reduce sentence, { true }, is for debugging, please ignore it.

```
open UPDATE .
pred anyOpen : SvSet .
eq anyOpen(sv(N,open) SVS) = true .
var CC : Bool .
reduce
< sv(1,closed) sv(2,open) > =(*,1)=>+ < SVS > if CC
suchThat CC implies anyOpen(SVS) { true } . -- to true.
```

The reduction returns true in which CafeOBJ finds any next states of the given global state such that at least one open service is appearing. In this case, transition rule c20 makes such next state. Note that when the conditional search predicate tries a transition rule, it binds the rule's condition to Boolean variable CC placed at if clause. The suchThat clause uses CC to check anyOpen(SVS) only when the rule is applied.

On the other hand, when we want to check some condition holds in all of the possible next states, we need some trick. The following code fragment checks whether all of the possible next states of global state < sv(1,closed) sv(2,open) > include at least one open services:

This style of coding is we call the *double negation idiom* because it returns true when it CAN-NOT find any next states of the given global state such that NO open service is appearing. The reduction proceeds as follows:

- 1. Try to match LHS of c2o to the given global state.
- 2. Also try to match the rule's condition (i.e. true because the rule is unconditional) to CC and the substituted RHS (i.e. < sv(1,open) sv(2,open) >) to < SVS >.
- 3. Evaluate the substituted suchThat clause which reduces to false because anyOpen(sv(1,open) sv(2,open)) reduces to true.
- 4. Then, continuing the search to find a next state where the suchThat clause holds, try to match LHS of o2r to the given global state, the condition (i.e. # SVS > 0) to CC, and the substituted RHS (i.e. < sv(2,ready) sv(1,closed) >) to < SVS >.
- 5. Evaluate the substituted suchThat clause which reduces to true because sv(2,ready) sv(1,closed) does not include any open services.
- 6. Then the search predicate returns true and the whole term reduces to false.

This means that there is a next states of global state < sv(1,closed) sv(2,open) > which does not include any open services; that is global state < sv(1,closed) sv(2,ready) >.

Note that this is a typical example where we need $_ == true$. In CafeOBJ, term1 == term2 reduces to true if both terms are reduced to be the same term and to false otherwise. On the other hand, term1 = term2 reduces to true iff term1 == term2 reduces to true. The following code fragment shows difference between $_ = _$ and $_ == _$.

In this case, CafeOBJ cannot decide anyOpen(SVS) does or does not hold because the definition of anyOpen is incomplete and thus the first reduction above can reduce to neither true nor false. The second one using _ == true reduces to false, which is the reason why suchThat clause in the double negation idiom works as we intended.

3.3.1 Formalization of Search Predicates

This section describes the search predicates more formally.

Definition 7 [unconditional search predicate] Let *Rule* be a set of transition rules, and let *S* and *S'* be terms of sort State. The unconditional search predicate, FS(S, S') is represented as "S =(*,1)=>+ *S'*" and holds iff there exists a transition rule $R = [l, r, c] \in Rule$ and a substitution σ such that $S\sigma = l\sigma$ holds, $S'\sigma = r\sigma$ holds, and $c\sigma$ reduces to true.

Definition 8 [conditional search predicate] Let *Rule* be a set of transition rules, *S* and *S'* terms of sort State, and *CC* and *B* terms of sort Bool. The conditional search predicate, CFS(S, S', CC, B) is represented as "S = (*, 1) = + S' if *CC* such That $B \{ debug_{info} \}$ " and holds iff there exists a transition rule $R = [l, r, c] \in Rule$ and a substitution σ such that $S\sigma = l\sigma$ holds, $S'\sigma = r\sigma$ holds, $CC\sigma = c\sigma$ holds, and $B\sigma$ reduces to true. *B* typically has a form "*CC* implies p(S, S')" where p(S, S') is a predicate of global states.

3.4 Verification by Proof Scores

A *proof score* is an executable specification in CafeOBJ such that if executed as expected, then the desired theorem is proved [11]. Verification by proof scores is an interactive developing process to think through meaning of the specification that is very important aspect of developing trusted systems.

For example, let us verify that in module UPDATE there should be a next state of global state *S* when at least two services included in *S* are not ready.

```
module! ProofUPDATE {
  protecting(UPDATE)
  -- Theorem to be proved.
  pred theorem : Nat LocalState Nat LocalState SvSet
  vars N N1 N2 : Nat
  vars Lst1 Lst2 : LocalState .
  var SVS : SvSet
  var SVS : SvSet
  var SS : State
  eq theorem(N1,Lst1,N2,Lst2,SVS)
    = ((Lst1 == ready) = false and (Lst2 == ready) = false)
      implies < sv(N1,Lst1) sv(N2,Lst2) SVS > =(*,1)=>+ SS .
  -- Axiom of Nat
  eq (1 + N > 0) = true .
  -- Arbitrary constants.
```

```
ops st1 st2 : -> LocalState
ops n1 n2 : -> Nat
op svs : -> SvSet
}
```

Module **ProofUPDATE** gets ready for verification; it defines the theorem to be proved and declares several arbitrary constants. Note that we require an axiom for natural numbers which says that the successor of a natural number is always greater than 0.

Firstly, we begin with the most general case where all the aruguments of theorem are arbitrary constants:

```
-- The most general case.
open ProofUPDATE .
reduce theorem(n1,st1,n2,st2,svs) . -- to false.
close
```

This case is too general for CafeOBJ to find any next states. We should split the case into cases which collectively cover the general case. There are three case; (1) both services are closed, (2) both services are open, and (3) one service is closed and another is open. The following is a proof score for the three cases.

```
-- Case 1: Both services are closed.
open ProofUPDATE .
eq st1 = closed .
eq st2 = closed .
reduce theorem(n1,st1,n2,st2,svs) . -- to true.
close
-- Case 2: Both services are open.
open ProofUPDATE .
eq st1 = open .
eq st2 = open .
reduce theorem(n1,st1,n2,st2,svs) . -- to true.
close
-- Case 3: A closed service and an open service.
open ProofUPDATE .
eq st1 = closed .
eq st2 = open .
reduce theorem(n1,st1,n2,st2,svs) . -- to true.
close
```

Verification is successfully done because all of the cases collectively covering the most general case are proved.

3.5 Constructor-based Inductive Theorem Prover (CITP)

As described above, interactive theorem proving is a systematic process to split general cases into collectively covering cases until all of the cases are specific enough to be proved. Thereby, a proof score should be written more carefully when case splitting becomes deeper. It sometimes causes to carelessly forget some cases to be proved. In fact, it may take considerable time to convince that the three cases in the previous section collectively cover all of the cases.

In order to assist to develop proof scores which are more systematic and easier to understand, CafeOBJ provides CITP method consisting of several special commands. The following is a list of part of CITP commands⁵:

- :goal { eq *term* = true . } Define the goal to be proved and let it be the current case. Multiple goal equations can be specified.
- :ctf { eq LHS = RHS . }
 Split the current case into two cases adding eq LHS = RHS . to one case and eq (LHS = RHS) = false . to another.
- :csp { eq $LHS_1 = RHS_1$. eq $LHS_2 = RHS_2$ } Split the current case into cases adding eq $LHS_i = RHS_i$. to each case.
- :apply (rd) Reduce the goal in the current case.
- :def name = :ctf { ... }
 :def name = :csp { ... }
 Name the case splitting tactic.

• :apply (name₁ name₂)

Combine named case splitting tactics. When tactic $name_1$ splits an case into n cases and tactic $name_2$ splits into m cases, the current case is split into totally $n \times m$ cases. It can also specify tactic rd, i.e. :apply $(n_1 \ n_2 \ rd)$, which means reducing the goal in every split case.

- :init [label] by { substitution }
 Introduce a labeled lemma proven by other proof scores. substitution specifies how to unify the lemma to the current case. Detailed examples will be explained in Chapter 6.
- describe proof

Describe the proof tree consisting of split cases. Proven cases are shown by "*" marks.

• show proof

Summarize the proof tree consisting of split cases. Proven cases are shown by "*" marks.

The following is a proof score of CITP version of the example in the previous section:

```
select ProofUPDATE .
:goal {
   eq theorem(n1,st1,n2,st2,svs) = true .
}
:def csp-st1 = :csp {
   eq st1 = closed .
   eq st1 = open .
```

⁵As its name suggests, CITP has capability to automatically produce inductive goals based on constructors, however we use it only for management of proof trees in this dissertation.

```
eq st1 = ready .
}
:def csp-st2 = :csp {
  eq st2 = closed .
  eq st2 = open .
  eq st2 = ready .
}
:apply (csp-st1 csp-st2 rd)
describe proof
```

Firstly, the goal to be proved should represent the most general case where all the aruguments of theorem are arbitrary constants. Then, since class LocalState has only three constants (closed, open, and ready) as constructors in module UPDATE, there are three cases where st1 (and also st2) is one of the three constants in each of cases. Thereby the combination of case splitting for st1 and st2 collectively covers all of the cases.

The final command, describe proof, describes the proof tree as follows:

```
==> root*
    -- context module: #Goal-root
    -- targeted sentence:
      eq theorem(n1, st1, n2, st2, svs) = true .
[csp-st1] 1*
    -- context module: #Goal-1
    -- assumption
      eq [csp-st1]: st1 = closed .
    -- targeted sentence:
      eq theorem(n1, st1, n2, st2, svs) = true .
[csp-st2] 1-1*
    -- context module: #Goal-1-1
    -- assumptions
      eq [csp-st1]: st1 = closed .
      eq [csp-st2]: st2 = closed .
    -- discharged sentence:
      eq [RD]: theorem(n1, st1, n2, st2, svs) = true .
[csp-st2] 1-2*
    -- context module: #Goal-1-2
    -- assumptions
      eq [csp-st1]: st1 = closed .
      eq [csp-st2]: st2 = open .
    -- discharged sentence:
      eq [RD]: theorem(n1, st1, n2, st2, svs) = true .
[csp-st2] 1-3*
    -- context module: #Goal-1-3
    -- assumptions
      eq [csp-st1]: st1 = closed .
      eq [csp-st2]: st2 = ready.
    -- discharged sentence:
      eq [RD]: theorem(n1, st1, n2, st2, svs) = true .
[csp-st1] 2*
    -- context module: #Goal-2
    -- assumption
```

```
eq [csp-st1]: st1 = open .
    -- targeted sentence:
      eq theorem(n1, st1, n2, st2, svs) = true .
[csp-st2] 2-1*
    -- context module: #Goal-2-1
    -- assumptions
      eq [csp-st1]: st1 = open .
      eq [csp-st2]: st2 = closed .
    -- discharged sentence:
      eq [RD]: theorem(n1, st1, n2, st2, svs) = true .
[csp-st2] 2-2*
    -- context module: #Goal-2-2
    -- assumptions
      eq [csp-st1]: st1 = open .
      eq [csp-st2]: st2 = open .
    -- discharged sentence:
      eq [RD]: theorem(n1, st1, n2, st2, svs) = true .
[csp-st2] 2-3*
    -- context module: #Goal-2-3
    -- assumptions
      eq [csp-st1]: st1 = open .
      eq [csp-st2]: st2 = ready.
    -- discharged sentence:
      eq [RD]: theorem(n1, st1, n2, st2, svs) = true .
[csp-st1] 3*
    -- context module: #Goal-3
    -- assumption
      eq [csp-st1]: st1 = ready .
    -- targeted sentence:
      eq theorem(n1, st1, n2, st2, svs) = true .
[csp-st2] 3-1*
    -- context module: #Goal-3-1
    -- assumptions
      eq [csp-st1]: st1 = ready .
      eq [csp-st2]: st2 = closed .
    -- discharged sentence:
      eq [RD]: theorem(n1, st1, n2, st2, svs) = true .
[csp-st2] 3-2*
    -- context module: #Goal-3-2
    -- assumptions
      eq [csp-st1]: st1 = ready .
      eq [csp-st2]: st2 = open.
    -- discharged sentence:
      eq [RD]: theorem(n1, st1, n2, st2, svs) = true .
[csp-st2] 3-3*
    -- context module: #Goal-3-3
    -- assumptions
      eq [csp-st1]: st1 = ready .
      eq [csp-st2]: st2 = ready .
    -- discharged sentence:
```

eq [RD]: theorem(n1, st1, n2, st2, svs) = true .

This means that the most general case (root) is split into three cases (1, 2, and 3) using csp-st1 each of which is also split into three case (for example, 1-1, 1-2, and 1-3) using csp-st2. "*" marks show all of the cases are successfully proved.

Chapter 4

Theorem Proving Framework

The theorem proving framework proposed by this dissertation aims to facilitate interactive proof development by allowing proof developers to devote their time to thinking through meaning of their own specifications and specific reasons why the specifications have some desired properties rather than reinventing how to construct proof scores or proving many specific versions of some common lemmas, thereby reducing overall development time. By doing so, the framework is expected to raise the skill level of novice proof developers and to enable a number of engineers to efficiently develop the proof score for a practical scale problem.

The framework supports developers using mainly two means to reuse proof developments. Firstly, it provides a procedure how to develop proof scores to verify leads-to properties as well as invariant properties of cloud orchestration specifications. For every such property, there are several proof goals all of which should reduce to true. A proof score for each property consists of proof case trees each of which corresponds to one of the proof goal. The root of a proof case tree represents the most general case of the proof goal. When the goal does not reduce to true in the root case, it should be split into more concrete sub-cases which collectively cover the root case. Such case splitting should be continued until all the leaf cases reduce to true and then the proof goal is verified. The proof development procedure provided by the framework prescribes what kind of set of proof goals should be sufficient to verify invariant and leads-to properties of specifications and guides how to split cases to develop proof case trees. The procedure supports proof developers to make the specific proof goals for their own specifications and to proceed case splitting until all the goals reduce to true.

Secondly, the framework provides many reusable lemmas that are commonly used in the course of verification for invariant and leads-to properties of cloud orchestration specifications. The provided lemmas are already proved in a general level of abstraction and can be reused simply by renaming included general terms to some specific ones without reproving. The reason why the framework can provide such a proof development procedure and reusable lemmas for the specific problem domain, cloud orchestration in our case, is because it makes specific specifications adopt a general structure and behavior model for the domain and its representation. Proof developers can describe such specifications only by instantiating logical templates provided by the framework and adding small specific part of codes.

The reusable entities provided by the framework are four kinds of logic templates, a lot of general predicates/operators included in the templates, and a lot of lemmas about such predicates/operators which are proved in the general level of abstraction. The framework also provides general sufficient conditions to verify invariant and leads-to properties of cloud orchestration specifications and provides a procedure to develop proof trees whose goals are the sufficient
conditions.

The rest of this chapter describes the general structure and behavior model and its representation. The reusable entities provided by the framework will be described in Chapter 5 and the proof development procedure will be described in Chapter 6.

4.1 Structure Models and Representations

Cloud Orchestration is automation of operations such as set-up, scale-out, scale-in, or shutdown of cloud systems. In order to verify correctness of an automated operation of a cloud system, we need to model the structure of the target cloud system and the behavior of the operation. We say "model" to mean abstractly and formally specifying the structure and behavior. A specified model is represented by a formal specification language, namely CafeOBJ in this dissertation.

CloudFormation models a structure of a cloud system simply as a set of *resources* on IaaS platform of AWS. The model is called a *template* which is represented by JSON as illustrated in Fig. 2.1. A resource has an identifier and a type and includes several *properties* which may depend on other resources.

On the other hand, TOSCA's model of a cloud system is more structured to manage any types of cloud resources, as well as inside VMs, and any types of operations such as scale-out, scale-in, shutdown, and so on. A TOSCA's model, called a *topology*, is represented by XML as illustrated in Fig 2.7. A topology consists of a set of *nodes* and a set of *relationships* between nodes. A node has several *capabilities* and *requirements*. A relationship relates a requirement of a source node to a capability of a target node.

In order to cover many different kinds of models of cloud system structures, our framework provides a generic model of a cloud system structure which consists of several *classes* of *objects*. For example, in the case of CloudFormation, a cloud system consists of two classes (resource and property) of objects whereas TOSCA models that a cloud system consists of four classes (node, relationship, capability, and requirement). For a while, we explain our framework using the simple CloudFormation template shown in Fig. 2.1 and the case of TOSCA topologies will be explained in Chapter 7.

An object has a *type*¹, an *identifier*(ID), a *local state*, and possibly *links* to other objects. In the case of the example shown in Fig. 2.1, a resource object whose type is AWS::EC2::Instance has its ID as MyInstance. The type of MyEIP resource is AWS::EC2::EIP. MyEIP has a property but its ID is hidden and we assume it is MyEIP::InsID since its parent is MyEIP and its type is InstanceId. MyEIP::InsID has a link to MyInstance. Local states of objects are used for automation of operations, which will be explained in Section 4.2.

An object belongs to a class and thus a class is a set of objects. We assume this set consists of countably infinite objects each of which has its fixed ID and type. Local states or links of objects may be dynamically changed. A class specifies the set of possible types, the set of possible local states of its objects. A class also specifies how its objects link to other objects.

Users of the framework should design representations of the system models in CafeOBJ language. A class should be represented as a CafeOBJ module that defines a sort of its objects, a constructor of the sort, a set of literals of types, and a set of literals of local states. An object is represented as a ground constructor term of the sort.

¹Do not think a *type* is that of programming languages which is called *sort* in CafeOBJ. A type is just an attribute of an object. We use the term because both CloudFormation and TOSCA use it.

For the example shown in Fig. 2.1, three objects may be represented as the following ground terms:

```
res(ec2Instance, myInstance, initial)
res(ec2Eip, myEIP, initial)
prop(instanceId,myEIP::InsID,notready,myEIP,myInstance)
```

Although the user of the framework can freely design the representation of objects, typically the constructor name represents the class of the object (res, prop), the first argument is its type (ec2Instance, ec2Eip, instanceId), the second is its identifier (myInstance, myEIP, myEIP::InsID)², and the third is its local state. The fourth argument of the property object represents a link to its parent, myEIP, and the fifth represents that the property depends on myInstance. The example of CafeOBJ modules representing resource and property classes will be shown in Chapter 5. Note that a link is represented by an identifier of the linked object in our framework.

4.2 Behavior Models and Representations

The framework models the behavior of an automated operation of a cloud system as a state transition system in which a set of *transition rules* of states specifies the behavior. We say a *global state* as a state of the state machine in order to avoid the confusion with local states of objects. A global state is a finite set of objects each of which is included in some class. A transition rule makes a global state transit to another global state where local states or links of some objects are changed.

In the case of a template of CloudFormation, a global state consists of finite number of resources and their properties. CloudFormation tries to start all of the resources according to the dependency specified by the template. In this dissertation, we use a very simple behavior model of CloudFormation as an example; a local state of a resource is firstly *initial* and becomes *started* but a dependent resource can be *started* after all of the resources it depends become *started*. The dependency is specified such that a property linking some resource is firstly *notready* and becomes *ready* when the linked resource is *started* and a resource can be *started* when all of its properties become *ready*. Figure 4.1 illustrates the model where solid arrows show changes of local states and dashed arrows show transition rules.



Figure 4.1: Simple Behavior Model of CloudFormation

 $^{^{2}}$ In this dissertation, we often use an identifier to designate an object which has the identifier for the sake of brevity.

A global state is represented in CafeOBJ as a ground constructor term of sort State, which is typically a tuple of sets of objects, each of the sets is a finite subset of a class. In the case of CloudFormation, sort State is defined as a pair of a set of resources and a set of properties as follows:³

```
module! STATE {
    protecting(LINKS)
    [State]
    op <_,_> : SetOfResource SetOfProperty -> State {constr}
}
```

The global state shown in Fig. 2.1 is represented as follows:

```
open STATE .
    -- Constants
    ops ec2Instance ec2Eip : -> RSTypeLt .
    ops myInstance myEIP : -> RSIDLt .
    ops myEIP::InsID : -> PRIDLt .
    op instanceId : -> PRTypeLt .
    op s0 : -> State .
    eq s0 =
      < (res(ec2Instance, myInstance, initial)
          res(ec2Eip, myEIP, initial)),
          (prop(instanceId, myEIP::InsID, notready, myEIP, myInstance)) >
```

The behavior is modeled and represented by a set of two transition rules as follows:

```
module! STATERules {
 protecting(STATEfuns)
 -- Variables
 vars IDRS IDRRS : RSID
 var IDPR : PRID
 var TRS : RSType
 var TPR : PRType
 var SetRS : SetOfResource
 var SetPR : SetOfProperty
 -- Start an initial resource
 -- if all of its properties are ready.
 ctrans [R01]:
    < (res(TRS, IDRS, initial) SetRS), SetPR >
 => < (res(TRS,IDRS,started) SetRS), SetPR >
    if allPROfRSInStates(SetPR,IDRS,ready) .
 -- Let a not-ready property be ready
 -- if its referring resource is started.
 trans [R02]:
    < (res(TRS, IDRRS, started) SetRS),
      (prop(TPR, IDPR, notready, IDRS, IDRRS) SetPR) >
```

³Module LINKS and several sorts of constants will be explained in the next chapter.

Predicate allPROfRSInStates(SetPR, IDRS, ready) checks a set of properties SetPR whether every property of resource IDRS is ready, which will be explained in Section 5.2. Thus, rule R01 means that an initial resource becomes started when all of its properties are ready. The LHS of rule R02 includes a resource and a property. The second link of the property is the identifier of the resource, which means the property refers the resource. Thereby, rule R02 means that a notready property becomes ready when it refers a started resource.

4.3 Simulation of Models

CafeOBJ provides execute command to execute a state machine trying to apply transition rules as long as possible.

```
open STATERules .
-- Constants
ops ec2Instance ec2Eip : -> RSTypeLt .
ops myInstance myEIP : -> RSIDLt .
ops myEIP::InsID : -> PRIDLt .
op instanceId : -> PRTypeLt .
op s0 : -> State .
eq s0 =
   < (res(ec2Instance, myInstance, initial)
      res(ec2Eip,myEIP,initial)),
     (prop(instanceId,myEIP::InsID,notready,myEIP,myInstance)) > .
execute s0 .
-- will be produced
 -- < (res(ec2Instance, myInstance,started)</pre>
       res(ec2Eip,myEIP,started)),
 ___
      (prop(instanceId,myEIP::InsID,ready,myEIP,myInstance)) > .
 _ _
```

The followings are part of log messages of the execution above, which shows that firstly rule R01 makes myInstance transit from *initial* to *ready*, then R02 makes myEIP::InsID transit from *notready* to *ready*, and finally R01 makes myEIP transit from initial to *started*.

```
1>[19] match success #1
1<[19] (< (res(ec2Eip,myEIP,initial) res(ec2Instance,myInstance,initial)),</pre>
          (prop(instanceId,myEIP::InsID,notready,myEIP,myInstance)) >)
   --> (< (res(ec2Instance,myInstance,started) res(ec2Eip,myEIP,initial)),
          (prop(instanceId,myEIP::InsID,notready,myEIP,myInstance)) >)
1>[20] rule: trans [R02]:
          (< (res(TRS,IDRRS,started) SetRS),</pre>
             (prop(TPR, IDPR, notready, IDRS, IDRRS) SetPR) >)
       => (< (res(TRS, IDRRS, started) SetRS),
             (prop(TPR,IDPR,ready,IDRS,IDRRS) SetPR) >)
    { IDPR |-> myEIP::InsID,
      TPR |-> instanceId,
      IDRS |-> myEIP,
      SetPR |-> empPR,
      IDRRS |-> myInstance,
      TRS |-> ec2Instance,
      SetRS |-> res(ec2Eip,myEIP,initial)
1<[20] (< (res(ec2Eip,myEIP,initial) res(ec2Instance,myInstance,started)),</pre>
          (prop(instanceId,myEIP::InsID,notready,myEIP,myInstance)) >)
   --> (< (res(ec2Instance,myInstance,started) res(ec2Eip,myEIP,initial)),
          (prop(instanceId,myEIP::InsID,ready,myEIP,myInstance)) >)
1>[21] apply trial #1
. . .
1>[42] match success #1
1<[42] (< (res(ec2Eip,myEIP,initial) res(ec2Instance,myInstance,started)),</pre>
          (prop(instanceId,myEIP::InsID,ready,myEIP,myInstance)) >)
   --> (< (res(ec2Eip,myEIP,started) res(ec2Instance,myInstance,started)),
          (prop(instanceId,myEIP::InsID,ready,myEIP,myInstance)) >)
```

(< (res(ec2Instance,myInstance,started) res(ec2Eip,myEIP,started)),
 (prop(instanceId,myEIP::InsID,ready,myEIP,myInstance)) >):State

Chapter 5

General Templates and Predicate Libraries

The framework uses the template mechanism of CafeOBJ to provide a general way to model cloud orchestration, predefined predicate libraries, and proved lemmas together with their proof scores.

5.1 Template Modules of Objects

Template module OBJECTBASE defines nine sorts and more than ten operators/predicates of objects, which generally and minimally defines what an object is in a class. The template can be instantiated and imported in a module for each class of objects, where the imported sorts and operators can be used just by renaming appropriately. For the example shown in Fig. 2.1, following module RESOURCE describes specifications of the resource class for CloudFormation¹.

```
module! RESOURCE {
  -- Instantiation of Template
  extending(OBJECTBASE
    * {sort Object -> Resource,
       sort ObjIDLt -> RSIDLt,
       sort ObjID -> RSID,
       sort ObjTypeLt -> RSTypeLt,
       sort ObjType -> RSType,
       sort ObjStateLt -> RSStateLt,
       sort ObjState -> RSState,
       sort SetOfObject -> SetOfResource,
       sort SetOfObjState -> SetOfRSState,
       op empObj -> empRS,
       op empState -> empSRS,
       op existObj -> existRS,
       op existObjInStates -> existRSInStates,
       op uniqObj -> uniqRS,
       op #ObjInStates -> #ResourceInStates,
       op getObject -> getResource,
```

¹OBJECTBASE is a template with no parameter and is used to instantiate a new module and to rename predefined sorts/operators.

```
op allObjInStates -> allRSInStates,
      op allObjNotInStates -> allRSNotInStates,
      op someObjInStates -> someRSInStates}
 )
  -- Constructor
  -- res(RSType, RSID, RSState) is a Resource.
 op res : RSType RSID RSState -> Resource {constr}
  -- Variables
 var TRS : RSType
  var IDRS : RSID
  var SRS : RSState
  -- Selectors
 eq type(res(TRS,IDRS,SRS)) = TRS .
 eq id(res(TRS,IDRS,SRS)) = IDRS .
  eq state(res(TRS,IDRS,SRS)) = SRS .
  -- Local States
 ops initial started : -> RSStateLt {constr}
}
```

The following is a list of nine sorts predefined by template module OBJECTBASE:

- Object (renamed as Resource in this case) Sort for objects themselves.
- ObjIDLt (as RSIDLt)
 Subsort of ObjID for identifier literals. A literal is a constant for which OBJECTBASE predefines a special equality predicate such that _ = _ is exactly the same as _ == _ .
- ObjID (as RSID) Sort for identifiers of objects.
- ObjTypeLt (as RSTypeLt) Subsort of ObjType for type literals.
- ObjType (as RSType) Sort for types of objects.
- ObjStateLt (as RSStateLt) Subsort of ObjState for local state literals.
- ObjState (as RSState) Sort for local states of objects.
- SetOfObject (as SetOfResource) Soft for sets of objects.
- SetOfObjState (as SetOfRSState) Sort for sets of local states of objects.

The following is a list of part of operators predefined by template module OBJECTBASE whereas argument *obj* is an object, *id* is an identifier of an object, *seto* is a set of objects, and *setls* is a set of local states of objects:

- empObj (renamed as empRS in this case) Constant representing an empty set of objects.
- empState (as empSRS) Constant representing an empty set of local states of objects.
- existObj (as existRS)
 Predicate used as existObj(*seto*,*id*) which holds iff some object with identifier *id* is included in *seto*;

 $\exists o \in seto : id(o) = id.$

• existObjInStates (as existRSInStates) Predicate used as existObjInStates(*seto*,*id*,*setls*) which holds iff some object with identifier *id* is included in *seto* and its local state is included in *setls*;

 $\exists o \in seto : (id(o) = id \land state(o) \in setls).$

• uniqObj (as uniqRS)

Predicate used as uniqObj(*seto*) which holds iff the identifier of each object is unique in *seto*;

 $\forall o, o' \in seto : (o \neq o' \rightarrow id(o) \neq id(o')).$

- #0bjInStates (as #ResourceInStates) Operator used as #0bjInStates(*setls*, *seto*) which returns the number of objects in *seto* whose local states are included in *setls*.
- getObject (as getResource) Operator used as getObject(*seto*,*id*) which returns an object in *seto* whose identifier is *id*.
- allObjInStates (as allRSInStates)
 Predicate used as allObjInStates(*seto*, *setls*) which holds iff the local states of all the objects in *seto* are included in *setls*;
 ∀o ∈ *seto* : state(o) ∈ *setls*.
- allObjNotInStates (as allRSNotInStates)
 Predicate used as allObjNotInStates(*seto*, *setls*) which holds iff the local states of all the objects in *seto* are not included in *setls*;
 ∀o ∈ *seto* : state(o) ∉ *setls*.
- someObjInStates (as someRSInStates)
 Predicate used as someObjInStates(*seto*, *setls*) which holds iff there exists an objects in *seto* whose local state is included in *setls*;

 $\exists o \in seto : state(o) \in setls.$

The module importing the instantiated template can extend it to freely define a constructor of objects and local state literals. In this case, module RESOURCE defines a constructor (res) of

sort **Resource** whose arguments are a type, an identifier, and a local state of the resource. It also defines two local state literals, initial and started, of a resource.

In addition, the module should implement three selector operators, type, id, and state, each of which takes a resource as an argument and returns the type, the identifier, and the local state of the resource respectively and OBJECTBASE uses them to implement the predefined general operators².

Similarly, following module PROPERTY specifies the property class for the example shown in Fig. 2.1.

```
module! PROPERTY {
  protecting(RESOURCE)
  -- Instantiation of Template
  extending(OBJECTBASE
    * {sort Object -> Property,
       sort ObjIDLt -> PRIDLt,
       sort ObjID -> PRID,
       sort ObjTypeLt -> PRTypeLt,
       sort ObjType -> PRType,
       sort ObjStateLt -> PRStateLt,
       sort ObjState -> PRState,
       sort SetOfObject -> SetOfProperty,
       sort SetOfObjState -> SetOfPRState,
       op empObj -> empPR,
       op empState -> empSPR,
       op existObj -> existPR,
       op existObjInStates -> existPRInStates,
       op uniqObj -> uniqPR,
       op #ObjInStates -> #PropertyInStates,
       op getObject -> getProperty,
       op allObjInStates -> allPRInStates,
       op allObjNotInStates -> allPRNotInStates,
       op someObjInStates -> somePRInStates}
  )
  -- Constructor
  -- prop(PRType, PRID, PRState, RSID, RSID) is a Property.
  op prop : PRType PRID PRState RSID RSID -> Property {constr}
  -- Variables
  var TPR : PRType
  var IDPR : PRID
  var SPR : PRState
  vars IDRS1 IDRS2 : RSID
  -- Selectors
  op parent : Property -> RSID
  op refer : Property -> RSID
  eq type(prop(TPR, IDPR, SPR, IDRS1, IDRS2)) = TPR .
```

²OBJECTBASE declares and uses these operators and so RESOURCE only should define them by equations.

```
eq id(prop(TPR,IDPR,SPR,IDRS1,IDRS2)) = IDPR .
eq state(prop(TPR,IDPR,SPR,IDRS1,IDRS2)) = SPR .
eq parent(prop(TPR,IDPR,SPR,IDRS1,IDRS2)) = IDRS1 .
eq refer(prop(TPR,IDPR,SPR,IDRS1,IDRS2)) = IDRS2 .
-- Local States
ops notready ready : -> PRStateLt {constr}
}
```

Module PROPERTY imports module RESOURCE using protecting because a property object links to its parent resource and also links to its referring resource.

Module PROPERTY defines a constructor (prop) of sort Property whose arguments are a type, an identifier, a local state, and links of the property. As noted before, a link is represented by an identifier of the linked object. It also defines two local state literals, notready and ready, of a property.

In addition to the mandatory selectors (type, id, and state), module PROPERTY declares and defines two more selectors, parent and refer, each of which returns a parent resource and a referring resource of the property respectively.

5.2 Template Modules for Links

In addition to the operators provided by template module OBJECTBASE, two template modules OBJLINKMANY2ONE and OBJLINKONE2ONE provide many predefined operators/predicates for links between objects. Representing object structures by using links, instead of nesting structures, enables the framework to be easily applied to any kinds of model structures and to effectively provide a predefined set of operators/predicates.

A template module OBJLINKMANY2ONE takes one parameter module of a class whose object links to another object. In order to provide predefined operators for links, the template module assumes that the parameter module defines eleven specific sorts and five specific operators. For example, it assumes that a parameter module defines Object as a sort for linking objects, LObject as a sort for linked objects, link as a selector of Object which returns the identifier of linked object, and so on. When the actual parameter module defines those sorts and operators with the different names from ones assumed, CafeOBJ allows to specify correspondence of the names. In the case of CloudFormation, the sort for linking objects is Property, the sort for linked objects is Resource, and the selectors are parent and refer defined by module PROPERTY. The following module LINKS imports OBJLINKMANY2ONE twice for both kinds of links specifying the correspondence of the names:

```
module! LINKS {
    -- A Property links to its parent Resource
    extending(OBJLINKMANY2ONE(
        PROPERTY {sort Object -> Property,
            sort ObjID -> PRID,
            sort ObjType -> PRType,
            sort ObjState -> PRState,
            sort SetOfObject -> SetOfProperty,
            sort SetOfObjState -> SetOfPRState,
            sort LObject -> Resource,
            sort LObjID -> RSID,
```

```
sort LObjState -> RSState,
            sort SetOfLObject -> SetOfResource,
            sort SetOfLObjState -> SetOfRSState,
            op link -> parent,
            op empLObj -> empRS,
            op existLObj -> existRS,
            op existLObjInStates -> existRSInStates,
            op getLObject -> getResource}
  )
  * {op hasL0bj -> hasParent,
     op getXOfZ -> getRSOfPR,
     op getZsOfX -> getPRsOfRS,
     op getZsOfXInStates -> getPRsOfRSInStates,
     op getXsOfZs -> getRSsOfPRs,
     op getXsOfZsInStates -> getRSsOfPRsInStates,
     op getZsOfXs -> getPRsOfRSs,
     op getZsOfXsInStates -> getPRsOfRSsInStates,
     op allZHaveX -> allPRHaveRS,
     op allZOfXInStates -> allPROfRSInStates,
     op ifOfXThenInStates -> ifOfRSThenInStates.
     op ifXInStatesThenZInStates -> ifRSInStatesThenPRInStates}
)
-- A Property links to its referring Resource
extending(OBJLINKMANY2ONE(
  PROPERTY {sort Object -> Property,
            sort ObjID -> PRID,
            sort ObjType -> PRType,
            sort ObjState -> PRState,
            sort SetOfObject -> SetOfProperty,
            sort SetOfObjState -> SetOfPRState,
            sort LObject -> Resource,
            sort LObjID -> RSID,
            sort LObjState -> RSState,
            sort SetOfLObject -> SetOfResource,
            sort SetOfLObjState -> SetOfRSState,
            op link -> refer,
            op empLObj -> empRS,
            op existLObj -> existRS,
            op existLObjInStates -> existRSInStates,
            op getLObject -> getResource}
  )
  * {op hasLObj -> hasRefRS,
     op getXOfZ -> getRRSOfPR,
     op getZsOfX -> getPRsOfRRS,
     op getZsOfXInStates -> getPRsOfRRSInStates,
     op getXsOfZs -> getRRSsOfPRs,
     op getXsOfZsInStates -> getRRSsOfPRsInStates,
     op getZsOfXs -> getPRsOfRRSs,
     op getZs0fXsInStates -> getPRs0fRRSsInStates,
```

```
op allZHaveX -> allPRHaveRRS,
op allZOfXInStates -> allPROfRRSInStates,
op ifOfXThenInStates -> ifOfRRSThenInStates,
op ifXInStatesThenZInStates -> ifRRSInStatesThenPRInStates}
)
}
```

The following is a list of eleven sorts assumed by module OBJLINKMANY2ONE:

- Object (actually named as Property in this case) Sort for linking objects.
- ObjID (as PRID) Sort for identifiers of linking objects.
- ObjType (as PRType) Sort for types of linking objects.
- ObjState (as PRState) Sort for local states of linking objects.
- SetOfObject (as SetOfProperty) Sort for sets of linking objects.
- SetOfObjState (as SetOfPRState) Sort for sets of local states of linking objects.
- LObject (as Resource) Sort for linked objects.
- LObjID (as RSID) Sort for identifiers of linked objects.
- LObjState (as RSState) Sort for local states of linked objects.
- SetOfLObject (as SetOfResource) Sort for sets of linked objects.
- SetOfLObjState (as SetOfRSState) Sort for sets of local states of linked objects.

The following is a list of five operators assumed by module OBJLINKMANY2ONE whereas argument *obj* is a linking object, *lid* is an identifier of a linked object, *setlo* is a set of linked objects, and *setlls* is a set of local states of linked objects:

- link (actually named as parent and refer in this case) Selector used as link(*obj*) which returns the identifier of the object linked by *obj*.
- empLObj (as empRS) Constant representing an empty set of linked objects.

• existLObj (as existRS)

Predicate used as existLObj(*setlo*,*lid*) which holds iff a linked object with identifier *lid* is included in *setlo*;

 $\exists lo \in setlo : id(lo) = lid.$

- existL0bjInStates (as existRSInStates)
 Predicate used as existL0bjInStates(*setlo*, *lid*, *setlls*) which holds iff a linked object with identifier *lid* is included in *setlo* and its local state is included in *setlls*;
 ∃*lo* ∈ *setlo* : (id(*lo*) = *lid* ∧ state(*lo*) ∈ *setlls*).
- getLObject (as getResource) Operator used as getLObject(*setlo*,*lid*) which returns an object in *setlo* whose identifier is *lid*.

Note that LINKS imports OBJLINKMANY2ONE twice but only selector link is specified differently, parent and refer, and others are the same.

Many operators/predicates between linking (Z) and linked (X) objects are provided. In this case, each of them is twice renamed differently. The following is a list of part of operators predefined by template module OBJLINKMANY2ONE whereas argument *obj* is a linking object, *seto* is a set of linking objects, *setls* is a set of local states of linking objects, *lobj* is a linked object, *lid* is an identifier of a linked object, *setlo* is a set of linked objects, and *setlls* is a set of local states of linked objects.

- hasLObj (renamed as hasParent and hasRefRS in this case)
- Predicate used as hasLObj(*obj*, *setlo*) which holds iff the object linked by *obj* is included in *setlo*;

 $\exists lo \in setlo : id(lo) = link(obj).$

• getX0fZ (as getRS0fPR and getRRS0fPR) Operator used as getX0fZ(*setlo*, *obj*) which returns an object linked by *obj* and included in *setlo*. When there is no such object in *setlo*, what it returns is undefined.

- getZsOfX (as getPRsOfRS and getPRsOfRRS) Operator used as getZsOfX(*seto*, *lobj*) which returns a subset *seto* each of whose element object links to *lobj*.
- getZsOfXInStates (as getPRsOfRSInStates and getPRsOfRRSInStates) Operator used as getZsOfXInStates(*seto*, *lobj*, *setls*) which returns a subset of *seto* each of whose element object links to *lobj* and is in one of local states of *setls*.
- getXsOfZs (as getRSsOfPRs and getRRSsOfPRs) Operator used as getXsOfZs(*setlo*, *seto*) which returns a subset of *setlo* each of whose element object is linked by some object included in *seto*.
- getXsOfZsInStates (as getRSsOfPRsInStates and getRRSsOfPRsInStates) Operator used as getXsOfZsInStates(*setlo*, *seto*, *setlls*) which returns a subset of *setlo* each of whose element object is linked by some object included in *seto* and is in one of local states of *setlls*.

- getZsOfXs (as getPRsOfRSs and getPRsOfRRSs) Operator used as getZsOfXs(*seto*, *setlo*) which returns a subset of *seto* each of whose element object links to some object included in *setlo*.
- getZsOfXsInStates (as getPRsOfRSsInStates and getPRsOfRRSsInStates) Operator used as getZsOfXsInStates(*seto*, *setlo*, *setls*) which returns a subset of *seto* each of whose element object links to some object included in *setlo* and is in one of local states of *setls*.
- allZHaveX (as allPRHaveRS and allPRHaveRRS)
 Predicate used as allZHaveX(*seto*, *setlo*) which holds iff every object included in *seto* has objects linked by it which are included in *setlo*;
 ∀o ∈ seto, ∃lo ∈ setlo : id(lo) = link(o).
- allZOfXInStates (as allPROfRSInStates and allPROfRRSInStates)
 Predicate used as allZOfXInStates(*seto*, *lid*, *setls*) which holds iff every object included in *seto* whose link is *lid* is in one of locals state in *setls*;
 ∀o ∈ seto : (link(o) = lid → state(o) ∈ setls).
- ifOfXThenInStates (as ifOfRSThenInStates and ifOfRRSThenInStates)
 Predicate used as ifOfXThenInStates(*obj*, *lid*, *setls*) which holds iff the link of *obj* is not *lid* or the local state of *obj* is included in *setls*;
 link(*obj*) = *lid* → state(*obj*) ∈ *setls*.

• ifXInStatesThenZInStates

(as ifRSInStatesThenPRInStates and ifRRSInStatesThenPRInStates) Predicate used as ifXInStatesThenZInStates(*setlo*, *setls*, *seto*, *setls*) which holds iff every object included in *setlo* whose local sate is included in *setlls* is linked by objects included in *seto* each of which is in one of local states in *setls*;

 $\forall lo \in setlo : (state(lo) \in setlls \rightarrow \\ \forall o \in seto : (link(o) = id(lo) \rightarrow state(o) \in setls)).$

Similarly module OBJLINKONE2ONE provides predicates for one to one relationships between objects, which will be explained in Section 7.1.1.

5.3 Proved Lemmas for Predefined Predicates

In the course of verification, a lot of lemmas about predefined predicates are commonly required. The framework provides many typical lemmas which are already proved in a general level of abstraction and can be used for any instantiated predicates without individual reproving. Most of proved lemmas provided together with proof scores written in CafeOBJ.

5.3.1 Basic Lemmas

Lemma 1 (**Implication Lemma**) Let A and B be Boolean terms in CafeOBJ, then "A implies B" is equivalent to "A and B = A."

A lemma typically has a form $A \rightarrow B$. When using this to prove a *goal*, we may write a proof score in CafeOBJ as follows:

reduce (A implies B) implies goal .

However, this style is somewhat inconvenient. Remember that CITP method tries to prove a fixed set of goals in many cases. If several lemmas are effective to different cases, we should use a complicated goal set such as:

```
:goal {
  eq (A1 implies B1) and (A2 implies B2) ... implies goal1 = true .
  eq (A1 implies B1) and (A2 implies B2) ... implies goal2 = true .
  ...
}
```

This style is not only complicated but also very expensive to execute. CafeOBJ internally represents a logical formula in the algebraic normal form (ANF), in which a formula represented as ANDed terms are XORed. For example, formula (A implies B) implies goal is represented as A xor B xor goal xor (A and B) xor (A and goal) xor (A and B and goal). The ANF of a goal would become exponentially long along with the number of lemmas.

Using the Implication Lemma, we can define lemmas in an independent style from goals as follows:

```
eq (A1 and B1) = A1 .
eq (A2 and B2) = A2 .
...
:goal {
    eq goal1 = true .
    eq goal2 = true .
...
}
```

Lemma 2 (Set Predicate Lemma) Let S be a set of object, P a predicate of an object, allObjP a predicate of a set of objects where allObjP(S) holds iff P(O) holds for every object O in S. Then, if allObjP(S) does not hold, then there exists an object O' and a set S' of objects such that S=(0' S') holds and P(0') does not hold³.

Corollary 1 Let S be a set of object, P a predicate of an object, someObjP a predicate of a set of objects where someObjP(S) holds iff P(O) holds for some object O in S. Then, if someObjP(S) holds, then there exists an object O' and a set S' of objects such that S=(0' S') holds and P(O') holds.

Since a cloud system structure is modeled as a collection of several classes of objects, proof is often split into two cases where all the elements in a certain set of objects do or do not satisfy a certain condition. For example, since the condition of rule R01 is allPROfRSInStates(SetPR, IDRS,ready), proof is split into two cases; all the properties of resource IDRS are or are not ready.

Template module OBJECTBASE predefines a general predicate allObjP that uses an object predicate P and checks if P(O) holds for every object O in a given set of objects. Similarly it predefines a general predicate someObjP. Here, it is important to note that many predicates provided by the template modules are ones instantiated from allObjP or someObjP.

³Many proved lemmas including the Set Predicate Lemma are proved using the mathematical induction about constructors. Therefor, the user should not additionally define constructors of predefined sorts.

For example, allZOfXInStates is instantiated from allObjP where P(0) holds iff 0 is in one of given local states whenever it links to a given linked object. As explained in Section 5.2, allPROfRSInStates is renamed from allZOfXInStates and thus the Set Predicate Lemma can be used to split cases where the condition of rule R01 does or does not hold as follows:

```
:csp {
  eq allPROfRSInStates(setPR,idRS,ready) = true .
  eq setPR = (PR' setPR') .
}
```

Note that in this case, PR' should be a property whose parent is resource idRS but is not ready (i.e. is notready). Thus, it can be represented as prop(tpr,idPR,notready,idRS,idRRS) where tpr, idPR, and idRRS are arbitrary constants. Then, the following case splitting collectively covers all of the cases:

```
:csp {
    eq allPROfRSInState(setPR,idRS,ready) = true .
    eq setPR = (prop(tpr,idPR,notready,idRS,idRRS) setPR') .
}
```

For another example, since existRS is instantiated from someObjP, a typical case splitting code is as follows:

```
:csp {
    eq existRS(setRS,idRS) = false .
    eq setRS = (res(trs,idRS,srs) setRS') .
}
```

5.3.2 Lemmas for Link Predicates

The framework provides many proved lemmas for predefined predicates provided by OBJLINKMANY2ONE and OBJLINKONE2ONE. This section describes two of them with example usages.

Lemma 3 (Many-2-One Lemma 07) Let S_X be a set of linking objects, S_Z a set of linked objects, St_X a set of local states of linking objects, St_Z a set of local states of linked objects, and let SX be a local state of linking object where SX is not included in St_X. Then, allObjInStates(S_X,St) implies ifXInStatesThenZInStates(S_X,St_X,S_Z,St_Z).

This lemma is represented in CafeOBJ as follows⁴:

⁴prec: 64 means the operator precedence of when is 64 (very low) and r-assoc means it is right associative.

In the course of verification of the transition rule set in Section 4.2, we need an invariant which says that every started parent resource has ready properties only. It is represented as follows:

```
var SetRS : SetOfResource
var SetPR : SetOfProperty
pred inv-ifRSStartedThenPRReady : State
eq inv-ifRSStartedThenPRReady(< SetRS,SetPR >)
  = ifRSInStatesThenPRInStates(SetRS,started,SetPR,ready) .
```

In order to show the invariant property of inv-ifRSStartedThenPRReady, we need a lemma which says that if all of the resources are initial then inv-ifRSStartedThenPRReady holds. The lemma could be defined as follows:

```
var SetRS : SetOfResource
var SetPR : SetOfProperty
pred lemma1 : SetOfResource SetOfProperty
eq lemma1(SetRS,SetPR) =
   allRSInStates(SetRS,initial) implies
   ifRSInStatesThenPRInStates(SetRS,started,SetPR,ready) .
```

Although this lemma may be intuitively true, a typical pitfall of developing proof scores is regarding some lemma as intuitive and skipping to prove it, which often results in leaving critical errors in specifications. However, recalling that we get allRSInStates by renaming allObjInStates and similarly ifRSInStatesThenPRInStates by renaming ifXInStatesThenZInStates, this lemma can be obtained by renaming m2o-lemma07 as fol-

lows:

```
var SetRS : SetOfResource
var SetPR : SetOfProperty
pred m2o-lemma07-renamed : SetOfResource SetOfProperty
eq m2o-lemma07-renamed(SetRS,SetPR)
        = allRSInStates(SetRS,initial) implies
        ifRSInStatesThenPRInStates(SetRS,started,SetPR,ready)
        when not (initial \in started) .
```

Since not (initial \in started) is true, the when clause can be omitted. This is why we use when instead of implies assuming it will be omitted when renamed. Using the Implication Lemma, this lemma can be define as follows:

```
var SetRS : SetOfResource
var SetPR : SetOfProperty
eq [m2o-lemma07]:
   (allRSInStates(SetRS,initial) and
   ifRSInStatesThenPRInStates(SetRS,started,SetPR,ready))
 = allRSInStates(SetRS,initial) .
```

Lemma 4 (Many-2-One Lemma 11) Let S_X be a set of linking objects, S_Z a set of linked objects, St_X a set of local states of linking objects, St_Z a set of local states of linked objects, and Z and Z' linked objects where Z and Z' are identical (i.e. whose identifiers, links, and types are the same) and only their local states are different⁵. Then, if the local state of Z' is included in St_Z, ifXInStatesThenZInStates(S_X,St_X,(Z S_Z),St_Z) implies ifXInStatesThenZInStates(S_X,St_X,(Z' S_Z),St_Z).

This lemma is represented in CafeOBJ as follows:

```
vars 01 02 : Object
pred changeObjState : Object Object
eq changeObjState(01,02)
   = (id(01) = id(02)) and
     (link(01) = link(02)) and
     (type(01) = type(02)).
vars Z Z' : Object
var S_X : SetOfLObject
var S_Z : SetOfObject
var St_X : SetOfLObjState
var St_Z : SetOfObjState
pred m2o-lemma11 : Object Object SetOfLObject SetOfLObjState
                                 SetOfObject SetOfObjState
eq m2o-lemma11(Z,Z',S_X,St_X,S_Z,St_Z)
   = ifXInStatesThenZInStates(S_X,St_X,(Z S_Z),St_Z) implies
     ifXInStatesThenZInStates(S_X,St_X,(Z' S_Z),St_Z)
   when (state(Z') \setminus St_Z) and changeObjState(Z,Z').
```

In order to show the invariant property of inv-ifRSStartedThenPRReady above, we also need another lemma which says that inv-ifRSStartedThenPRReady keeps to hold when rule R02 is applied and makes a property transit from notready to ready. The lemma could be defined as follows:

```
vars IDRS IDRRS : RSID
var IDPR : PRID
var TPR : PRType
var SetRS : SetOfResource
var SetPR : SetOfProperty
pred lemma2 : SetOfResource PRType PRID RSID RSID SetOfProperty
eq lemma2(SetRS,TPR,IDPR,IDRS,IDRRS,SetPR)
 = ifRSInStatesThenPRInStates
   (SetRS,started,(prop(TPR,IDPR,notready,IDRS,IDRRS) SetPR),ready)
implies
   ifRSInStatesThenPRInStates
   (SetRS,started,(prop(TPR,IDPR, ready,IDRS,IDRRS) SetPR),ready) .
```

Again this lemma may be intuitively true because its antecedent part requires that some properties should be ready and one specific property with identifier IDPR changes its local state from notready to ready. And again this lemma can also be obtained by renaming m2o-lemma11 as follows:

⁵Exactly speaking, Z and Z' are terms of CafeOBJ representing when the same object in the model is in the different local states.

```
vars IDRS IDRRS : RSID
var IDPR : PRID
var TPR : PRType
var SetRS : SetOfResource
var SetPR : SetOfProperty
pred m2o-lemma11-renamed : SetOfResource PRType PRID
                            RSID RSID SetOfProperty
eq m2o-lemma11-renamed(SetRS,TPR,IDPR,IDRS,IDRRS,SetPR) =
  = ifRSInStatesThenPRInStates
    (SetRS, started, (prop(TPR, IDPR, notready, IDRS, IDRRS) SetPR), ready)
  implies
    ifRSInStatesThenPRInStates
    (SetRS, started, (prop(TPR, IDPR,
                                      ready,IDRS,IDRRS) SetPR),ready)
   when (state(prop(TPR, IDPR, ready, IDRS, IDRRS)) \in ready) and
        changeObjState(prop(TPR, IDPR, notready, IDRS, IDRRS),
                                          ready,IDRS,IDRRS)) .
                        prop(TPR, IDPR,
```

The when clause reduces to true and can be omitted. Using the Implication Lemma, this lemma can be define as follows:

```
vars IDRS IDRRS : RSID
var IDPR : PRID
var TPR : PRType
var SetRS : SetOfResource
var SetPR : SetOfProperty
eq [m2o-lemma11]:
   (ifRSInStatesThenPRInStates
    (SetRS,started,(prop(TPR,IDPR,notready,IDRS,IDRRS) SetPR),ready)
   and
    ifRSInStatesThenPRInStates
    (SetRS,started,(prop(TPR,IDPR, ready,IDRS,IDRRS) SetPR),ready))
   =
    ifRSInStatesThenPRInStates
    (SetRS,started,(prop(TPR,IDPR, ready,IDRS,IDRRS) SetPR),ready)).
```

5.3.3 Cyclic Dependency Lemma

A rule typically produces dependency of objects. For example, rule R01 in Section 4.2 makes myEIP transit from initial to started when its property myEIP::InsID is ready, which means myEIP depends on myEIP::InsID. Similarly, rule R02 makes property myEIP::InsID depend on its referring resource myInstance.

If such dependency is cyclic it should be troublesome because there may be a situation where each of objects in the cycle is waiting for its dependent object and no rule is applicable to any of them. Such situation is called a deadlock. For example, if myInstance had a property referring myEIP, then these two resources would be mutually dependent and no transition rule could be applied.

In order to start transitions and reach a desired final state, a cloud system should not include such cyclic dependency. Verification of the system requires (1) to formalize that the dependency is acyclic, (2) to prove the invariant property of the acyclicness, and (3) to prove that when acyclic there exists at least one applicable transition rule and the state machine continues to transit. The framework provides a template module to formalize acyclicness of dependency for (1) and a lemma that guarantees existence of applicable rules for (3). It also provides several common techniques and proved lemmas for (2).

Formalization of Dependency and Acyclicness

This section will describe a formal definition of cyclic dependency and show examples using the CloudFormation example case shown in Fig. 2.1 and transition rules R01 and R02 in Section 4.2.

Notation 2 $[X \in C]$ Let *C* be a class of objects in a cloud system, and let *X* be an object the system consisting of, then we denote $X \in C$ when *X* is of *C*.

Notation 3 [st(X, S)] Let S be a global state of a cloud system, and let X be an object in S, then st(X, S) is the local state of X in the context of S.

Definition 9 [can make an object transit] Let R = [l, r, c] be a transition rule, C a class of objects, S a global state, and X an object of C. We say \underline{R} can make X transit in S iff there exists a ground substitution σ such that $S = l\sigma$, $c\sigma$ reduces to true, and $st(X, l\sigma) \neq st(X, r\sigma)$. We also say \underline{R} can make X transit from $st(X, l\sigma)$ to $st(X, r\sigma)$ in S. Let s and s' be local states of C, then we say \underline{R} can make an object of C transit form s to s' iff there exists a global state S such that R can make an object of C transit form s to s' in S.

Definition 10 [pre-transit local state set] Let *R* be a transition rule, and *C* a class of objects, then the pre-transit local state set of *R* for *C*, denoted prels(R, C), is the set of local states of *C* where $s \in prels(R, C)$ iff there exists some local state $\overline{s'}$ of *C* such that *R* can make an object of *C* transit from *s* to *s'*.

For example, if st(myInstance, S) is *initial* then R01 can make myInstance transit from *initial* to *started* in S and thus *prels*(R01, Resource) is { initial }. Note that a transition rule can make objects of more than one classes transit.

Notation 4 (S[X/s]) Let S be a global state, C a class of objects, X an object of C in S, and s a local state of C, then S[X/s] is the global state such that:

- S[X/s] consists of the identical objects (i.e. identifiers and types are the same) as S,
- each link of objects in S[X/s] is the same as S, and
- st(X, S[X/s]) = s and $\forall X' \neq X : st(X', S[X/s]) = st(X', S)$.

This notation can specify more than one objects such that $\underline{S[X_1/s_1, X_2/s_2, ...]}$. Let Σ be a set of pairs of an object and a local state, $\Sigma = \{ (X_1, s_1), (X_2, s_2), ... \}$, then we denote $\underline{S[\Sigma]}$ as $S[X_1/s_1, X_2/s_2, ...]$.

Let S_0 be the following global state:

```
< ( res(ec2Instance, myInstance, initial)
res(ec2Eip, myEIP, initial) ),
( prop(instanceId, myEIP::InsID, notready, myEIP, myInstance) ) >
```

Let us denote an object by its identifier and let Σ_0 be a set of pairs of an object and a local state such that $\Sigma_0 = \{ (myInstance, started), (myEIP::InsID, ready) \}$, then $S_0[\Sigma_0]$ is the following global state:

< (res(ec2Instance, myInstance, started) res(ec2Eip, myEIP, initial)), (prop(instanceId, myEIP::InsID, ready, myEIP, myInstance)) >

Definition 11 [depends on] Let *S* be a global state, *X* and *X'* objects in *S*, and *R* a transition rule where *R* cannot make *X* transit in *S*. We say *X* depends on *X'* in *S* w.r.t. *R*, denoted $dep_R(X, X', S)$, iff there exists a set Σ of pairs of an object and a local state such that $\overline{\Sigma}$ includes a pair whose first element is *X'*, *R* can make *X* transit in *S*[Σ], and Σ is minimal. Here we say "minimal" to mean that there exists no subset Σ' of Σ such that *R* can make *X* transit in *S*[Σ']. We also say *X* depends on *X'* in *S*, denoted dep(X, X', S), when there exists some transition rule *R* such that $dep_R(X, X', S)$.

For example, rule R01 can make myEIP transit from initial to started in $S_0[\Sigma_0]$, however, there is a subset of Σ_0 such that $\Sigma_{R01} = \{(myEIP:InsID,ready)\}$ where rule R01 can make myEIP transit also in $S_0[\Sigma_{R01}]$. Thereby, myEIP depends only on myEIP:InsID but not on myInstance in S_0 w.r.t. R01. Similarly, when $\Sigma_{R02} = \{(myInstance, started)\}$, rule R02 can make myEIP::InsID transit from notready to ready in $S_0[\Sigma_{R02}]$ and thus myEIP::InsID depends on myInstance in S_0 w.r.t. R02.

Definition 12 [depending set] Let X be an object, R a transition rule, and S a global state, then the depending set of X in S, denoted DS(X, S), is recursively defined as (1) if X depends on some other object X' in S then X' is included in DS(X, S), i.e. $\forall X' : (dep(X, X', S) \rightarrow X' \in DS(X, S))$, and (2) if $X' \in DS(X, S)$ and X' depends on some other object X'' in S then X'' is included in DS(X, S), i.e. $\forall X', X'' : (X' \in DS(X, S) \land dep(X', X'', S) \rightarrow X'' \in DS(X, S))$.

Definition 13 [no cyclic dependency] Let *C* be a class, *X* an object of *C*, and *S* a global state. We say *X* is in no cyclic dependency in *S*, denoted noCycle(X, S), iff *X* itself is not included in DS(X, S). We also say there is no cyclic dependency of *C* in *S*, denoted $noCycle_C(S)$, iff all of the objects of *C* in *S* are in no cyclic dependency in *S*.

For example, $DS(myEIP, S_0) = \{myEIP::InsID, myInstance\}$ because myEIP depends on myEIP::InsID in S_0 w.r.t. R01 and myEIP::InsID depends on myInstance in S_0 w.r.t. R02. Since the depending set of myEIP does not include myEIP itself, myEIP is in no cyclic dependency in S_0 , and there is no cyclic dependency of Resource in S_0 .

Lemma 5 (Cyclic Dependency Lemma) Let *S* be a global state, *R* a transition rule, and *C* a class of objects. If there is no cyclic dependency of *C* in *S* and there exists some object *X* of *C* in *S* whose local state is included in prels(R, C), then there exists some object O of C in S such that the local state of O is included in prels(R, C) and the depending set of O includes no object of *C* whose local state is included in prels(R, C), i.e.:

$$\begin{aligned} noCycle_{C}(S) \land \exists X \in C : (st(X,S) \in prels(R,C)) \rightarrow \\ \exists O \in C : (st(O,S) \in prels(R,C) \land \\ \forall O' \in C : (O' \in DS(O,S) \rightarrow st(O',S) \notin prels(R,C))) \end{aligned}$$

Proof: Let C^R be a set of objects of C in S whose local states are included in prels(R, C), i.e. $C^R = \{ O \mid O \in C \land st(O, S) \in prels(R, C) \}$. C^R is not empty because it includes X. If every object O in C^R has at least one object $O' \in C^R \cap DS(O, S)$ then there should be some object O in C^R such that $O \in DS(O, S)$ because DS is transitive and C^R is finite. However, it means there is cyclic dependency of C in S. \Box

For example, let S_0 be a global state shown above, then there is no cyclic dependency of Resource in S_0 and there exists myEIP whose local state is *initial*. Thereby, the Cyclic Dependency Lemma ensures that there exists a Resource object whose local state is *initial* and whose depending set includes no initial Resource objects, which is myInstance.

Focusing on One Class

When using the Cyclic Dependency Lemma, we can usually focus on one class of objects. In the CloudFormation example case, we can focus on Resource objects and not on Property objects; we should consider no cyclic dependency of only Resource objects and existence of a Resource object whose local state is in *prels*(R01,Resource), i.e. is initial. The following is a modified version of the formalization focusing on one class.

Definition 14 [depending set of the same class as] Let *C* be a class , *X* an object of *C*, *R* a transition rule, and *S* a global state, then the depending set of the same class as *X* in *S*, denoted $DS_C(X, S)$, is defined as $DS_C(X, S) = \{ X' \in \overline{C \mid X' \in DS(X, S)} \}$

Lemma 6 Let C be a class, X an object of C, and S a global state. If X itself is not included in $DS_C(X, S)$, then X is in no cyclic dependency of C in S.

Corollary 2 Let *S* be a global state, *R* a transition rule, and *C* a class of objects. If there is no cyclic dependency of *C* in *S* and there exists some object *X* of *C* in *S* whose local state is included in prels(*R*, *C*), then there exists some object *O* of *C* in *S* such that the local state of *O* is included in prels(*R*, *C*) and $DS_C(O, S)$ includes no object whose local state is included in prels(*R*, *C*); typically $DS_C(O, S)$ is empty.

Definition 15 [dependency chain] Let $X_1, X_2, ..., X_n$ be objects, and S a global state, then the dependency chain in S, denoted $\underline{dc([X_1, X_2, ..., X_n], S)}$, is defined as $\forall i \in [1, n - 1]$: $\underline{dep(X_i, X_{i+1}, S)}$.

For example, since myEIP depends on myEIP::InsID and it in turn depends on myInstance in S_0 , there is a dependency chain in S_0 , $dc([myEIP,myEIP::InsID,myInstance], S_0)$.

Definition 16 [directly depending set of the same class as] Let *C* be a class of objects, *X* an object of *C*, and *S* a global state. The directly depending set of the same class as *X* in *S*, denoted $DDS_C(X, S)$, is defined as $\{X' \mid \exists dc(\overline{[X, X_1, \dots, X_n, X']}, S) \land X' \in C \land \forall i \in [1, n] : X_i \notin C \}$. We also say *X* directly depends on *X'* in *S* when $X' \in DDS_c(X, S)$.

When X and X' are objects of C, $X' \in DDS_C(X)$ means that there exists a dependency chain in which the first object is X, the last object is X', and every object between X and X' is not of C. For example, $DDS_C(myEIP, S_0) = \{ myInstance \}$ since there is a dependency chain $dc([myEIP,myEIP::InsID,myInstance], S_0).$ **Corollary 3** Let *S* be a global state, *R* a transition rule, and *C* a class of objects. If there is no cyclic dependency of *C* in *S* and there exists some object *X* of *C* in *S* whose local state is included in prels(*R*,*C*), then there exists some object *O* of *C* in *S* such that the local state of *O* is included in prels(*R*,*C*) and $DDS_C(O, S)$ includes no object whose local state is included in prels(*R*,*C*); typically $DDS_C(O, S)$ is empty.

Using a Template Module to Represent *noCycle*_C

Using the formalization of cyclic dependency explained above, the framework provides a predicate, noCycleC(S), which checks there is no cyclic dependency in the given global state S. Predicate noCycleC is defined by a template module, CYCLEPRED and a parameter module, PRMCYCLE:

```
module* PRMCYCLE {
  [Object < SetOfObject]</pre>
  op empObj : -> SetOfObject
  op _ _ : SetOfObject SetOfObject -> SetOfObject
  op _\in_ : Object SetOfObject -> Bool
  [State]
  op getAllObjInState : State -> SetOfObject
  op DDSC : Object State -> SetOfObject
}
module! CYCLEPRED(P :: PRMCYCLE) {
  var 0 : Object
  vars V OS : SetOfObject
  var S : State
  pred noCycleC : State
  pred noCycleC : Object State
  pred noCycleC : SetOfObject SetOfObject State
  eq noCycleC(S)
     = noCycleC(getAllObjInState(S),empObj,S) .
  eq noCycleC(0,S)
     = noCycleC(0,empObj,S) .
  eq noCycleC(empObj,V,S)
     = true .
  eq noCycleC((0 0S),V,S)
     = if 0 \in V then false else noCycleC(DDSC(0,S),(0 V),S) fi
       and noCycleC(OS,V,S) .
}
```

Parameter module PRMCYCLE requires five operator parameters three of which can be defined just by using template module OBJECTBASE. The user of the framework should appropriately define getAllObjInState and DDSC because they are specific to each problem. Given a global state S, operator getAllObjInState(S) should return the set of all the objects of the specific class we focus; that is the resource class in the CloudFormation example case. Operator DDSC(0,S) should return the directly depending set of the same class as the given object 0 in the given global state S.

Using these operators, template module CYCLEPRED defines predicate noCycleC. Given a global state S, predicate noCycleC(S) transitively visits objects in directly depending sets DDSC(0,S) and checks not to find any objects already visited.

In the CloudFormation example case, getAllObjInState and DDSC can be defined as follows:

Remember that rule R01 can make an initial resource transit when all of its properties are ready and that rule R02 can make a notready property when its parent is started. As explained in Section 5.2, getPRsOfRSInStates(SetPR,RS,notready) returns a set of properties which are included in the set SetPR of properties, whose parents are the resource RS, and whose local states are notready. And getRRSsOfPRsInStates(SetRS, *setPR*, initial) returns a set of resources which are included in the set SetRS of resources, which are referred by one of the properties in the set *setPR*, and whose local states are initial. Thereby, $DDS_C(X, S)$ can be defined by combining these operators.

Using getAllRSInState and DDSC as parameters template module CYCLEPRED can be instantiated as follows:

```
extending(CYCLEPRED(
    STATECyclefuns {sort Object -> Resource,
        sort SetOfObject -> SetOfResource,
        op empObj -> empRS,
        op getAllObjInState -> getAllRSInState})
 * {op noCycleC -> noRSCycle}
)
```

Resource, SetOfResource, empRS, and getAllRSInState are specified as actual parameters where DDSC is not specified because the name is the same as the formal parameter. noCycleC is renamed as noRSCycle.

Lemmas for Proving the Invariant Property of Acyclicness

In order to use the Cyclic Dependency Lemma, the user of the framework should prove the invariant property of $noCycle_C$, especially should prove that $noCycle_C(S) \rightarrow noCycle_C(S')$ for any global state S and any possible next state S' of S. Although such proof is specific to each problem, there are several common techniques and the framework provides several proved lemmas for them.

It is often the case where a transition rule decreases dependencies between objects when it is applied. For example, when rule R01 is applied to a global state, it makes a resource object transit from initial to started. If the resource object is referred by some notready property object, then the property depends on the resource in the global state w.r.t. R02 and does not depend on it in the next state. Similarly, when rule R02 is applied, it makes a property object transit from notready to ready and the dependency between the property and its parent resource disappears. Thereby, when these rules are applied, the depending sets will become smaller than in the previous global states.

Lemma 7 (Depending Subset Lemma) Let *S* and *S'* be global states and *X* an object in both of them. If $DS(X, S') \subseteq DS(X, S)$, then $noCycle(X, S) \rightarrow noCycle(X, S')$.

Proof: noCycle(X, S) means that $X \notin DS(X, S)$, which implies that $X \notin DS(X, S')$ because $DS(X, S') \subseteq DS(X, S)$. \Box

Corollary 4 Let C be a class of objects and let S and S' be global states. If $DS_C(X, S') \subseteq DS_C(X, S)$ for all objects X of C in S, then $noCycle_C(S) \rightarrow noCycle_C(S')$.

Corollary 5 Let C be a class of objects and let S and S' be global states. If $DDS_C(X, S') \subseteq DDS_C(X, S)$ for all objects X of C in S, then $noCycle_C(S) \rightarrow noCycle_C(S')$.

Lemma 8 (Many-2-One Lemma 24) Let S_X be a set of linking objects, S_Z a set of linked objects, S_X a set of local states of linking objects, and let X and X' be linking objects where X and X' are identical and only their local states are different Then, if the local state of X' is not included in S_X , $getXsOfZsInStates((X' S_X), S_Z, S_X)$ is a subset of or equal to $getXsOfZsInStates((X S_X), S_Z, S_X)$).

This Many-2-One Lemma 24 is represented in CafeOBJ as follows:

In the CloudFormation example case, in order to show the invariant property of noRSCycle, the corollary of the Depending Subset Lemma ensures that we should only prove that DDSC becomes a subset of itself when rule R01 or R02 is applied. It then requires another lemma which says that getRRSsOfPRsInStates becomes a subset of itself when rule R01 is applied and makes a resource transit from initial to started. The lemma could be defined as follows:

As explained in Section 5.2, getRRSsOfPRsInStates is renamed from getXsOfZsInStates and thus this lemma can be obtained by renaming m2o-lemma24 as follows:

```
vars RS RS' : Resource
var SetRS : SetOfResource
var SetSRS : SetOfRSState
var SetPR : SetOfProperty
ceq [m2o-lemma24]:
   subset(getRRSsOfPRsInStates((RS' SetRS),SetPR,SetSRS),
        getRRSsOfPRsInStates((RS SetRS),SetPR,SetSRS))
   = true
   if id(RS) = id(RS') and not state(RS') \in SetSRS .
```

In the other cases, systems are intentionally designed to have some constraints to avoid cyclic dependencies. For example, if a system is constrained to have no cyclic chains of links of objects, then there should be no cyclic dependency in the system no matter how the local states of the objects transit. Since the purpose of such constraints is to simplify complicated controls of dependencies of objects, it is typically easier to check the constraints than to use $noCycle_C$ defined above.

Notation 5 [rel(X, X', S)] Let *S* be a global state, and let *X* and *X'* be objects in *S*. When there is some relationship *r* between *X* and *X'*, we denote it as $\underline{r(X, X', S)}$. Note that "*X* depends on *X'* in *S*" is one of such relationships.

Definition 17 [directly relating set] Let *S* be a global state, *X* an object in *S*, and *r* a relationship of objects. Then, the directly relating set of *X* in *S* w.r.t. *r*, denoted $DRS_r(X, S)$, is defined as $DRS_r(X, S) = \{ X' \mid r(\overline{X, X', S}) \}$.

Definition 18 [relating set] Let *X* be an object, *S* a global state, and *r* a relationship of objects, then the relating set of *X* in *S* w.r.t. *r*, denoted $RS_r(X,S)$, is recursively defined as (1) $\forall X'$: $(r(X, X', \overline{S}) \rightarrow X' \in RS_r(X, S))$, and (2) $\forall X', \overline{X''} : (X' \in RS_r(X, S) \land r(X', X'', S) \rightarrow X'' \in RS_r(X,S))$.

Definition 19 [no cyclic relationship] Let X be an object, S a global state, and r a relationship of objects, then we say X is in no cyclic relationship in S w.r.t. r, denoted $\underline{noCycle_r(X, S)}$, iff X itself is not included in $\overline{RS_r(X, S)}$.

Lemma 9 Let C is a class, X an object of C, S a global state, and r a relationship of objects. If $DDS_c(X, S)$ is a subset of $DRS_R(X, S)$ for all X in S, then $noCycle_r(X, S)$ implies $noCycle_c(X, S)$ for all X, i.e.:

 $\forall X : DDS_c(X, S) \subseteq DRS_r(X, S) \rightarrow \forall X : (noCycle_r(X, S) \rightarrow noCycle_c(X, S))$

Proof: $DDS_c(X, S) \subseteq DRS_r(X, S)$ means that $DS_c(X, S) \subseteq RS_r(X, S)$. Thereby, if $noCycle_c(X, S)$ does not holds, then $X \in DS_c(X, S)$ and $X \in RS_r(X, S)$, which is a contradiction. \Box

This lemma allows the user of the framework to define DDSC implementing some simpler relationship r instead of the true DDS_c and use noCycleC defined by using the DDSC instead of the true $noCycle_c$. For example, when we adopt the constraint of no cyclic chains of links in the CloudFormation example case, DDSC can be simply defined as follows:

```
var RS : Resource
var SetRS : SetOfResource
var SetPR : SetOfProperty
eq DDSC(RS,< SetRS,SetPR >)
  = getRRSsOfPRs(SetRS,getPRsOfRS(SetPR,RS)) .
```

However noCycleC defined by using the simpler DDSC above is not the true $noCycle_C$, we can use the Cyclic Dependency Lemma if we can prove the invariant property of noCycleC.

Chapter 6

Verification Procedure of Leads-to Properties

The framework provides an overall verification procedure for a kind of liveness properties, *leads-to* properties adopted from UNITY logic [5], as well as invariant properties. The procedure assists users of the framework to systematically think and develop proof scores for verification of cloud orchestration.

A typical property of an automated system setup operation, which we want to verify, is that the operation surely brings a cloud system to a global state where all of its resources are started. We say "surely" to mean that the system always reaches some final state from any initial states. This kind of reachability is one of the most important properties of practical automation of cloud systems.

Futatsugi [10] defines leads-to property based on transition sequences of state machines and proposes a set of sufficient conditions for it as follows:

Definition 20 [*p* leads-to *q*] Let TS = (St, Tr, In) be a state machine, *p* and *q* predicates of $St, St^R \subseteq St$ the set of reachable states of TS, and Θ the set of transition sequences of TS, then *p* leads-to *q* defined as follows:

$$\forall S \alpha \in \Theta : (S \in St^R \land p(S) \land \forall S' \in S \alpha : \neg q(S') \rightarrow \exists T \in St, \exists \beta \in \Theta : (q(T) \land S \alpha \beta T \in \Theta))$$

Lemma 10 Let p_0 , p, and q be predicates of St: $(p_0 \rightarrow p) \land (p \text{ leads-to } q) \rightarrow p_0 \text{ leads-to } q$.

Lemma 11 (sufficient conditions for leads-to) Let TS = (St, Tr, In) be a state machine, p and q predicates of St, inv an invariant of TS, and m a natural number function of St, then the following three conditions¹ are sufficient for (p leads-to q) to hold².

¹However Futatsugi [10] proposes four conditions, we have discussed and concluded that they can be rearranged into three conditions.

²Definition 20 of (p leads-to q) includes the case where there is an infinite transition sequence $\alpha_{\infty} = (S_0, S_1, ...)$ such that predicate q never holds in α_{∞} , $\forall S_i \in \alpha_{\infty} : \neg q(S_i)$, but any prefix of α_{∞} reaches a state where q holds, $\forall \alpha_i = (S_0, ..., S_i)$, $\exists T \in St$, $\exists \beta \in \Theta : (q(T) \land S \alpha_i \beta T \in \Theta)$). However, leads-to may be defined in a narrower sense where no such infinite transition sequence is allowed. Here, we call the former as *weak-leads-to* and the latter as *strong-leads-to*. The set of conditions proposed by Lemma 11 is sufficient to both meanings of leads-to because the properly decreasing natural number function, m, ensures that transition sequences never become infinite while keeping q not to hold. In the rest of this dissertation, we mean (p leads-to q) as (p strong-leads-to q).

$$\begin{array}{ll} \forall (S,S') \in Tr: & ((inv(S) \land p(S) \land \neg q(S)) \to (p(S') \lor q(S'))) \\ \forall (S,S') \in Tr: & ((inv(S) \land p(S) \land \neg q(S)) \to (m(S) > m(S'))) \\ \forall S \in St: & ((inv(S) \land p(S) \land \neg q(S)) \to \exists S' \in St: (S,S') \in Tr) \end{array}$$

Let the automation of a setup operation be modeled as a state machine TS = (St, Tr, In)specified by sort State and a set of transition rules, and let $Fn \subseteq St$ be a set of expected final states, reachability we want to verify is formalized as (*init* leads-to *final*) where *init* and *final* are predicates for a given global state S such that *init*(S) holds iff $S \in In$ and *final*(S) holds iff $S \in Fn$.

The lemma 10 ensures that what we should do is to find a state predicate p such that (*init* \rightarrow p) and p satisfies the sufficient conditions for (p leads-to *final*). However such p is specific to the individual problem, one of the most typical and general ones is that p(S) means that "S has a next state," i.e. "S will transit." When a state machine has such general p, it always continues to transit until it reaches a final state.

Definition 21 [continuous predicate] The continuous predicate, *cont*, is the predicate which holds iff there exists some next state of a given state. Let TS = (St, Tr, In) be a state machine, then $\forall S \in St : cont(S) \text{ iff } \exists S' \in St : (S, S') \in Tr$.

Lemma 12 (sufficient conditions for *init* leads-to *final)* Let TS = (St, Tr, In) be a state machine, inv a conjunction of some state predicates and m a natural number function of St, then the following five conditions are sufficient for (init leads-to final) to hold.

$$\forall S \in St: \quad (init(S) \to cont(S)) \tag{1}$$

$$\forall (S, S') \in Tr: \quad ((inv(S) \land \neg final(S)) \to (cont(S') \lor final(S')))$$
(2)

$$\forall (S, S') \in Tr: \quad ((inv(S) \land \neg final(S)) \to (m(S) > m(S')))$$
(3)

$$\forall S \in St: \quad (init(S) \to inv(S)) \tag{4}$$

$$\forall (S, S') \in Tr: \quad (inv(S) \to inv(S')) \tag{5}$$

Proof: Let *p* in the "sufficient conditions for leads-to" lemma be *cont*, then $\forall (S, S') \in Tr$: p(S) = true holds and $\forall S \in St : (p(s) \rightarrow \exists S' \in St : (S, S') \in Tr)$. \Box

Condition (1) means an initial state should be a continuing state, i.e. it should start transitions. Condition (2) means transitions continue until final(S') holds. Condition (3) implies that m(S) keeps to decrease properly while final(S) does not hold. Since m(S) is a natural number, it should stop to decrease in finite steps and the state machine should get to state S' where cont(S') does not hold and final(S') does hold, because condition (2) ensures that transitions would still continue if cont(S') does hold. Here, m is called a *state measuring function*. When condition (4) and (5) hold, each state predicate included in *inv* is called an invariant.

The rest of this chapter explains the verification procedure for five sufficient conditions above using the CloudFormation example case and the case of TOSCA topologies will be explained in Chapter 7.

6.1 **Procedure: Definition of Predicates**

```
Step 0-1: Define init and final.
```

In the CloudFormation example case, predicates init(S) and final(S) can be represented by CafeOBJ as follows:

```
var SetRS : SetOfResource
var SetPR : SetOfProperty
var S : State
pred init : State
eq init(< SetRS.SetPR >)
   = wfs(< SetRS,SetPR >) and
     noRSCycle(< SetRS,SetPR >) and
     allRSInStates(SetRS, initial) and
     allPRInStates(SetPR,notready) .
pred final : State
eq final(< SetRS,SetPR >)
   = allRSInStates(SetRS, started) .
pred wfs : State
eq wfs(S)
   = wfs-atLeastOneRS(S) and
     wfs-uniqRS(S)
                    and wfs-uniqPR(S) and
     wfs-allPRHaveRS(S) and wfs-allPRHaveRRS(S).
pred wfs-atLeastOneRS : State
eq wfs-atLeastOneRS(< SetRS,SetPR >) = not (SetRS = empRS) .
pred wfs-uniqRS : State
eq wfs-uniqRS(< SetRS,SetPR >) = uniqRS(SetRS) .
pred wfs-uniqPR : State
eq wfs-uniqPR(< SetRS,SetPR >) = uniqPR(SetPR) .
pred wfs-allPRHaveRS : State
eq wfs-allPRHaveRS(< SetRS,SetPR >) = allPRHaveRS(SetPR,SetRS) .
pred wfs-allPRHaveRRS : State
eq wfs-allPRHaveRRS(< SetRS,SetPR >) = allPRHaveRRS(SetPR,SetRS) .
```

Among conditions explicitly composing init(S), one referring to no local states of objects and being expected to be an invariant is called a *wfs (well-formed state)* and we usually gather them and define predicate wfs as a conjunction of them. The reason why we need several wfs predicates is because representing a global state as a tuple of sets of objects is too general to represent structural constraints, such as identifiers should be unique, there is no dangling link, and so on. Each structural constraint is typically represented as a wfs and should be an invariant. In addition, do not forget to include $noCycle_C$ in the *init* predicate when using the Cyclic Dependency Lemma.

Step 0-2: Define cont.

Since cont(S) means that state S has at least one next state, it can be specified as follows using the unconditional search predicate of CafeOBJ :

vars S SS : State
eq cont(S) = (S =(*,1)=>+ SS) .

Step 0-3: Define *m*.

We should find a natural number function that properly decreases in transitions. If we can model a cloud system as a state machine where every transition rule changes at least one local state of an object and there is no loop transition, then the measuring function, *m*, can be easily defined as the weighted sum of counting local states of all the classes of objects. Suppose that local states of class *C* are st_C^0 , st_C^1 , ..., $st_C^{n_c}$ and they are straightforward, that is, there is no backward transition, then *m* can be $\sum_C \sum_{0 \le k \le n_C} #st_C^k \times (n_c - k)$ where $#st_C^k$ is the number of objects of class *C* whose local state is st_C^k . For the CloudFormation example case, *m* can be defined as follows:

```
var SetRS : SetOfResource
var SetPR : SetOfProperty
op m : State -> Nat
eq m(< SetRS,SetPR >)
= (#ResourceInStates(initial,SetRS) * 1)
+ (#ResourceInStates(started,SetRS) * 0)
+ (#PropertyInStates(notready,SetPR) * 1)
+ (#PropertyInStates(ready,SetPR) * 0) .
```

When a rule makes an object of class *C* transit from state s_c^k to st_C^{k+1} , $\#st_C^k$ decreases by 1 and $\#st_C^{k+1}$ increases by 1 so that $m(S') = m(S) - (n_c - k) + (n_c - k - 1) = m(S) - 1$ holds.

When the state machine has a rule without changing any local states of objects, m should include an additional term that decreases when the rule is applied. But, instead, we recommend introducing some local state representing whether the rule is already applied or not yet.

When there is a loop transition, *m* should include an additional term that properly decreases whenever a loop occurs. The simplest approach is to introduce an object whose local state is a loop counter.

Step 0-4: Define inv.

Invariants other than wfs predicates are usually recognized to be necessary in the course of proving conditions (1) to (5) above and are introduced by the user of the framework. For example, the CloudFormation example case requires an invariant inv-ifRSStartedThenPRReady as explained in Section 5.3.

Predicate *inv* is a conjunction of all the invariants, however, the straightforward representation is not so efficient. CafeOBJ needs to internally maintain long ANDed terms and to spend much processing time. Fortunately, there is more efficient representation. Since the sufficient conditions (2), (3), and (5) include *inv* in their antecedent parts, it is enough to know whether each invariant does or does not reduce to false. Thereby, we can define *inv* such that it reduces to false when one of invariants reduces to false as follows:

```
var S : State
pred inv : State
-- wfs-*:
```

```
ceq inv(S) = false if not wfs-atLeastOneRS(S) .
ceq inv(S) = false if not wfs-allPRHaveRS(S) .
ceq inv(S) = false if not wfs-allPRHaveRRS(S) .
-- inv-*:
ceq inv(S) = false if not inv-ifRSStartedThenPRReady(S) .
```

Note that only three of six wfs predicates are used to define *inv*, since they directly take some roles in proofs.

As to sufficient conditions (4) and (5), *inv* is also included in their consequent parts, which case will be explained in Section 6.5.

Step 0-5: Prepare for using the Cyclic Dependency Lemma.

When using the Cyclic Dependency Lemma, we firstly introduce an object which is in one of the pre-transit local state set of a transition rule and then we claim that DDS_C of the object includes no object in the pre-transit local state set.

CITP method used a :init command to introduce a lemma on the way of proofs. The lemma should be defined in the non-execute mode and be labeled in advance. The :init command is used to specify the labeled lemma and the appropriate substitution of variables.

In the CloudFormation example case, we will introduce an initial resource and claim that every resource in DDS_c of the resource is not initial. The following conditional equation is defined in advance and means that there is a contradiction when DDS_c of the specified resource includes any initial resource.

```
-- The Cyclic Dependency Lemma ensures
-- an initial resource whose DDSC includes no initial resourecs.
var T : RSType
var IDRS : RSID
var S : State
ceq [Cycle :nonexec]:
    true = false
    if someRSInStates(DDSC(res(T, IDRS, initial),S),initial) .
```

Cycle is the label of this lemma and :nonexec means that this lemma is executed only when it is introduced by a :init command and variables T, IDRS, and S are substituted. The usage of an :init command will be described in the next section.

Step 0-6: Prepare arbitrary constants.

Proof scores for the sufficient conditions require many arbitrary constants. We say such constants as *proof constants*. In order to make the proof score be easy to understand, proof constants are consistently named and declared. The following shows the definitions of proof constants for the CloudFormation example case:

```
ops idRS idRS' idRS1 : -> RSIDLt
ops idRRS idRRS' idRRS1 : -> RSIDLt
ops idPR idPR' idPR1 : -> PRIDLt
ops sRS sRS' sRS'' sRS'' : -> SetOfResource
ops sPR sPR' sPR'' sPR''' : -> SetOfProperty
ops trs trs' trs'' trs''' : -> RSType
ops tpr tpr' tpr'' tpr''' : -> PRType
ops srs srs' srs'' srs''' : -> RSState
```

```
ops spr spr' spr'' spr'' : -> PRState
op stRS : -> SetOfRSState
op stPR : -> SetOfPRState
```

6.2 **Procedure: Proof of Sufficient Condition (1)**

The verification procedure is basically a process to repeat three actions; (1) pick up an unproved case which is then called the *current case*, (2) split the current case into cases which collectively cover the current case, (3) try to reduce the split cases to true.

Step 1-0: Define a predicate to be proved. Predicate initcont to represent condition (1) can be defined as follows:

```
var S : State
pred initcont : State .
eq initcont(S) = init(S) implies cont(S) .
```

Step 1-1: Begin with the most general case.

In the most general case for proof of condition (1), the global state consists of proof constants every of which represents an arbitrary set of objects of each class. For the CloudFormation example case, the most general case is as follows where sRS and sPR are proof constants for a set of resources and properties respectively:

```
:goal {eq initcont(< sRS, sPR >) = true .}
```

This case is too general to judge whether the condition does or does not hold. Thereby, no reduction occurs.

Step 1-2: Consider which rule can be applied to the global state in the current case. The rule is referred to as the *current rule*.

One of the main benefits of interactive proof development is that thinking through meaning of the specification leads to deep understanding of it. If the developer of proofs cannot find the first applied rule, it means insufficient understanding of the specification. For the CloudFormation example case, the first rule is R01.

Step 1-3: Split the current case into cases which collectively cover the current case and one of which matches to LHS of the current rule.

Since LHS of rule R01 requires the global state to have at least one initial resource, the current case is split into three more cases, i.e. no resource, at least one initial or started resource. In the following proof score, trs, idRS, and sRS' are proof constants for a type of the resource, an identifier of the resource, and a set of resources respectively.

```
:csp {
    eq sRS = empRS .
    eq sRS = (res(trs,idRS,srs) sRS') .
}
-- Case 1: When there is no resource:
:apply (rd) -- 1
-- Case 2: When there is a resource:
-- The state of the resource is initial or started.
```

```
:csp {
    eq srs = initial .
    eq srs = started .
}
-- Case 2-1: When the resource is initial:
... -- More case splitting needed.
-- Case 2-2: When the resource idRS is started:
:apply (rd) -- 2-2
```

Note that res(trs,idRS,srs) represents an arbitrary resource. The goal of Case 1 is proved because wfs-atLeastOneRS(S) does not hold and thus init(S) does not hold. The goal of Case 2-2 is also proved because allRSInStates(SetRS,initial) does not hold. Only Case 2-1 remains unproved and it then becomes the current case.

Step 1-4: Split the current case into cases where the condition of the current rule does or does not hold.

Since the condition of rule R01 requires all the properties of the initial resource are ready, Case 2-1 is split into two more cases; all the properties are or are not ready. As explained in Section 5.3, the Set Predicate Lemma ensures that these cases are represented as follows where tpr, idPR, idRRS, and sPR' are proof constants for a type of the property, an identifier of the property, an identifier of a resource referred by the property, and a set of properties respectively:

```
-- Case 2-1: When the resource is initial:
-- The condition of R01 is allPROfRSInStates(sPR,idRS,ready) .
:csp {
    eq allPROfRSInStates(sPR,idRS,ready) = true .
    eq sPR = (prop(tpr,idPR,notready,idRS,idRRS) sPR') .
}
-- Case 2-1-1: When all properties of the resource are ready.
:apply (rd) -- 2-1-1
-- Case 2-1-2: When there is a not-ready property of the resource:
... -- More case splitting needed.
```

Note that prop(tpr,idPR,notready,idRS,idRRS) represents an arbitrary notready property whose parent is idRS. In Case 2-1-1, rule R01 can be applied, which means cont(S) holds. Only Case 2-1-2 remains unproved.

Step 1-5: When there is a dangling link, split the current case into cases where the linked object does or does not exist.

In Case 2-1-2, property idPR has a link to a resource with identifier idRRS. Thereby, it is split into three more cases; a resource with identifier idRRS does not exist, does exist and it is initial or started. The nonexistence can be represented as predefined predicate existObj (renamed to existRS in this case) does not hold. Case 2-1-2 is split into the following three cases.

```
-- Case 2-1-2: When there is a not-ready property of the resource:
-- The resource referred by the property does or does not exist.
:csp {
  eq existRS(sRS',idRRS) = false .
  eq sRS' = (res(trs',idRRS,srs') sRS'') .
```

```
}
-- Case 2-1-2-1: When the referred resource does not exist:
:apply (rd) -- 2-1-2-1
-- Case 2-1-2-2: When the referred resource exists:
-- The state of the resource is initial or started.
:csp {
    eq srs' = initial .
    eq srs' = started .
}
-- Case 2-1-2-2-1: When the resource idRRS is initial:
... -- More consideration needed.
-- Case 2-1-2-2-2: When the resource idRRS is started:
:apply (rd) -- 2-1-2-2-2
```

The goal of Case 2-1-2-1 is proved because wfs-allPRHaveRRS(S) does not holds and the goal of Case 2-1-2-2-2 is proved because allRSInStates(SetRS,initial) does not holds. Only Case 2-1-2-2-1 remains unproved.

Step 1-6: When falling in a cyclic situation, use the Cyclic Dependency Lemma.

Since noRSCycle is included in the init condition and the resource idRS is initial, the Cyclic Dependency Lemma ensures there exists some initial resource RS such that no resource in DDSC(RS,S) is initial. Recalling that we chose idRS as an arbitrary initial resource in Step 1-3, we can assume that resource idRS itself is such RS and can claim that there is a contradiction when its DDS_C includes any initial resource using a :init command as follows:

```
-- Case 2-1-2-2-1: When the resource idRRS is initial:
-- The Cyclic Dependency Lemma rejects this case.
:init [Cycle] by {
   T:RSType <- trs;
   IDRS:RSID <- idRS;
   S:State <- < sRS, sPR >;
}
:apply (rd) -- 2-1-2-2-1
```

The :init command substitutes variable T and IDRS with the type and identifier of the resource and S with the global state. It has the same effect as adding the following equation into the current case:

Since DDS_C of the resource includes resource res(trs',idRRS,initial), there is a contradiction and the goal of this case is proved.

The following is the result of a "show proof" command, which shows that goals of all of the split cases are proved and thus condition (1) is proved.

root* [csp] 1* [csp] 2* [csp] 2-1*



Figure 6.1: Verification Procedure for Condition (1)

[csp] 2-1-1* [csp] 2-1-2* [csp] 2-1-2-1* [csp] 2-1-2-2* [csp] 2-1-2-2-1* [csp] 2-1-2-2-1* [csp] 2-1-2-2-2* [csp] 2-2*

Figure 6.1 summarizes the procedure.

6.3 **Procedure: Proof of Sufficient Condition (2)**

Step 2-0: Define a predicate to be proved.

pred contcont : State

Using the double negation idiom in Section 3.3, predicate contcont for condition (2) can be defined as follows:

```
vars S SS : State
var CC : Bool
pred ccont : State State
eq ccont(S,SS)
  = inv(S) and not final(S) implies cont(SS) or final(SS) .
```
```
eq contcont(S)
= not (S =(*,1)=>+ SS if CC suchThat
    not ((CC implies ccont(S,SS)) == true)
    { true }) .
```

Step 2-1: Begin with the cases each of which matches to LHS of each rule. Since condition (2) checks every possible next state of a given state *S*, we only need to prove the cases each of which matches to each rule. For the CloudFormation example case, we can begin with two cases for two rules as follows, which are too general:

The rest of this section describes the procedure for condition (2) using the case of rule R01 as an example. The case of rule R02 will be explained in Section 6.6.

Step 2-2: Split the current case for a rule into cases where the condition of the rule does or does not hold.

Since the condition of rule R01 requires all the properties of the initial resource are ready, the root case is split into two cases; all the properties are or are not ready.

```
-- The condition of R01 does or does not hold for the resource of idRS.
:ctf {
    eq allPROfRSInStates(sPR,idRS,ready) = true .
}
-- Case 1: When the condition of R01 holds:
... -- More case splitting needed
-- Case 2: When the condition of R01 does not hold:
:apply (rd) -- 2
```

Remember that in Step 1-4 explained above, we used a :csp command for case splitting based on the condition of rule R01 because we need more consideration for the negative case. In Step 2-2, we can simply use a :ctf command, since Case 2 has no next state and its goal can be proved. Thereby, only Case 1 remains unproved.

Step 2-3: Split the current case into cases where predicate *final* does or does not hold in the next state.

In Case 1, rule R01 makes an initial resource transit to started and the next state becomes a final state if all other resources included the set sRS of resources are already started. Otherwise there is at least one other initial resource. Using the Set Predicate Lemma, we can split the case as follows where trs', idRS', and sRS' are proof constants for a type of the resource, an identifier of the resource, and a set of resources respectively:

```
-- Case 1: When the condition of R01 holds for the resource of idRS:
-- All of the other resources are or are not started.
:csp {
  eq allRSInStates(sRS,started) = true .
  eq sRS = (res(trs',idRS',initial) sRS') .
}
-- Case 1-1: When all of the other resources are started:
:apply (rd) -- 1-1
-- Case 1-2: When there is an initial resource:
... -- More case splitting needed
```

The goal of Case 1-1 is proved because the next state is final. Case 1-2 remains unproved.

Step 2-4: Similarly as Step 1-2, consider which rule can be applied to the next state. The rule is referred to as the *current rule*.

Since the next state in Case 1-2 includes an initial resource with identifier idRS', rule R01 can be applied to it.

Step 2-5: Similarly as Step 1-3, split the current case into cases which collectively cover the current case and the next state of one of the split cases matches to LHS of the current rule. In this example, the next state of the current case already matches to LHS of rule R01.

Step 2-6: Similarly as Step 1-4, split the current case into cases where the condition of the current rule does or does not hold in the next state.

Again the Set Predicate Lemma can be used similarly as Step 1-4 as follows:

```
-- Case 1-2: When there is an initial resource:
:csp {
 eq allPROfRSInStates(sPR,idRS',ready) = true .
  eq sPR = (prop(tpr,idPR,notready,idRS',idRRS) sPR') .
}
-- Case 1-2-1: When all of properties of the resource idRS' are ready.
:apply (rd) -- 1-2-1
-- Case 1-2-2: When at least one of properties is not-ready.
-- Because sPR is redefined,
-- allPROfRSInStates(sPR,idRS,ready) should be claimed again.
:set(normalize-init,on)
:init ( ceq B1:Bool = true if not B2:Bool . ) by {
 B1:Bool <- allPROfRSInStates(sPR,idRS,ready) ;</pre>
 B2:Bool <- allPROfRSInStates(sPR,idRS,ready) == true ;</pre>
}
:set(normalize-init,off)
... -- More consideration needed.
```

The goal of Case 1-2-1 is proved. Case 1-2-2 remains unproved and this is somewhat troublesome for CafeOBJ system.

Remember that in Step 2-2 we already introduced an equation which claims that every property of the resource idRS in the set of properties sPR is ready. Here in Case 1-2-2, we need to define that sPR has a notready property idPR (consequently its parent should not be the resource idRS) and the rest of properties are included in the set sPR'. This breaks the confluence property of equations; when reducing the term allPROfRSInStates(sPR,idRS,ready), it reduces to true if CafeOBJ firstly uses the equation introduced in Step 2-2. But if CafeOBJ firstly uses the equation introduced here, it reduces to allPROfRSInStates(sPR',idRS,ready) and what we hope is the former. However we should not break the confluence property, it is a tradeoff between the ideal and the consistent case splitting manner. What is more important is to keep proof scores independent from the reduction strategy of CafeOBJ system. To do so, we have to write the proof score such as it does nothing when allPROfRSInStates(sPR,idRS,ready) reduces to true but otherwise it claims that the term reduces to true, which is the meaning of the :init command above.

The command :set(normalize-init,on) means that substituted variables should be reduced to normal forms when the equation is introduced by the :init command; its default option is off. When the variable B1 reduces to true, B2 also reduces to true and the equation to be introduced becomes "ceq true = true if not true ." which has no meaning because the condition part never holds. When B1 reduces to allPROfRSInStates(sPR',idRS,ready), B2 reduces to false and thus the equation to be introduced becomes as follows, which we want to claim:

```
ceq allPROfRSInStates(sPR',idRS,ready) = true if not false .
```

Step 2-7: Similarly as Step 1-5, when there is a dangling link, split the current case into cases where the linked object does or does not exist.

In Case 1-2-2, a property has a link to a resource with identifier idRRS. Thereby, it is split into three more cases; a resource with identifier idRRS does not exist, does exist and it is initial or started. The nonexistence can be represented as predefined predicate existRS does not hold. Case 1-2-2 is split into the following three cases:

```
-- Case 1-2-2: When at least one of properties is not-ready.
... -- Consideration above needed.
-- The resource referred by the property does or does not exist.
:csp {
  eq existRS(sRS',idRRS) = false .
 eq sRS' = (res(trs'',idRRS,srs'') sRS'') .
}
-- Case 1-2-2-1: When the referred resource does not exist:
:apply (rd) -- 1-2-2-1
-- Case 1-2-2-2: When the referred resource exists:
-- The state of the resource is initial or started.
:csp {
 eq srs'' = initial .
 eq srs'' = started .
}
-- Case 1-2-2-2-1: When the resource idRRS is initial:
... -- More consideration needed.
-- Case 1-2-2-2: When the resource idRRS is started:
:apply (rd) -- 1-2-2-2-2
```

The goal of Case 1-2-2-1 is proved because wfs-allPRHaveRRS(S) does not holds and then inv(S) does not hold as described in Section 6.1. The goal of Case 1-2-2-2 is also proved because the notready property idPR refers the started resource and so rule R02 is applicable in the next state. Only Case 1-2-2-2-1 remains unproved.

Step 2-8: Similarly as Step 1-6, when falling in a cyclic situation, use the Cyclic Dependency Lemma.

If the invariant property of noRSCycle is proved, we can use the Cyclic Dependency Lemma in any reachable state. In Case 1-2-2-2-1, there is an initial resource idRS' and so the lemma ensures there exists some initial resource RS such that no resource in DDSC(RS,S) is initial. Recalling that we chose idRS' as an arbitrary initial resource in Step 2-3, we can assume that itself is such RS and can claim that there is a contradiction when its DDS_C includes any initial resource using a :init command as follows:

```
-- The Cyclic Dependency Lemma rejects this case.
:init [Cycle] by {
   T:RSType <- trs';
   IDRS:RSID <- idRS';
   S:State <- < (res(trs,idRS,initial) sRS), sPR >;
}
:apply (rd) -- 1-2-2-2-1
```

The goal of this case is proved by the contradiction.

The following is the result of a "show proof" command, which shows that goals of all of the split cases are proved and thus condition (2) for rule R01 is proved:

root* [ctf] 1* [csp] 1-1* [csp] 1-2* [csp] 1-2-1* [csp] 1-2-2* [csp] 1-2-2-1* [csp] 1-2-2-2* [csp] 1-2-2-2* [csp] 1-2-2-2-1* [csp] 1-2-2-2-2* [csp] 1-2-2-2-2*

Figure 6.2 summarizes the procedure for each transition rule.

6.4 **Procedure: Proof of Sufficient Condition (3)**

Since the antecedent part of condition (3) is equivalent to (2), the proof procedure of (3) is almost the same as of (2).

Step 3-0: Use natural number axioms.

Since the standard sort Nat of CafeOBJ does not have enough information to deduce natural number expressions, the framework provides several axioms to be used for proof of condition (3). The following is one of those axioms to be used for the CloudFormation example:

var N : Nat eq (1 + N) > N = true.

Step 3-1: Define a predicate to be proved.

Using the double negation idiom in Section 3.3, predicate mesmes for condition (3) can be defined as follows:



Figure 6.2: Verification Procedure for Condition (2) for each rule

Step 3-2: Begin with the cases each of which matches to LHS of each rule. **Step 3-3:** Split the current case for a rule into cases where the condition of the rule does or does not hold.

For the CloudFormation example case, we can begin with two cases for two rules. Since rule R01 is conditional, the general case should be split into two cases according to Step 3-3. Then, the goals of totally three cases can be proved and thus condition (3) is proved as follows:

```
-- Goal of Condition (3) for rule R01
:goal {
  eq mesmes(< (res(trs,idRS,initial) sRS), sPR >) = true .
}
-- The condition of R01 does or does not hold for S.
:ctf {
  eq allPROfRSInStates(sPR,idRS,ready) = true .
}
-- Case 1: When the condition of R01 holds:
:apply (rd) -- 1
-- Case 1: When the condition of R01 does not hold:
:apply (rd) -- 2
-- Goal of Condition (3) for rule R02
:goal {
  eq mesmes(< (res(trs,idRRS,started) sRS),</pre>
              (prop(tpr,idPR,notready,idRS,idRRS) sPR) >) = true .
}
:apply (rd) -- goal
```

6.5 **Procedure: Proof of Sufficient Condition (4) & (5)**

Since predicate *inv* typically is a conjunction of many predicates, it is better to prove each of them separately. Suppose $inv(S) = inv_1(S) \land inv_2(S) \land \cdots \land inv_n(S)$, then we can separately prove the invariant property of each $inv_k(S)$ since the followings hold:

$$\forall S \in St : (\forall k : init(S) \to inv_k(S)) \to (init(S) \to inv(S))$$

$$\forall (S, S') \in Tr : (\forall k : inv(S) \to inv_k(S')) \to (inv(S) \to inv(S'))$$

(**a**))

....

. . . .

The rest of this section describes the proof procedure for three typical kinds of invariants in the CloudFormation example case.

Proof of Invariants for Local State Constraints

The most typical kind of invariants other that well-formed state predicates is for constraints about local states of objects. For example, inv-ifRSStartedThenPRReady says that every started parent resource has ready properties only. It is defined by using a predefined predicate ifXInStatesThenZInStates (renamed as ifRSInStatesThenPRInStates). Since the framework provides many lemmas for predefined predicates, it is easy to prove the invariant property of such a predicate.

Step 4-0: Define a predicate to be proved. Predicate initinv for condition (4) can be defined as follows:

```
vars S : State
pred invK : State
pred initinv : State
eq initinv(S) = init(S) implies invK(S) .
```

eq invK(S) = inv-ifRSStartedThenPRReady(S) .

Step 4-1: Instantiate proved lemmas for predefined predicates. As described in Section 5.3.2, proved lemma m2o-lemma07 can be instantiated and used for proof of condition (4) as follows:

```
var SetRS : SetOfResource
var SetPR : SetOfProperty
-- Instantiating m2o-lemma07:
-- eq m2o-lemma07(S_X,SX,St_X,S_Z,St_Z)
-- = allObjInStates(S_X,SX) implies
-- ifXInStatesThenZInStates(S_X,St_X,S_Z,St_Z)
-- when not (SX \in St_X) .
eq [m2o-lemma07]:
   (allRSInStates(SetRS,initial) and
    ifRSInStatesThenPRInStates(SetRS,started,SetPR,ready))
 = allRSInStates(SetRS,initial) .
```

Step 4-2: Begin with the most general case.

The most general case is as follows where sRS and sPR are proof constants for a set of resources and properties respectively:

```
:goal {
   eq initinv(< sRS,sPR >) = true .
}
:apply (rd) -- goal
```

The instantiated proved lemma is effective enough to prove the most general goal.

Step 5-0: Define a predicate to be proved. Using the double negation idiom, predicate invinv for condition (5) can be defined as follows:

```
eq invK(S) = inv-ifRSStartedThenPRReady(S) .
```

However inv(S) includes $inv_k(S)$, the antecedent part of iinv(S) doubly specifies invK(S). This is because inv(S) is defined only to reduce to false when one of invK(S) reduces to false as described in Section 6.1.

Step 5-1: Instantiate proved lemmas for predefined predicates. Rule R02 increases ready properties which has intuitively no effect on inv-ifRSStartedThenPRReady. As explained in Section 5.3.2, proved lemma m2o-lemma11 ensures it and can be used for proof of condition (5) as follows:

```
vars IDRS IDRRS : RSID
var IDPR : PRID
var TPR : PRType
var SetRS : SetOfResource
var SetPR : SetOfProperty
-- Instantiating m2o-lemma11:
-- eq m2o-lemma11(Z,Z',S_X,St_X,S_Z,St_Z)
     = ifXInStatesThenZInStates(S_X,St_X,(Z S_Z),St_Z)
         implies ifXInStatesThenZInStates(S_X,St_X,(Z' S_Z),St_Z)
     when (state(Z') \setminus St_Z) and changeObjState(Z,Z').
_ _
eq [m2o-lemma11]:
   (ifRSInStatesThenPRInStates
    (SetRS, started, (prop(TPR, IDPR, notready, IDRS, IDRRS) SetPR), ready)
   and
    ifRSInStatesThenPRInStates
    (SetRS,started,(prop(TPR,IDPR, ready,IDRS,IDRRS) SetPR),ready))
   _
    ifRSInStatesThenPRInStates
    (SetRS, started, (prop(TPR, IDPR, notready, IDRS, IDRRS) SetPR), ready) .
```

Step 5-2: Begin with the cases each of which matches to LHS of each rule.

Step 5-3: Split the current case for a rule into cases where the condition of the rule does or does not hold.

We can begin with two cases for two rules. Since rule R01 is conditional, the general case should be split into two cases according to Step 5-3. The first case should be split into more two cases where the set of properties is or is not empty. Then, the goals of all four cases can be proved and thus condition (5) is proved as follows:

```
-- Goal of Condition (5) for rule R01
:goal {
  eq invinv(< (res(trs,idRS,initial) sRS), sPR >) = true .
}
:ctf {
  eq allPROfRSInStates(sPR,idRS,ready) = true .
}
-- Case 1: When the condition of R01 holds:
:ctf {
 eq sPR = empPR.
}
-- Case 1-1: sPR is empty.
:apply (rd) -- 1-1
-- Case 1-2: sPR is not empty.
:apply (rd) -- 1-2
-- Case 2: When the condition of R01 does not hold:
:apply (rd) -- 2
-- Goal of Condition (5) for rule R02
:goal {
 eq invinv(< (res(trs,idRRS,started) sRS),</pre>
              (prop(tpr,idPR,notready,idRS,idRRS) sPR) >) = true .
}
:apply (rd) -- goal
```

Proof of Invariants for Structural Constraints

We should prove all of the wfs predicates as invariants, however, they are included in *init* and so we only need to prove condition (5) for each of them. Most of them check some structural constraints of the cloud systems, which should usually keep to hold when some transition rule changes a local state only and does not change any links of some object. When a wfs predicate is defined using predefined predicates, it is easy to prove the invariant property of the wfs because the framework provides many lemmas for the predefined predicates.

Here we use wfs-allPRHaveRS as an example to show the procedure.

Step 5-0: Define a predicate to be proved.

```
var S : State
eq invK(S) = wfs-allPRHaveRS(S) .
```

Step 5-1: Instantiate proved lemmas for predefined predicates. Since wfs-allPRHaveRS uses the predefined predicate allZHaveX, the proved lemma m2o-lemma05 can be instantiated and used for proof of condition (5) as follows:

```
var IDRS : RSID
var TPR : PRType
var SetRS : SetOfResource
var SetPR : SetOfProperty
-- Instantiating m2o-lemma05:
-- eq m2o-lemma05(X,X',S_Z,S_X)
-- = allZHaveX(S_Z,(X S_X)) implies allZHaveX(S_Z,(X' S_X))
```

```
-- when id(X) = id(X') .
eq [m2o-lemma05]:
   (allPRHaveRS(SetPR,(res(TRS,IDRS,initial) SetRS))
    and allPRHaveRS(SetPR,(res(TRS,IDRS,started) SetRS)))
= allPRHaveRS(SetPR,(res(TRS,IDRS,initial) SetRS)) .
```

Step 5-2: Begin with the cases each of which matches to LHS of each rule. **Step 5-3:** Split the current case for a rule into cases where the condition of the rule does or does not hold.

```
-- Goal of Condition (5) for rule R01
:goal {
 eq invinv(< (res(trs,idRS,initial) sRS), sPR >) = true .
}
:ctf {
  eq allPROfRSInStates(sPR,idRS,ready) = true .
}
-- Case 1: When the condition of R01 holds:
:apply (rd) -- 1
-- Case 2: When the condition of R01 does not hold:
:apply (rd) -- 2
-- Goal of Condition (5) for rule R02
:goal {
 eq invinv(< (res(trs,idRRS,started) sRS),</pre>
              (prop(tpr,idPR,notready,idRS,idRRS) sPR) >) = true .
}
:apply (rd) -- goal
```

Proof of *noCycle*^{*C*} as an Invariant

We should prove the invariant property of $noCycle_C(S)$ in order to use the Cyclic Dependency Lemma, however, it is included in *init* and thus we only need to prove condition (5) for $noCycle_C$. The Depending Subset Lemma in Section 5.3 ensures that we should prove that $\forall (S, S') \in Tr, \forall X \in C : DDS_C(X, S') \subseteq DDS_C(X, S)$ instead of condition (5).

Step 5-0: Define a predicate to be proved.

Step 5-1: Instantiate proved lemmas for predefined predicates.

As described in Section 5.3, the proved lemma m2o-lemma24 and set-lemma12 can be instantiated and used for proof as follows:

```
var S : State
vars RS RS' : Resource
var SetRS : SetOfResource
var SetSRS : SetOfRSState
var SetPR : SetOfProperty
-- Instantiating set-lemma12:
-- eq set-lemma12(S) = subset(S,S) .
eq [set-lemma12]:
  subset(SetRS,SetRS) = true .
-- Instantiating m2o-lemma24:
-- eq m2o-lemma24(X,X',S_X,S_Z,St_X)
     = subset(getXsOfZsInStates((X' S_X),S_Z,St_X),
___
              getXs0fZsInStates((X S_X),S_Z,St_X))
     when id(X) = id(X') and not state(X') \setminus in St_X.
_ _
ceq [m2o-lemma24]:
  subset(getRRSsOfPRsInStates((RS' SetRS),SetPR,SetSRS),
         getRRSsOfPRsInStates((RS SetRS),SetPR,SetSRS))
  = true
  if id(RS) = id(RS') and not state(RS') \in SetSRS .
```

Step 5-2: Begin with the cases each of which matches to LHS of each rule. **Step 5-3:** Split the current case for a rule into cases where the condition of the rule does or does not hold.

The following is a proof score for $DDS_C(X, S') \subseteq DDS_C(X, S)$ for rule R01:

```
:goal {
  eq invnoRSCycle(x,< (res(trs,idRS,initial) sRS), sPR >) = true .
}
:ctf {
  eq allPROfRSInStates(sPR,idRS,ready) = true .
}
-- Case 1: When the condition of R01 holds:
:ctf {
  eq x = res(trs, idRS, initial).
}
-- Case 1-1: X is the resource with identifier idRS.
:apply (rd) -- 1-1
-- Case 1-2: X is not the resource with identifier idRS.
:ctf {
 eq state(x) = initial .
}
-- Case 1-2-1: The resource is initial.
:apply (rd) -- 1-2-1
-- Case 1-2-2: The resource is not initial.
:apply (rd) -- 1-2-2
-- Case 2: When the condition of R01 does not hold:
:apply (rd) -- 2
```

Additionally two :ctf commands are required to split Case 1 into three more cases since the considering global state explicitly includes a resource with identifier idRS. The three cases are where the considering resource x is the resource idRS (Case 1-1), is not idRS and is initial (Case 1-2-1), and is neither idRS nor initial (Case 1-2-2).

The following is a proof score for $DDS_C(X, S') \subseteq DDS_C(X, S)$ for rule R02:

```
:goal {
 eq invnoRSCycle(x,
        < (res(trs,idRRS,started) sRS),
          (prop(tpr,idPR,notready,idRS,idRRS) sPR) >) = true .
}
:ctf {
 eq x = res(trs,idRRS,started) .
-- Case 1: X is the resource with identifier idRRS.
:apply (rd) -- 1
-- Case 2: X is not the resource with identifier idRRS.
:ctf {
  eq state(x) = initial .
}
-- Case 2-1: The resource is initial.
:ctf {
 eq id(x) = idRS.
}
-- Case 2-1-1: The identifier of X is idRS.
:apply (rd) -- 2-1-1
-- Case 2-1-2: The identifier of X is not idRS.
:apply (rd) -- 2-1-2
-- Case 2-2: The resource is not initial.
:apply (rd) -- 2-2
```

Similarly, additional case splitting is required since the considering global state includes two identifiers of resources. We need to consider cases where x is or is not idRS or idRRS.

6.6 A Lemma for Using Cyclic Dependency Lemma

Let us return to proof of condition (2) for rule R02.

Step 2-1: Begin with the cases each of which matches to LHS of each rule.

Step 2-2: Split the current case for a rule into cases where the condition of the rule does or does not hold.

Rule R02 is unconditional.

Step 2-3: Split the current case into cases where predicate *final* does or does not hold in the next state.

If all of the other resources are started, the next state is final. But it is not the case because we know a notready property has an initial parent resource.

Step 2-7: When there is a dangling link, split the current case into cases where the linked object does or does not exist.

```
-- The parent resource of the property does or does not exist.
:csp {
 eq existRS(sRS,idRS) = false .
 eq sRS = (res(trs',idRS,srs') sRS') .
}
-- Case 1: When the parent resource of the property does not exist:
:apply (rd) --1
-- Case 2: When the parent resource of the property exists:
-- The parent resource is initial or started.
:csp {
 eq srs' = initial .
 eq srs' = started .
}
-- Case 2-1: When the parent resource is initial:
... -- More consideration needed.
-- Case 2-2: When the parent resource is started:
:apply (rd) -- 2-2
```

Case 2-1 for rule R02 is the same situation as Case 1-2 for R01 where there is an initial resource in the next state and the Cyclic Dependency Lemma ensures there exists some initial resource RS such that no resource in DDSC(RS,S) is initial. Thus, here we need to write almost the same proof score as of Case 1-2 for R01. In addition, since we choose an arbitrary initial resource in Case 1-2 for R01, we can assume itself is the resource RS which the Cyclic Dependency Lemma ensures to exist. In this case, however, the initial resource we have is a parent of the property which rule R02 make transit. It means that we should consider two similar cases where the resource RS is the parent resource or another arbitrary resource. We might have to repeat almost the same proof totally three times.

Thereby, it is wise to define a lemma and use it in the similar cases. The lemma claims that if there is an initial resource in a global state then there exists a transition rule applicable to the global state. It can be proved similar to the proof of condition 1 as follows. **Step 1-0:** Define a predicate to be proved.

```
vars B1 B2 : Bool
pred (_when _) : Bool Bool { prec: 64 r-assoc }
eq (B1 when B2)
        = B2 implies B1 .
var S: State
pred invcont : State
eq invcont(S)
        = cont(S) = true
      when inv(S) .
```

Step 1-1: Begin with the most general case.

:goal {eq invcont(< (res(trs, idRS, initial) sRS), sPR >) = true .}

Step 1-2: Consider which rule can be applied to the global state in the current case. The rule is referred to as the *current rule*.

The applicable transition may be R01 because the global state includes an initial resource.

Step 1-3: Split the current case into cases which collectively cover the current case and one of which matches to LHS of the current rule.

The global state already matches to LHS of R01.

Step 1-4: Split the current case into cases where the condition of the current rule does or does not hold.

```
:csp {
    eq allPROfRSInStates(sPR,idRS,ready) = true .
    eq sPR = (prop(tpr,idPR,notready,idRS,idRRS) sPR') .
}
-- Case 1: When all of or properties of the resource idRS are ready:
:apply (rd) -- 1
```

Step 1-5: When there is a dangling link, split the current case into cases where the linked object does or does not exist.

```
-- Case 2: When at least one of properties of the resource idRS is notready.
-- The resource referred by the property does or does not exist.
:csp {
    eq existRS(sRS,idRRS) = false .
    eq sRS = (res(trs',idRRS,srs) sRS') .
}
-- Case 2-1: When the resource referred by the property does not exist:
:apply (rd) -- 2-1
-- Case 2-2: When the resource referred by the property exists:
```

Step 1-2: Consider which rule can be applied to the global state in the current case. In this case, the transition rule to be applied may be R02 because the global state includes a property.

Step 1-3: Split the current case into cases which collectively cover the current case and one of which matches to LHS of the current rule.

```
-- The state of the resource is initial or started.
:csp {
   eq srs = initial .
   eq srs = started .
}
```

Step 1-6: When falling in a cyclic situation, use the Cyclic Dependency Lemma.

-- Case 2-2-1: When the resource idRRS is initial:
-- The Cyclic Dependency Lemma rejects this case.

```
:init [Cycle] by {
  T:RSType <- trs;
  IDRS:RSID <- idRS;
  S:State <- < (res(trs,idRS,initial) sRS), sPR >;
}
:apply (rd) -- 2-2-1
-- Case 2-2-2: When the resource idRRS is started:
:apply (rd) -- 2-2-2
```

Thus, all of the cases are successfully proved and we can assume that cont(S) holds for any global state S which include an initial resource.

Assuming that *inv* holds, this lemma can be used as follows:

```
var IDRS : RSID
var TRS : RSType
var SetRS : SetOfResource
var SetPR : SetOfProperty
eq cont(< (res(TRS,IDRS,initial) SetRS), SetPR >) true .
```

Then, the proof of the sufficient condition (2) for rule R02 becomes very simple as follow:

```
-- Goal of Condition (2) for rule R02
:goal {
 eq contcont(< (res(trs,idRRS,started) sRS),</pre>
                (prop(tpr,idPR,notready,idRS,idRRS) sPR) >) = true .
}
-- The parent resource of the property does or does not exist.
:csp {
 eq existRS(sRS,idRS) = false .
 eq sRS = (res(trs',idRS,srs') sRS') .
}
-- Case 1: When the parent resource of the property does not exist:
:apply (rd) -- 1
-- Case 2: When the parent resource of the property exists:
-- The parent resource is initial or started.
:csp {
 eq srs' = initial .
 eq srs' = started .
}
-- Case 2-1: When the parent resource is initial:
:apply (rd) -- 2-1
-- Case 2-2: When the parent resource is started:
:apply (rd) -- 2-2
```

6.7 Recommended Module Structure

The framework provides a recommended module structure which the user can adopt when developing proof scores for verifying the property (*init* leads-to *final*). Using the recommended structure results in proof scores which are consistent and easier to understand. Figure 6.3 depicts



Figure 6.3: Recommended Module Structure

the recommended module structure whereas each box represents a module and each dashed arrow represents a "protecting" or "extending" import of another module. An italic name means a template module.

The following list describes the role and content of each module:

• OBJECTCLASS_n

Module for each class of objects. This class should be named as representing the class appropriately. The name usually consists of upper case letters because the same name will be capitalized and used for the sort of the class. The contents of this module is as follows:

- 1. Protecting import the modules of other classes which this class links.
- 2. Extending import the template module OBJECTBASE and rename predefined sorts and operators for the class.
- 3. Define the constructor of the class.
- 4. Define literals of the type and local state of the class.
- 5. Define the selectors of the class.
- 6. Define operators that are specific to the class if any.
- LINKS

Module for links between objects.

- 1. Protecting import the modules of classes of links.
- 2. Extending import the template modules OBJLINKONE2ONE and OBJLINKMANY2ONE, and rename predefined sorts and operators for links between objects.

• STATE

Module for global states.

- 1. Protecting import LINKS.
- 2. Define sort State for representing global states. A global state is usually represented as a tuple of sets of objects, each of the sets is a finite subset of a class.
- STATECyclefuns

Module for preparing to use the Cyclic Dependency Lemma.

- 1. Protecting import STATE.
- 2. Define operator getAllObjInState.
- 3. Define operator DDSC.

• STATEfuns

Module for defining many kinds of operators for global states.

- 1. Protecting import STATE.
- 2. Extending import the template module CYCLEPRED with STATECyclefuns as a parameter module, and rename predefined operator noCycleC.
- 3. Define wfs predicates.
- 4. Define predicates init, final, and wfs.
- 5. Define operators required to implement standard predicates above if any.

• STATERules

Module for transition rules.

- 1. Protecting import STATEfuns.
- 2. Define transition rules.

• ProofBase

Module for common definitions to prove five sufficient conditions.

- 1. Protecting import STATERules.
- 2. Define invariant predicates.
- 3. Define predicate cont.
- 4. Define operator m.
- 5. Define predicate inv such that it reduces to false when one of invariants reduces to false.
- 6. Define problem specific lemmas if any.
- 7. Prepare proof constants.
- ProofInitCont

Module for proving sufficient condition (1).

1. Protecting import ProofBase.

- 2. Define predicate initcont.
- 3. Define problem specific lemmas if any.
- ProofContCont

Module for proving sufficient condition (2).

- 1. Protecting import ProofBase.
- 2. Define predicate contcont.
- 3. Define problem specific lemmas if any.

• ProofMeasure

Module for proving sufficient condition (3).

- 1. Protecting import ProofBase.
- 2. Define predicate mesmes.
- 3. Define axioms of Nat.
- 4. Define problem specific lemmas if any.
- ProofInv

Module for common definitions for proving sufficient condition (4) and (5).

- 1. Protecting import ProofBase.
- 2. Define predicates invK, initinv, and invinv.

• Proofinv-* Proofwfs-*

Module for proving each invariant. The name of this module is usually **Proof**+*name_of_invariant*.

- 1. Protecting import ProofInv.
- 2. Define predicates invK to be the invariant.
- 3. Define lemmas if necessary.

6.8 Considerations on Sound Proof Scores

6.8.1 Usage of Equivalent Operator _ == _

As described in Section 3.3, term1 == term2 reduces to true if both terms are reduced to be the same term and to false otherwise. On the other hand, term1 = term2 reduces to true iff term1 == term2 reduces to true. This means that there is a case where term1 == term2 reduces to false and term1 = term2 does not so. Thus the users should not carelessly use _ == _ operator because it may lead unintended results.

The framework recommends using $_{-} = _{-}$ operator only in the following three cases:

1. As equal operator $_{-} = _{-}$ for literals:

Three of sorts provided by the framework, such as ObjIDLt, ObjTypeLt and ObjStateLt, are to represent literals. A literal is a constant for which the framework predefines a special equality predicate such that $_{-} = _{-}$ is exactly the same as $_{-} = = _{-}$. Since a Boolean

term "*literal*₁ = *literal*₂" always reduces to false, the users should not write such Boolean terms in their proof scores.

2. In the double negation idiom:

As described in Section 3.3, the double negation idiom uses " $_{-} = true$ " to stop the search when there is a next state where the specified condition cannot reduce to either true or false.

3. To keep the confluence property in the case splitting:

The following set of three equations are not confluent because p(s) reduces to true when equation (2) is used but it also reduces to p(s') when equation (3) is firstly used:

```
pred p : SetOfObject
eq p(0:Object S:SetOfObject) = p(S) . -- (1)
ops s s' : -> SetOfObject
op o : -> Object
eq p(s) = true . -- (2)
eq s = (o s') . -- (3)
```

As described in Section 6.3, this situation sometimes occurs when being guided by the proof procedure of the framework. For example, in the current case, p(s) matches to the condition part of a transition rule and the case should be split into two more cases where set of object s, is or not is empty. While we may avoid this situation by changing the order of the case splitting guided by the framework, it requires careful considerations and results in proof scores difficult to understand and maintain. Thus, we decided to recommend writing proof codes which explicitly ensure the confluent property as follows:

```
:set(normalize-init,on)
:init ( ceq B1:Bool = true if not B2:Bool . ) by {
  B1:Bool <- p(s) ;
  B2:Bool <- p(s) == true ;
}
:set(normalize-init,off)</pre>
```

When CafeOBJ processes as p(s) reduces to true, the :init command introduces the following meaningless equation:

ceq true = true if not true .

Otherwise, when p(s) reduces to p(s'), it introduces the following desired equation:

ceq p(s') = true if not false.

6.8.2 Usage of Search Predicates

When the behavior model is not *coherent*, search predicates may not be able to search all possible transitions. Coherence means that, given a global state term S, for any next state S^R of S such that some transition rule R makes S transit to S^R , if S reduces to S' then there exists some rule R' which makes S' transit to $S^{R'}$ such that both S^R and $S^{R'}$ reduce to the same global state term S^* [19]. Otherwise, there may be two different next states of S and a search predicate can search only one of them depending on whether transition rules or equations are used firstly.

In general, it is difficult to keep behavior model coherent. However, if the users of the framework go along with the following three rules, then search predicates can search next states of the given global state terms without depending on the order to use transition rules and equations:

- 1. A global state term included in the top goal of a proof should be a ground constructor term which consists of the constructors declared in the structure model and fresh proof constants, e.g., < sRS, sPR >.
- 2. When a current case is split and an equation is introduced whose LHS is a proof constant in the current goal, RHS of the equation should be a ground constructor term which consists of the constructors declared in the structure model and fresh proof constants, e.g., eq sRS = (res(trs',idRS,srs') sRS'). Moreover, any pair of equations in a proof case does not define the same proof constant.
- 3. A global state term included in LHS or RHS of a transition rule should be a constructor term, e.g., < (res(TRS, IDRS, started) SetRS), SetPR >.

Let the goal and proof constants in a proof case and transition rules in the model follow the above rules. We say a term as *a ground semi-constructor term* iff it consists of only the constructors declared in the structure model and proof constants. We also say a ground term *has a canonical form* iff it reduces to a single term regardless of the order in which the equations are applied.

Lemma 13 Let c be a constructor whose arity is n and let ground terms $g_i, 1 \le i \le n$ have canonical forms. Then, ground term $c(g_1, \ldots, g_n)$ has a canonical form.

Lemma 14 A ground semi-constructor term in a proof case has a canonical form.

Proof: Let a, b be proof constants in the proof case and let a > b mean that there is an equation whose LHS is a and RHS includes b in the proof case, then > is a partial order of proof constants assuming that they follow the above rules. This lemma can be proved using the mathematical induction about the partial order.

- **Base case:** When the ground semi-constructor term does not include any defined proof constants, it is a ground constructor term and it always reduces to itself.
- **Induction case:** Let *a* be a defined proof constant and let us assume that any ground semiconstructor term, including proof constants all of which are less than *a*, has a canonical form. Let *T* be a ground semi-constructor term whose included proof constants are less than *a* or *a* itself. Any subterm of *T* except *a* has a canonical form because of the induction hypothesis. The equation which defines *a* rewrites term *a* to its RHS which has a canonical form because of the induction hypothesis. The lemma 13 guarantees that a term consisting of a constructor which has *a* as its argument has a canonical form. Thus, all subterms of *T* have canonical forms and *T* itself does so. \Box

Lemma 15 Let global state term S be a ground semi-constructor term and R a transition rule which makes S transit to next state S^R . If S reduces to S' then R also makes S' transit to S'^R such that both S^R and S'^R reduce to the same global state term S^* .

Proof: Let LHS of *R* be $C_L(V_1, \ldots, V_n)$ where C_L is a context with *n* holes and $V_i, 1 \le i \le n$, are variables placed in the holes. Similarly, let RHS of *R* be $C_R(V_1, \ldots, V_n)$ although context C_R may have less than *n* holes in which case several V_i 's are omitted. When *R* makes *S* transit to S^R , each variable V_i matches to some subterm t_i of *S*, i.e. $S = C_L(t_1, \ldots, t_n)$, thus $S^R = C_R(t_1, \ldots, t_n)$. Let t_i reduce to t_i^* , then $S' = C_L(t_1^*, \ldots, t_n^*)$ because it is the canonical form of *S*. Similarly S^R has a canonical form $S^* = C_R(t_1^*, \ldots, t_n^*)$. On the other hand, LHS $C_L(V_1, \ldots, V_n)$ matches to $S' = C_L(t_1^*, \ldots, t_n^*)$ where each V_i matches to t_i^* and thus *R* makes *S'* transit to S^* . \Box

When the goal and proof constants in a proof case and transition rules in the model follow the above three rules, the global state given to the search predicates is always a ground semiconstructor term. Then Lemma 15 ensures that the result of the search does not depend on the order to use transition rules and equations.

6.8.3 Usage of the Double Negation Idiom

It should be noted that the double negation idiom always returns true when there is no next state. The typical pitfall is to give the idiom a global state term which does not match to any LHS and condition of transition rules. Since the idiom is used for the sufficient conditions (2) (3) and (5), the users of the framework should carefully check the goal of proofs especially in Step 2-1, 2-2, 3-2, 3-3, 5-2, and 5-3.

A simple but effective way to check this pitfall is to temporally remove the inner "not" in the double negation idiom and see that the goal does not reduce to true. If the goal reduces to true regardless of whether the inner condition is or is not denied, it means that there is no next state of the given global state.

Chapter 7

Applying the Framework to TOSCA Specifications

This chapter describes how to use our framework to define behavior of TOSCA types and to verify that a specified topology can correctly automate to set up the cloud system.

7.1 Structure Model of TOSCA Templates

A TOSCA topology models a cloud system that it consists of four classes of objects corresponding to the four main kinds of elements of a topology, i.e. nodes, relationships, capabilities, and requirements. There is an additional object, a message pool, to represent messaging between resources inside of different VMs because they cannot communicate directly. The message pool is simply a bag of messages, which abstracts implementations of messaging.

There are several domain specific constraints of the structure:

- 1. A node should be hosted on at most one other node.
- 2. A relationship should not relate a capability and a requirement of the same node.
- 3. A local relationship should relate a capability and a requirement of the nodes hosted on the same virtual machine.
- 4. A remote relationship should relate a capability and a requirement of the nodes hosted on the different virtual machines.
- 5. We assume that types of capabilities and requirements are the same as relationships that link them in this dissertation for the sake of simplicity.

7.1.1 Representation of the Example Structure Model

Let us use a typical example where four node types and three relationship types in Fig. 2.6 participate in automation of a setup operation. There are nine nodes of four types, nine capabilities, nine requirements, and nine relationships of three types. An initial global state may be represented in CafeOBJ as the following ground term:

< (node(VM, VMApache, initial) node(OS, OSApache, initial)

```
node(MW, ApacheWebServer, initial)
 node(SC, CRMApp, initial)
 node(SC, PhpModule, initial)
 node(VM, VMMySQL, initial)
 node(OS, OSMySQL, initial)
 node(MW, MySQL, initial)
 node(SC, CRMDB, initial) ),
( cap(hostedOn, VMApacheOS, closed, VMApache)
 cap(hostedOn, OSApacheSoftware, closed, OSApache)
 cap(hostedOn, ApacheWebServerWebapps, closed, ApacheWebServer)
 cap(hostedOn, ApacheWebServerModules, closed, ApacheWebServer)
 cap(dependsOn, PhpModulePhpApps, closed, PhpModule)
 cap(hostedOn, VMMySQLOS, closed, VMMySQL)
 cap(hostedOn, OSMySQLSoftware, closed, OSMySQL)
 cap(hostedOn, MySQLDatabases, closed, MySQL)
 cap(connectsTo, CRMDBClients, closed, CRMDB) ),
( req(hostedOn, OSApacheContainer, unbound, OSApache)
 req(hostedOn, ApacheWebServerContainer, unbound, ApacheWebServer)
 req(dependsOn, CRMAppPhpRuntime, unbound, CRMApp)
 reg(connectsTo, CRMAppDatabase, unbound, CRMApp)
 req(hostedOn, CRMAppContainer, unbound, CRMApp)
 req(hostedOn, PhpModuleContainer, unbound, PhpModule)
 req(hostedOn, OSMySQLContainer, unbound, OSMySQL)
 req(hostedOn, MySQLContainer, unbound, MySQL)
 req(hostedOn, CRMDBContainer, unbound, CRMDB) ),
( rel(hostedOn, OSApacheHostedOnVMApache,
     VMApacheOS, OSApacheContainer)
 rel(hostedOn, ApacheHostedOnOSApache,
     OSApacheSoftware, ApacheWebServerContainer)
 rel(hostedOn, CRMAppHostedOnApache,
     ApacheWebServerWebapps, CRMAppContainer)
 rel(hostedOn, PhpModuleHostedOnApache,
     ApacheWebServerModules, PhpModuleContainer)
 rel(dependsOn, CRMAppDependsOnPhpModule,
     PhpModulePhpApps, CRMAppPhpRuntime)
 rel(hostedOn, OSMySQLHostedOnVMMySQL,
     VMMySQLOS. OSMySQLContainer)
 rel(hostedOn, MySQLHostedOnOSMySQL,
     OSMySQLSoftware, MySQLContainer)
 rel(hostedOn, CRMDBHostedOnMySQL,
     MySQLDatabases, CRMDBContainer)
 rel(connectsTo, CRMAppConnectsToCRMDB,
     CRMDBClients, CRMAppDatabase) ),
empMsg >
```

The constructor name represents the class of the object (node, cap, req, rel), the first argument is its type (VM, hostedOn, and so on), the second is its identifier (VMApache, VMApacheOS, and so on), and the third is its local state. The fourth argument of the capability or requirement object represents a link to its parent. The fourth and fifth arguments of the relationship object represent links to its corresponding capability and requirement respectively. The last term, empMsg, represents an empty message pool.

The representation of these four classes can be easily defined using the template module OBJECTBASE provided by the framework. Module NODE for the node class is as follows:

```
module! NODE {
    -- Instantiation of Template
    extending(OBJECTBASE
        * {sort ObjIDLt -> NDIDLt,
           sort ObjID -> NDID,
           sort ObjTypeLt -> NDTypeLt,
           sort ObjType -> NDType,
           sort ObjStateLt -> NDStateLt,
           sort ObjState -> NDState,
           sort Object -> Node,
           sort SetOfObject -> SetOfNode,
           sort SetOfObjState -> SetOfNDState,
           op empObj -> empND,
           op empState -> empSND,
           op existObj -> existND,
           op existObjInStates -> existNDInStates,
           op uniqObj -> uniqND,
           op #ObjInStates -> #NodeInStates,
           op getObject -> getNode,
           op allObjInStates -> allNDInStates,
           op allObjOfTypeInStates -> allNDOfTypeInStates,
           op allObjNotInStates -> allNDNotInStates,
           op someObjInStates -> someNDInStates})
  -- Constructor
  -- node(NDType, NDID, NDState) is a Node.
  op node : NDType NDID NDState -> Node {constr}
  -- There are four typical node types.
  ops VM OS MW SC : -> NDTypeLt {constr}
  -- Variables
  var TND : NDType
  var IDND : NDID
  var SND : NDState
  -- Selectors
  eq type(node(TND,IDND,SND)) = TND .
  eq id(node(TND,IDND,SND)) = IDND .
  eq state(node(TND,IDND,SND)) = SND .
  -- Local States
  ops initial created started : -> NDStateLt {constr}
  -- Predicate for Local States
  pred isCreated : NDState
  eq isCreated(initial) = false .
  eq isCreated(created) = true .
```

```
eq isCreated(started) = true .
}
```

The types of nodes are VM (virtual machine), OS (operating system), MW (middleware), and SC (software component). The local states of nodes are initial, created, and started. Among them, created and started are isCreated.

In addition to the predefined predicates/operators explained in Section 5.2, module NODE instantiates a predicate concerning the node types, allObjOfTypeInStates, described as follows whereas argument *seto* is a set of linking objects, *setls* is a set of local states of linking objects, and *ty* is a type of an object:

• allObjOfTypeInStates (renamed as allNDOfTypeInStates) Predicate used as allObjOfTypeInStates(*seto*,*ty*,*setls*) which holds iff every object of type *ty* in *seto* is in one of local states of *setls*;

 $\forall o \in seto : type(o) = ty \rightarrow state(o) \in setls.$

Since a capability links to its parent node, module CAPABILITY for its class protecting includes NODE as follows:

```
module! CAPABILITY {
  protecting(NODE)
  -- Instantiation of Template
  extending(OBJECTBASE
        * {sort ObjIDLt -> CPIDLt,
           sort ObjID -> CPID,
           sort ObjTypeLt -> CPTypeLt,
           sort ObjType -> CPType,
           sort ObjStateLt -> CPStateLt,
           sort ObjState -> CPState,
           sort Object -> Capability
           sort SetOfObject -> SetOfCapability,
           sort SetOfObjState -> SetOfCPState,
           op empObj -> empCP,
           op empState -> empSCP,
           op existObj -> existCP,
           op existObjInStates -> existCPInStates,
           op uniqObj -> uniqCP,
           op #ObjInStates -> #CapabilityInStates,
           op getObject -> getCapability,
           op allObjInStates -> allCPInStates,
           op allObjOfTypeInStates -> allCPOfTypeInStates,
           op allObjNotInStates -> allCPNotInStates,
           op someObjInStates -> someCPInStates})
  -- Constructor
  -- cap(CPType, CPID, CPState, NDID) is a Capability of a Node
  op cap : CPType CPID CPState NDID -> Capability {constr}
  -- Variables
  var TCP : CPType
```

```
var IDCP : CPID
 var SCP : CPState
 var IDND : NDID
  -- Selectors
 op node : Capability -> NDID
 eq type(cap(TCP,IDCP,SCP,IDND)) = TCP .
  eq id(cap(TCP,IDCP,SCP,IDND)) = IDCP .
  eq state(cap(TCP,IDCP,SCP,IDND)) = SCP .
  eq node(cap(TCP,IDCP,SCP,IDND)) = IDND .
  -- Local States
 ops closed open available : -> CPStateLt {constr}
  -- Predicate for Local States
 pred isActivated : CPState
 eq isActivated(closed) = false .
 eq isActivated(open) = true .
  eq isActivated(available) = true .
}
```

Note that node is a selector for a link to the parent node of the capability. The local states of capabilities are closed, open, and available. Among them, open and available are isActivated.

Since a requirement also links to its parent node, module REQUIREMENT for its class protecting includes NODE as follows:

```
module! REQUIREMENT {
  protecting(NODE)
  -- Instantiation of Template
  extending(OBJECTBASE
        * {sort ObjIDLt -> RQIDLt,
           sort ObjID -> RQID,
           sort ObjTypeLt -> RQTypeLt,
           sort ObjType -> RQType,
           sort ObjStateLt -> RQStateLt,
           sort ObjState -> RQState,
           sort Object -> Requirement,
           sort SetOfObject -> SetOfRequirement,
           sort SetOfObjState -> SetOfRQState,
           op empObj -> empRQ,
           op empState -> empSRQ,
           op existObj -> existRQ,
           op existObjInStates -> existRQInStates,
           op uniqObj -> uniqRQ,
           op #ObjInStates -> #RequirementInStates,
           op getObject -> getRequirement,
           op allObjInStates -> allRQInStates,
           op allObjOfTypeInStates -> allRQOfTypeInStates,
           op allObjNotInStates -> allRQNotInStates,
           op someObjInStates -> someRQInStates})
```

```
-- Constructor
-- req(RQType, RQID, RQState, NDID) is a Requirement of a Node
op req : RQType RQID RQState NDID -> Requirement {constr}
-- Variables
var TRQ : RQType
var IDRQ : RQID
var IDND : NDID
var SRQ : RQState
-- Selectors
op node : Requirement -> NDID
eq type(req(TRQ,IDRQ,SRQ,IDND)) = TRQ .
eq id(req(TRQ,IDRQ,SRQ,IDND)) = IDRQ .
eq state(req(TRQ,IDRQ,SRQ,IDND)) = SRQ .
eq node(req(TRQ,IDRQ,SRQ,IDND)) = IDND .
-- Local States
ops unbound waiting ready : -> RQStateLt {constr}
```

Note that node is a selector for a link to the parent node of the requirement. The local states of requirements are unbound, waiting, and ready.

Since a relationship links to both of its corresponding capability and requirement, module RELATIONSHIP for its class protecting includes CAPABILITY and REQUIREMENT as follows:

```
module! RELATIONSHIP {
  protecting(CAPABILITY + REQUIREMENT)
  -- Instantiation of Template
  extending(OBJECTBASE
        * {sort ObjIDLt -> RLIDLt,
           sort ObjID -> RLID,
           sort ObjTypeLt -> RLTypeLt,
           sort ObjType -> RLType,
           sort ObjStateLt -> RLStateLt,
           sort ObjState -> RLState,
           sort Object -> Relationship,
           sort SetOfObject -> SetOfRelationship,
           sort SetOfObjState -> SetOfRLState,
           op empObj -> empRL,
           op existObj -> existRL,
           op uniqObj -> uniqRL})
  -- Constructor
  -- rel(RLType, RLID, CPID, RQID) is a Relationship
  op rel : RLType RLID CPID RQID -> Relationship {constr}
  -- There are three typical relationship types.
  ops hostedOn dependsOn connectsTo : -> RLTypeLt {constr}
```

}

```
-- Types of capabilities and requirements are the same as relationships
  [RLType < CPType RQType]</pre>
  -- Variables
 var TRL : RLType
 var IDRL : RLID
 var IDCP : CPID
 var IDRQ : RQID
  -- Selectors
  op cap : Relationship -> CPID
 op req : Relationship -> RQID
  eq type(rel(TRL,IDRL,IDCP,IDRQ)) = TRL .
  eq id(rel(TRL,IDRL,IDCP,IDRQ)) = IDRL .
  eq cap(rel(TRL,IDRL,IDCP,IDRQ)) = IDCP .
  eq req(rel(TRL, IDRL, IDCP, IDRQ)) = IDRQ .
  -- Predicate for Locality
 pred isLocalRL : Relationship
  eq isLocalRL(rel(hostedOn,IDRL,IDCP,IDRQ)) = true .
  eq isLocalRL(rel(dependsOn,IDRL,IDCP,IDRQ)) = true .
  eq isLocalRL(rel(connectsTo,IDRL,IDCP,IDRQ)) = false .
}
```

Sort RLType is declared as a subsort of CPType and RQType which means types of relationships can be used as types of capabilities and requirements. The types of relationships are hostedOn, dependsOn, and connectsTo. Among them, hostedOn and dependsOn are isLocal. Note that cap and req are selectors for links to the corresponding capability and requirement respectively of the relationship.

Predefined predicates and operators for links between objects also can be easily instantiated using the template modules OBJLINKMANY2ONE and OBJLINKONE2ONE as follows:

```
module! LINKS {
  protecting(NODE + CAPABILITY + REQUIREMENT + RELATIONSHIP)
  -- Instantiation of Template
  -- A many-to-one link from a capability to its parent node
  extending(OBJLINKMANY2ONE(
        CAPABILITY {sort Object -> Capability,
                    sort ObjID -> CPID,
                    sort ObjType -> CPType,
                    sort ObjState -> CPState,
                    sort SetOfObject -> SetOfCapability,
                    sort SetOfObjState -> SetOfCPState,
                    sort LObject -> Node,
                    sort LObjID -> NDID,
                    sort LObjState -> NDState,
                    sort SetOfLObject -> SetOfNode,
                    sort SetOfLObjState -> SetOfNDState,
                    op getLObject -> getNode,
                    op existLObj -> existND,
```

```
op empLObj -> empND,
                  op link -> node,
                  op existLObjInStates -> existNDInStates})
      * {op getX0fZ -> getND0fCP,
         op getZsOfX -> getCPsOfND,
         op getZsOfTypeOfX -> getCPsOfTypeOfND,
         op getZsOfXInStates -> getCPsOfNDInStates,
         op getZs0fType0fXInStates -> getCPs0fType0fNDInStates,
         op getXsOfZs -> getNDsOfCPs,
         op getXsOfZsInStates -> getNDsOfCPsInStates,
         op getZsOfXs -> getCPsOfNDs,
         op getZs0fXsInStates -> getCPs0fNDsInStates,
         op getZsOfTypeOfXsInStates -> getCPsOfTypeOfNDsInStates,
         op allZHaveX -> allCPHaveND,
         op allZOfXInStates -> allCPOfNDInStates,
         op allZOfTypeOfXInStates -> allCPOfTypeOfNDInStates,
         op ifXInStatesThenZInStates -> ifNDInStatesThenCPInStates,
         op ifXInStatesThenZOfTypeInStates
            -> ifNDInStatesThenCPOfTypeInStates}
      )
-- Instantiation of Template
-- A many-to-one link from a requirement to its parent node
extending(OBJLINKMANY2ONE(
      REQUIREMENT {sort Object -> Requirement,
                   sort ObjID -> RQID,
                   sort ObjType -> RQType,
                   sort ObjState -> RQState,
                   sort SetOfObject -> SetOfRequirement,
                   sort SetOfObjState -> SetOfRQState,
                   sort LObject -> Node,
                   sort LObjID -> NDID,
                   sort LObjState -> NDState,
                   sort SetOfLObject -> SetOfNode,
                   sort SetOfLObjState -> SetOfNDState,
                   op getLObject -> getNode,
                   op existLObj -> existND,
                   op empLObj -> empND,
                   op link -> node,
                   op existLObjInStates -> existNDInStates})
      * {op getXOfZ -> getNDOfRQ,
         op getXsOfZs -> getNDsOfRQs,
         op getXsOfZsInStates -> getNDsOfRQsInStates,
         op getZsOfX -> getRQsOfND,
         op getZsOfTypeOfX -> getRQsOfTypeOfND,
         op getZsOfXInStates -> getRQsOfNDInStates,
         op getZsOfTypeOfXInStates -> getRQsOfTypeOfNDInStates,
         op getZsOfXs -> getRQsOfNDs,
         op getZsOfXsInStates -> getRQsOfNDsInStates,
         op getZsOfTypeOfXsInStates -> getRQsOfTypeOfNDsInStates,
```

```
op allZHaveX -> allRQHaveND,
         op allZOfXInStates -> allRQOfNDInStates,
         op allZOfTypeOfXInStates -> allRQOfTypeOfNDInStates,
         op ifXInStatesThenZInStates -> ifNDInStatesThenRQInStates,
         op ifXInStatesThenZOfTypeInStates
            -> ifNDInStatesThenRQOfTypeInStates}
      )
-- Instantiation of Template
-- A one-to-one link from a relationship to its capability
extending(OBJLINKONE2ONE(
      RELATIONSHIP {sort Object -> Relationship,
                    sort ObjID -> RLID,
                    sort ObjType -> RLType,
                    sort ObjState -> RLState,
                    sort SetOfObject -> SetOfRelationship,
                    sort SetOfObjState -> SetOfRLState,
                    sort LObject -> Capability,
                    sort LObjID -> CPID,
                    sort LObjState -> CPState,
                    sort SetOfLObject -> SetOfCapability,
                    sort SetOfLObjState -> SetOfCPState,
                    op getLObject -> getCapability,
                    op existLObj -> existCP,
                    op empLObj -> empCP,
                    op link \rightarrow cap,
                    op existLObjInStates -> existCPInStates})
      * {op existX -> existCP,
         op getX0fY -> getCP0fRL,
         op getXsOfYs -> getCPsOfRLs,
         op getXsOfYsInStates -> getCPsOfRLsInStates,
         op getYOfX -> getRLOfCP,
         op getYsOfXs -> getRLsOfCPs,
         op getYsOfXsInStates -> getRLsOfCPsInStates,
         op unigX \rightarrow unigCP.
         op YOfXInStates -> RLOfCPInStates,
         op ifXInStatesThenYInStates -> ifCPInStatesThenRLInStates,
         op ifYInStatesThenXInStates -> ifRLInStatesThenCPInStates,
         op allYHaveX -> allRLHaveCP,
         op allXHaveY -> allCPHaveRL,
         op onlyOneYOfX -> onlyOneRLOfCP}
      )
-- Instantiation of Template
-- A one-to-one link from a relationship to its relationship
extending(OBJLINKONE2ONE(
      RELATIONSHIP {sort Object -> Relationship,
                    sort ObjID -> RLID,
                    sort ObjType -> RLType,
                    sort ObjState -> RLState,
```

```
sort SetOfObject -> SetOfRelationship,
              sort SetOfObjState -> SetOfRLState,
              sort LObject -> Requirement,
              sort LObjID -> RQID,
              sort LObjState -> RQState,
              sort SetOfLObject -> SetOfRequirement,
              sort SetOfLObjState -> SetOfRQState,
              op getLObject -> getRequirement,
              op existLObj -> existRQ,
              op empLObj -> empRQ,
              op link -> req,
              op existLObjInStates -> existRQInStates})
* {op existX -> existRQ,
   op getXOfY -> getRQOfRL,
   op getXsOfYs -> getRQsOfRLs,
   op getXsOfYsInStates -> getRQsOfRLsInStates,
   op getYOfX -> getRLOfRQ,
   op getYsOfXs -> getRLsOfRQs,
   op getYsOfXsInStates -> getRLsOfRQsInStates,
   op uniqX -> uniqRQ,
   op YOfXInStates -> RLOfRQInStates,
   op ifXInStatesThenYInStates -> ifRQInStatesThenRLInStates,
   op ifYInStatesThenXInStates -> ifRLInStatesThenRQInStates,
   op allYHaveX -> allRLHaveRQ,
   op allXHaveY -> allRQHaveRL,
   op onlyOneYOfX -> onlyOneRLOfRQ}
)
```

Links from capabilities to their parent nodes and from requirements to their parent nodes are many-to-one, whereas links from relationships to their corresponding capabilities and requirements are one-to-one.

In addition to the predefined predicates/operators explained in Section 5.2, module LINKS uses OBJLINKMANY2ONE to instantiate several operators concerning object types. The following is a list of such operators whereas argument *seto* is a set of linking objects, *setls* is a set of local states of linking objects, *lobj* is a linked object, *lid* is an identifier of a linked object, *setlo* is a set of local states of linked objects, *setls* is a set of local states of linked objects, *setlls* is a set of local states of linked objects.

```
• allZOfTypeOfXInStates
```

}

(renamed as allCPOfTypeOfNDInStates and allRQOfTypeOfNDInStates) Predicate used as allZOfTypeOfXInStates(*seto*, *ty*, *lid*, *setls*) which holds iff every object included in *seto* whose type is *ty* and whose link is *lid* is in one of locals state in *setls*; $\forall o \in seto : (type(o) = ty \land link(o) = lid \rightarrow state(o) \in setls).$

- getZsOfTypeOfX (as getCPsOfTypeOfND and getRQsOfTypeOfND) Operator used as getZsOfTypeOfX(*seto*, *ty*, *lobj*) which returns a subset *seto* each of whose element object is of type *ty* and links to *lobj*.
- getZsOfTypeOfXInStates

 (as getCPsOfTypeOfNDInStates and getRQsOfTypeOfNDInStates)

Operator used as getZsOfTypeOfXInStates(*seto*, *tylobj*, *setls*) which returns a subset of *seto* each of whose element object is of type *ty*, links to *lobj*, and is in one of local states of *setls*.

• getZsOfTypeOfXsInStates

(as getCPsOfTypeOfNDsInStates and getRQsOfTypeOfNDsInStates) Operator used as getZsOfTypeOfXsInStates(*seto*, *ty*, *setlo*, *setls*) which returns a subset of *seto* each of whose element object is of type *ty*, links to some object included in *setlo*, and is in one of local states of *setls*.

• ifXInStatesThenZOfTypeInStates

(as ifNDInStatesThenCPOfTypeInStates and ifNDInStatesThenRQOfTypeInStates) Predicate used as ifXInStatesThenZOfTypeInStates(*setlo*,*ty*,*setlls*,*seto*,*setls*) which holds iff every object included in *setlo* whose type m is *ty* and whose local sate is included in *setlls* is linked by objects included in *seto* each of which is in one of local states in *setls*;

 $\begin{aligned} \forall lo \in setlo: \quad (type(lo) = ty \land state(lo) \in setlls \rightarrow \\ \forall o \in seto: (link(o) = id(lo) \rightarrow state(o) \in setls)). \end{aligned}$

Module LINKS also uses OBJLINKONE2ONE to instantiate many predicates/operators. The following is a list of such operators whereas argument *obj* is a linking object, *seto* is a set of linking objects, *setls* is a set of local states of linking objects, *lobj* is a linked object, *lid* is an identifier of a linked object, *setlo* is a set of linked objects, and *setlls* is a set of local states of linked objects:

existX (renamed as existCP and existRQ)
 Predicate used as existX(*seto*,*lid*) which holds iff some object whose link is *lid* is included in *seto*;

 $\exists o \in seto : link(o) = lid.$

- getXOfY (as getCPOfRL and getRQOfRL) Operator used as getXOfY(*setlo*, *obj*) which returns an object linked by *obj* and included in *setlo*.
- getXsOfYs (as getCPsOfRLs and getRQsOfRLs) Operator used as getXsOfYs(*setlo*, *seto*) which returns a subset of *setlo* each of whose element object is linked by some object included in *seto*.
- getXsOfYsInStates (as getCPsOfRLsInStates and getRQsOfRLsInStates) Operator used as getXsOfYsInStates(*setlo*, *seto*, *setlls*) which returns a subset of *setlo* each of whose element object is linked by some object included in *seto* and is in one of local states of *setlls*.
- getYOfX (as getRLOfCP and getRLOfRQ) Operator used as getYOfX(*seto*, *lobj*) which returns an object which included in *seto* and whose link is *lobj*.
- getYsOfXs (as getRLsOfCPs and getRLsOfRQs) Operator used as getYsOfXs(*seto*, *setlo*) which returns a subset of *seto* each of whose element object links to some object included in *setlo*.

- getYsOfXsInStates (as getRLsOfCPsInStates and getRLsOfRQsInStates) Operator used as getYsOfXsInStates(*seto*, *setlo*, *setls*) which returns a subset of *seto* each of whose element object links to some object included in *setlo* and is in one of local states of *setls*.
- uniqX (as uniqCP and uniqRQ)

Predicate used as uniqX(*seto*) which holds iff the link of each object is unique in *seto*; $\forall o, o' \in seto : (o \neq o' \rightarrow link(o) \neq link(o')).$

- YOfXInStates (as RLOfCPInStates and RLOfRQInStates)
 Predicate used as YOfXInStates(*seto*, *lid*, *setls*) which holds iff an object included in *seto* whose link is *lid* is in one of locals state in *setls*;
 ∃o ∈ seto: (link(o) = lid ∧ state(o) ∈ setls).
- ifXInStatesThenYInStates

(as if CPInStates Then RLInStates and if RQInStates Then RLInStates)

Predicate used as ifXInStatesThenYInStates(*setlo*, *setlls*, *seto*, *setls*) which holds iff every object included in *setlo* whose local sate is included in *setlls* is linked by an object included in *seto* which is in one of local states in *setls*;

 $\forall lo \in setlo : (state(lo) \in setlls \rightarrow \exists o \in seto : (link(o) = id(lo) \land state(o) \in setls)).$

ifYInStatesThenXInStates

(as ifRLInStatesThenCPInStates and ifRLInStatesThenRQInStates)

Predicate used as ifYInStatesThenXInStates(*seto*, *setls*, *setlo*, *setlls*) which holds iff every object included in *seto* whose local sate is included in *setls* links to an object included in *setlo* which is in one of local states in *setlls*;

 $\forall o \in seto : (state(o) \in setls \rightarrow \exists lo \in setlo : (link(o) = id(lo) \land state(lo) \in setlls)).$

• allYHaveX (as allRLHaveCP and allRLHaveRQ)

Predicate used as allYHaveX(*seto*, *setlo*) which holds iff every object included in *seto* has an object linked by it which is included in *setlo*;

 $\forall o \in seto, \exists lo \in setlo : id(lo) = link(o).$

- allXHaveY (as allCPHaveRL and allRQHaveRL)
 Predicate used as allXHaveY(*setlo*, *seto*) which holds iff every object included in *setlo* has an object which links to it and is included in *seto*;
 ∀lo ∈ setlo, ∃o ∈ seto : id(lo) = link(o).
- OnlyOneYOfX (renamed as onlyOneRLOfCP and onlyOneRLOfRQ) Predicate used as OnlyOneYOfX(*seto*,*lid*) which holds iff only one object whose link is *lid* is included in *seto*;

 $\exists o \in seto : link(o) = lid \land (\forall o' \in seto : o \neq o' \rightarrow link(o) \neq link(o')).$

A global state of the TOSCA structure models includes one additional object, a message pool. There are two kinds of messages, open messages and available messages, which will be explained in the next section. The representation of the messages is defined as follows:

```
module! MSG {
   protecting(LINKS)
   [Msg]
   -- An open message
```

```
op opMsg : CPID -> Msg {constr}
-- An available message
op avMsg : CPID -> Msg {constr}
vars IDCP1 IDCP2 : CPID
eq (opMsg(IDCP1) = opMsg(IDCP2))
  = (IDCP1 = IDCP2) .
eq (avMsg(IDCP1) = avMsg(IDCP2))
  = (IDCP1 = IDCP2) .
eq (opMsg(IDCP1) = avMsg(IDCP2))
  = false .
}
```

An open message (and also an available message) has an argument of the identifier of a capability. Open messages are equal to each other iff they have the same capability identifier, which is similar to available messages. An open message and an available message are never equal to each other.

The representation of a global state is defined by sort State as a tuple consisting of a set of nodes, a set of capabilities, a set of requirements, a set of relationships, and a message pool as follows whereas parameterized module BAG defines generic bags similarly to module SET explained in Section 3.1:

In addition to the instantiated operators from the predefined ones, it requires to define several problem specific operators in module STATEfuns. There are three kinds of them; (1) to represent invariants for the consistency between messages and local states of objects, (2) to represent invariants for the consistency between capabilities and requirements connected by relationships, and (3) to represent other problem specific constraints. All of these operators can be easily implemented by combining predefined operators.

The following is a list of such operators whereas argument setCP is a set of capabilities, setRQ is a set of requirements, setRL is a set of relationships, *node* is a node, *cap* is a capability, *req* is a requirement, *rel* is a relationship, *setlCP* is a set of local states of capabilities, *setlRQ* is a set of local states of requirements, and *pool* is a message pool¹:

allHostedOnCPInStates (categorized as (3) above)
 Predicate used as allHostedOnCPInStates(*setCP*, *setlCP*) which holds iff every capability included in *setCP* whose type is hostedOn is in one of locals state in *setlCP*;

 $\forall cap \in setCP : (type(cap) = hostedOn \rightarrow state(cap) \in setlCP).$

¹Note that here we do not distinguish between an object and its identifier for the sake of brevity.

• allHostedOnRQInStates (categorized as (3))

Predicate used as allHostedOnRQInStates(*setRQ*, *setlRQ*) which holds iff every requirement included in *setRQ* whose type is hostedOn is in one of locals state in *setlRQ*; $\forall req \in setRQ$: (type(*req*) = hostedOn \rightarrow state(*req*) $\in setlRQ$).

- allHostedOnRQOfNDInStates (categorized as (3))
 - Predicate used as allHostedOnRQOfNDInStates(setRQ, node, setlRQ) which holds iff every requirement included in setRQ whose type is hostedOn and whose parent is node is in one of locals state in setlRQ;

 $\forall req \in setRQ : (type(req) = hostedOn \land node(req) = node \rightarrow state(req) \in setlRQ).$

• getCPOfRQ (categorized as (2))

Operator used as getCPOfRQ(*setCP*, *setRL*, *req*) which returns the corresponding capability of *req* by firstly finding the corresponding relationship of *req* in *setRL* and then finding the corresponding capability of the relationship in *setCP*.

• getRQOfCP (categorized as (2))

Operator used as getRQOfCP(setRQ, setRL, cap) which returns the corresponding requirement of cap by firstly finding the corresponding relationship of cap in setRL and then finding the corresponding requirement of the relationship in setRQ.

• allRLHaveSameTypeCPRQ (categorized as (3))

Predicate used as allRLHaveSameTypeCPRQ(*setRL*, *setCP*, *setRQ*) which holds iff every relationship included in *setRL* has the corresponding capability included in *setCP* and the corresponding requirement included in *setRQ* and those three objects has the same type;

 $\forall rel \in setRL : \\ (\forall cap \in setCP : cap(rel) = cap \rightarrow type(rel) = type(cap)) \land \\ (\forall req \in setRQ : req(rel) = req \rightarrow type(rel) = type(req)).$

• allRLNotInSameND (categorized as (3))

Predicate used as allRLNotInSameND(*setRL*, *setCP*, *setRQ*) which holds iff every relationship included in *setRL* has the corresponding capability included in *setCP* and the corresponding requirement included in *setRQ* and their parent nodes are not the same;

 $\forall rel \in setRL, \exists cap \in setCP, \exists req \in setRQ : \\ cap(rel) = cap \land req(rel) = req \land node(cap) \neq node(req).$

- getHostedOnRQOfND (categorized as (3)) Operator used as getHostedOnRQOfND(*setRQ*, *node*) which returns the hostedOn requirement in *setRQ* whose parent is *node*.
- getHostedOnRQsOfNDInStates (categorized as (3)) Operator used as getHostedOnRQsOfNDInStates(*setRQ*, *node*, *setlRQ*) which returns the set of hostedOn requirements in *setRQ* whose parent is *node* and whose local state is in *setlRQ*.
- VMOfND (categorized as (3))
 Operator used as VMOfND(*node*, *setND*, *setCP*, *setRQ*, *setRL*) which returns the VM node which hosts *node*; precisely, the operator recursively traverses hostedOn requirements,

relationships, and capabilities starting from *node* and returns the first found VM node including *node* itself.

- VMOfCP (categorized as (3)) Operator used as VMOfCP(*cap*, *setND*, *setCP*, *setRQ*, *setRL*) which returns the VM node which hosts the parent node of *cap*.
- VMOfRQ (categorized as (3)) Operator used as VMOfRQ(*req*, *setND*, *setCP*, *setRQ*, *setRL*) which returns the VM node which hosts the parent node of *req*.
- allRLHoldLocality (categorized as (3)) Predicate used as allRLHoldLocality(*setRL*, *setND*, *setCP*, *setRQ*) which holds iff every relationship included in *setRL* satisfies the locality constraint, which means that if the type of a relationship is local, it should be between a capability and a requirement of the nodes hosted on the same virtual machine, while if the type is not local (i.e. remote), it should be between a capability and a requirement of the nodes hosted on the different virtual machines.
- allNDHaveAtMostOneHost (categorized as (3)) Predicate used as allNDHaveAtMostOneHost(*setND*, *setRQ*) which holds iff every node included in *setND* has 0 or 1 hostedOn requirement included in *setRQ*.
- ifOpenMsgThenCPInStates (categorized as (1))

Predicate used as ifOpenMsgThenCPInStates(*pool*, *setCP*, *setlCP*) which holds iff every open message included in *pool* has the corresponding capability which is included in *setCP* and whose local state is in *setlCP*;

 $\forall msg \in pool : (isOpen(msg) \rightarrow (\exists cap \in setCP : cap(msg) = cap \land state(cap) \in setICP)).$

• ifAvailableMsgThenCPInStates (categorized as (1))

Predicate used as ifAvailableMsgThenCPInStates(*pool*, *setCP*, *setlCP*) which holds iff every available message included in *pool* has the corresponding capability which is included in *setCP* and whose local state is in *setlCP*;

 $\forall msg \in pool : (isAvail(msg) \rightarrow (\exists cap \in setCP : cap(msg) = cap \land state(cap) \in setICP)).$

• ifCPInStatesThenRQInStates (categorized as (2))

Predicate used as ifCPInStatesThenRQInStates(*setCP*, *setlCP*, *setRQ*, *setlRQ*, *setRL*) which holds iff every capability included in *setCP* whose local sate is included in *setlCP* has the corresponding requirement included in *setRQ* whose local state is in *setlRQ*;

 $\begin{aligned} \forall cap \in setCP : (\texttt{state}(cap) \in setlCP \rightarrow \\ \exists rel \in setRL, req \in setRQ : \\ (\texttt{cap}(rel) = cap \land \texttt{req}(rel) = req \land \texttt{state}(req) \in setlRQ)). \end{aligned}$

• ifConnectsToCPInStatesThenRQInStatesOrOpenMsg (categorized as (1) (2)) Predicate used as ifConnectsToCPInStatesThenRQInStatesOrOpenMsg(*setCP*, *setlCP*, *setRQ*, *setRQ*, *setRL*, *pool*) which holds iff every connectsTo capability in *setCP* whose local sate is included in *setlCP* has the corresponding requirement included in *setRQ*
whose local state is in *setlRQ* or has the corresponding open message included in *pool*;

 $\begin{aligned} \forall cap \in setCP : (type(cap) = hostedOn \land state(cap) \in setlCP \rightarrow \\ (\exists rel \in setRL, req \in setRQ : \\ (cap(rel) = cap \land req(rel) = req \land state(req) \in setlRQ)) \lor \\ \exists msq \in pool : cap(msq) = cap \land isOpen(msq)). \end{aligned}$

• ifConnectsToCPInStatesThenRQInStatesOrAvailableMsg (categorized as (1) (2)) Predicate used as ifConnectsToCPInStatesThenRQInStatesOrAvailableMsg(*setCP*, *setlCP*, *setRQ*, *setlRQ*, *setRL*, *pool*) which holds iff every connectsTo capability included in *setCP* whose local sate is included in *setlCP* has the corresponding requirement included in *setRQ* whose local state is in *setlRQ* or has the corresponding available message included in *pool*;

 $\begin{aligned} \forall cap \in setCP : (type(cap) = hostedOn \land state(cap) \in setlCP \rightarrow \\ (\exists rel \in setRL, req \in setRQ : \\ (cap(rel) = cap \land req(rel) = req \land state(req) \in setlRQ)) \lor \\ \exists msg \in pool : cap(msg) = cap \land isAvail(msg)). \end{aligned}$

7.2 Behavior Model of TOSCA Templates

The framework models the behavior of an automated system operation as a state machine in which a set of transition rules of global states specifies the behavior. As described in Section 2.3, the behavior of a topology of TOSCA is decided by the behavior of types of nodes and relationships included in the topology. Here, we propose to model the behavior of a type as a set of transition rules each of which is called an *invocation rule* and specifies when a type operation can be invoked and how it changes the local state of a node or relationship of the type.

As described in Section 2.3, type operations and their invocation rules should be defined by type architects. When an application architect defines a topology, the set of all invocation rules of included node/relationship types collectively composes a state machine which specifies the whole behavior of the topology.

In the example of Fig. 2.6, we assume that behavior of four node types is the same focusing on when a node is created and started because they are the most essential for setup operations.

On the other hand, behavior of relationship types usually varies according to their nature; they may be in the IaaS layer or in the inside of VM layer, "local" or "remote", "immediate" or "await". Three relationship types of this example typically cover the variation. A HostedOn relationship is one between resources in the IaaS layer. It is "immediate", i.e. it can be established as soon as the target node is created. Each of DependsOn and ConnectsTo relationships is between resources inside of VMs and is "await", i.e. it should wait for the target node to be started. A DependsOn relationship is "local" in the same VM, while a ConnectsTo is "remote" to a different VM and should use some messages to notice the states of its capability to its requirement. We assume that a state of a relationship is a pair of the states of its capability and requirement in this dissertation for the sake of simplicity. Thereby, an operation of a relationship type changes the state of its capability or requirement.

Behavior of these types is depicted in Fig. 7.1. A solid arrow represents a state transition of each object caused by a type operation and a dashed arrow represents an invocation of a type operation or a message sending.

There are twelve invocation rules; two of them are for node operations, two are for operations of HostedOn relationship, four are for DependsOn, and four are for ConnectsTo. The



Figure 7.1: Typical Behavior of Relationship Types

followings are their detailed definitions explained in natural language:

Initial States: Every node is initially in a local state named as *initial*, every capability of the node is *closed*, and every requirement is *unbound*.

Invocation Rule of Node Type Operations:

- *CREATE* operation can be invoked if all of the HostedOn requirements of the node are *ready* and changes the local state of the node from *initial* to *created*.
- *START* operation can be invoked if all of the requirements are *ready* and changes the local state from *created* to *started*.

Invocation Rule of Operations of HostedOn Relationship Type:

- *CAPAVAILABLE* operation can be invoked if the target node is already created, i.e. *created* or *started* and changes the local state of its capability from *closed* to *available*.
- *REQREADY* operation can be invoked if its capability is *available* and changes the local state of the requirement from *unbound* to *ready*.

Invocation Rule of Operations of DependsOn Relationship Type:

- *CAPOPEN* operation can be invoked if the target node is already created. It changes the local state of its capability from *closed* to *open*.
- *CAPAVAILABLE* operation can be invoked if the target node is *started* and changes the local state of its capability from *open* to *available*.
- *REQWAITING* operation can be invoked if its capability is already activated, i.e. *open* or *available*, and the source node is *created*. It changes the local state of its requirement from *unbound* to *waiting*.

• *REQREADY* operation can be invoked if its capability is *available* and changes the local state of its requirement from *waiting* to *ready*.

Invocation Rule Operations of ConnectsTo Relationship Type:

- *CAPOPEN* operation can be invoked if the target node is already created. It changes the local state of its capability from *closed* to *open* and also issues an open message of the capability to the message pool.
- *CAPAVAILABLE* operation can be invoked if the target node is *started*. It changes the local state of its capability from *open* to *available* and also issues an available message of the capability to the message pool.
- *REQWAITING* operation can be invoked if it finds an open message of its capability and the source node is *created*. It changes the local state of its requirement from *unbound* to *waiting*.
- *REQREADY* operation can be invoked if it finds an available message of its capability and changes the local state of its requirement from *waiting* to *ready*.

7.2.1 Representation of the Example Behavior Model

Each of twelve rules explained in English above is more formally represented by a transition rule of CafeOBJ as follows:

```
module! STATERules {
  protecting(STATEfuns)
  -- Variables
  var TND : NDType
  vars IDND IDND1 IDND2 : NDID
  var IDCP : CPID
  var IDRQ : RQID
  var IDRL : RLID
  var SetND : SetOfNode
  var SetCP : SetOfCapability
  var SetRQ : SetOfRequirement
  var SetRL : SetOfRelationship
  var SCP : CPState
  var MP : PoolOfMsg
  -- CREATE Operation for Node Type
  ctrans [R01]:
     < (node(TND,IDND,initial) SetND), SetCP, SetRQ, SetRL, MP >
  => < (node(TND,IDND,created) SetND), SetCP, SetRQ, SetRL, MP >
  if allHostedOnRQOfNDInStates(SetRQ,IDND,ready) .
  -- START Operation for Node Type
  ctrans [R02]:
     < (node(TND,IDND,created) SetND), SetCP, SetRQ, SetRL, MP >
  => < (node(TND,IDND,started) SetND), SetCP, SetRQ, SetRL, MP >
  if allRQOfNDInStates(SetRQ,IDND,ready) .
```

-- CAPAVAILABLE Operation for HostedOn Relationship Type ctrans [R03]: < SetND, (cap(hostedOn, IDCP, closed, IDND) SetCP), SetRQ, SetRL, MP > => < SetND, (cap(hostedOn,IDCP,available,IDND) SetCP), SetRQ, SetRL, MP > if isCreated(state(getNode(SetND,IDND))) . -- REQREADY Operation for HostedOn Relationship Type trans [R04]: < SetND, (cap(hostedOn,IDCP,available,IDND1) SetCP), (req(hostedOn,IDRQ,unbound,IDND2) SetRQ), (rel(hostedOn,IDRL,IDCP,IDRQ) SetRL), MP > => < SetND, (cap(hostedOn,IDCP,available,IDND1) SetCP), (req(hostedOn, IDRQ, ready, IDND2) SetRQ), (rel(hostedOn,IDRL,IDCP,IDRQ) SetRL), MP > . -- CAPOPEN Operation for DependsOn Relationship Type ctrans [R05]: < SetND, (cap(dependsOn,IDCP,closed,IDND) SetCP), SetRQ, SetRL, MP > => < SetND, (cap(dependsOn, IDCP, open, IDND) SetCP), SetRQ, SetRL, MP > if isCreated(state(getNode(SetND,IDND))) . -- CAPAVAILABLE Operation for DependsOn Relationship Type ctrans [R06]: < SetND, (cap(dependsOn, IDCP, open, IDND) SetCP), SetRQ, SetRL, MP > => < SetND, (cap(dependsOn, IDCP, available, IDND) SetCP), SetRQ, SetRL, MP > if state(getNode(SetND,IDND)) = started . -- REQWAITING Operation for DependsOn Relationship Type ctrans [R07]: < SetND, (cap(dependsOn, IDCP, SCP, IDND1) SetCP), (req(dependsOn, IDRQ, unbound, IDND2) SetRQ), (rel(dependsOn,IDRL,IDCP,IDRQ) SetRL), MP > => < SetND, (cap(dependsOn, IDCP, SCP, IDND1) SetCP), (reg(dependsOn, IDRQ, waiting, IDND2) SetRQ), (rel(dependsOn,IDRL,IDCP,IDRQ) SetRL), MP > if state(getNode(SetND, IDND2)) = created and isActivated(SCP) . -- REQREADY Operation for DependsOn Relationship Type trans [R08]: < SetND, (cap(dependsOn, IDCP, available, IDND1) SetCP), (reg(dependsOn, IDRQ, waiting, IDND2) SetRQ), (rel(dependsOn,IDRL,IDCP,IDRQ) SetRL), MP > => < SetND, (cap(dependsOn, IDCP, available, IDND1) SetCP), (req(dependsOn,IDRQ,ready, IDND2) SetRQ), (rel(dependsOn,IDRL,IDCP,IDRQ) SetRL), MP > . -- CAPOPEN Operation for ConnectsTo Relationship Type ctrans [R09]: < SetND, (cap(connectsTo,IDCP,closed,IDND) SetCP),

```
SetRQ, SetRL, MP >
 => < SetND, (cap(connectsTo,IDCP,open, IDND) SetCP),
       SetRQ, SetRL, (opMsg(IDCP) MP) >
  if isCreated(state(getNode(SetND,IDND))) .
  -- CAPAVAILABLE Operation for ConnectsTo Relationship Type
 ctrans [R10]:
     < SetND, (cap(connectsTo,IDCP,open,
                                              IDND) SetCP),
       SetRQ, SetRL, MP >
 => < SetND, (cap(connectsTo,IDCP,available,IDND) SetCP),
       SetRQ, SetRL, (avMsg(IDCP) MP) >
 if state(getNode(SetND,IDND)) = started .
  -- REQWAITING Operation for ConnectsTo Relationship Type
 ctrans [R11]:
     < SetND, SetCP,
       (req(connectsTo,IDRQ,unbound,IDND) SetRQ),
       (rel(connectsTo,IDRL,IDCP,IDRQ) SetRL),
       (opMsg(IDCP) MP) >
 => < SetND, SetCP,
       (req(connectsTo,IDRQ,waiting,IDND) SetRQ),
       (rel(connectsTo,IDRL,IDCP,IDRQ) SetRL), MP >
 if state(getNode(SetND,IDND)) = created .
  -- REQREADY Operation for ConnectsTo Relationship Type
 trans [R12]:
     < SetND, SetCP,
       (req(connectsTo,IDRQ,waiting,IDND) SetRQ),
       (rel(connectsTo,IDRL,IDCP,IDRQ) SetRL),
       (avMsg(IDCP) MP) >
 => < SetND, SetCP,
       (req(connectsTo,IDRQ,ready, IDND) SetRQ),
       (rel(connectsTo,IDRL,IDCP,IDRQ) SetRL), MP > .
}
```

7.3 Verification of TOSCA Templates

This section presents the verification of the liveness property of setup operations of the TOSCA models consisting of four node types, three relationship types, and twelve transition rules. As described in Chapter 6, reachability of setup operations of cloud systems is formalized as (*init* leads-to *final*) and there are five sufficient conditions for it.

7.3.1 Definition of Predicates

```
Step 0-1: Define init and final.
```

The initial and final states of the TOSCA models are represented in CafeOBJ as follows:

```
module! STATEfuns {
    protecting(STATE)
```

```
-- Many operator definitions explained in Section 7.1.1
  . .
  var SetND : SetOfNode
 var SetCP : SetOfCapability
 var SetRQ : SetOfRequirement
 var SetRL : SetOfRelationship
 var MP : PoolOfMsg
 var S : State
 pred init : State
  eq init(< SetND,SetCP,SetRQ,SetRL,MP >)
     = not (SetND = empND) and (MP = empMsg) and
       wfs(< SetND,SetCP,SetRQ,SetRL,MP >) and
       noNDCycle(< SetND,SetCP,SetRQ,SetRL,MP >) and
       allNDInStates(SetND, initial) and
       allCPInStates(SetCP, closed) and
       allRQInStates(SetRQ,unbound) .
 pred final : State
  eq final(< SetND,SetCP,SetRQ,SetRL,MP >)
     = allNDInStates(SetND,started) .
 pred wfs : State
 eq wfs(S)
    = wfs-uniqND(S) and wfs-uniqCP(S) and
       wfs-uniqRQ(S) and wfs-uniqRL(S) and
       wfs-allCPHaveND(S) and wfs-allRQHaveND(S) and
       wfs-allCPHaveRL(S) and wfs-allRQHaveRL(S) and
       wfs-allRLHaveCP(S) and wfs-allRLHaveRQ(S) and
       wfs-allRLHaveSameTypeCPRQ(S) and
       wfs-allRLNotInSameND(S) and
       wfs-allRLHoldLocality(S) and
       wfs-allNDHaveAtMostOneHost(S) .
 pred wfs-uniqND : State
  eq wfs-uniqND(< SetND,SetCP,SetRQ,SetRL,MP >)
     = uniqND(SetND) .
. . .
-- Similar fourteen definitions of wfs-*.
. . .
}
```

As described in Section 5.3.3, we need to define operators DDSC and getAllObjInState in order to use the Cyclic Dependency Lemma in the verification. Section 5.3.3 also describes two techniques to prove the invariant property of noCycle(X, S). One is to design each transition rule to decrease dependencies between objects when it is applied. Section 6.5 shows example proofs using this technique.

Another technique used in this chapter is to design the system having a simpler constraint where some relationship between objects have no cyclic chains. Recalling Lemma 9, we can de-

fine DDSC to implement some simpler relationship r instead of the true DDS_C and use noCycleC defined by using r instead of the true $noCycle_c$. Module STATECyclefuns defines an example of such DDSC:

```
module! STATECyclefuns {
  protecting(UtilFuns)
  var ND : Node
  var SetND : SetOfNode
  var SetCP : SetOfCapability
  var SetRQ : SetOfRequirement
  var SetRL : SetOfRelationship
  var MP : PoolOfMsg
  op getAllNDInState : State -> SetOfNode
  eq getAllNDInState(< SetND,SetCP,SetRQ,SetRL,MP >) = SetND .
  op DDSC : Node State -> SetOfNode
  eq DDSC(ND, < SetND, SetCP, SetRQ, SetRL, MP >)
  eq DDSC(ND,< SetND,SetCP,SetRQ,SetRL,MP >)
    = getNDsOfCPs(SetND,
                  getCPsOfRLs(SetCP,
                               getRLsOfRQs(SetRL,
                                           getRQsOfND(SetRQ,ND)))) .
}
```

Since this DDSC firstly finds the corresponding requirements of the given node, then finds the corresponding capabilities of the requirements, and finally finds and returns the parents of the capabilities, the true DDS_C is obviously a subset of this DDSC. Moreover this DDSC does not refer local states of objects and twelve transition rules of the example behavior model never change links of objects. It means that DDSC(X,S) for any reachable global state S from an initial state S_0 is the same as DDS(X, S_0) and noCycleC defined by using DDSC is an invariant. noCycleC can be defined using template module CYCLEPRED as follows:

```
module! STATEfuns {
    protecting(STATE)
    ...
    -- Other definitions explained above.
    ...
    extending(CYCLEPRED(
        STATECyclefuns {sort Object -> Node,
            sort SetOfObject -> SetOfNode,
                op empObj -> empND,
                op getAllObjInState -> getAllNDInState})
        * {op noCycleC -> noNDCycle}
        )
}
```

Step 0-2: Define *cont*. Step 0-3: Define *m*.

```
module! ProofBase {
```

```
protecting(STATERules)
vars S SS : State
eq cont(S) = (S =(*,1)=>+ SS) .
```

Step 0-3: Define *m*.

```
var SetND : SetOfNode
   var SetCP : SetOfCapability
   var SetRQ : SetOfRequirement
   var SetRL : SetOfRelationship
   var MP : PoolOfMsq
   op m : State -> Nat
    eq m(< SetND,SetCP,SetRQ,SetRL,MP >)
       = (#NodeInStates(initial,SetND) * 2)
      + (#NodeInStates(created,SetND) * 1)
       + (#NodeInStates(started,SetND) * 0)
       + (#CapabilityInStates(closed,
                                        SetCP) * 2)
       + (#CapabilityInStates(open,
                                        SetCP) * 1)
       + (#CapabilityInStates(available,SetCP) * 0)
      + (#RequirementInStates(unbound,SetRQ) * 2)
       + (#RequirementInStates(waiting,SetRQ) * 1)
       + (#RequirementInStates(ready, SetRQ) * 0) .
Step 0-4: Define inv.
 var SetND : SetOfNode
 var SetCP : SetOfCapability
 var SetRQ : SetOfRequirement
 var SetRL : SetOfRelationship
```

```
var MP : PoolOfMsg
var S : State
```

```
pred inv-ifNDInitialThenRQUnboundReady : State
eq inv-ifNDInitialThenRQUnboundReady(< SetND,SetCP,SetRQ,SetRL,MP >)
   = ifNDInStatesThenRQInStates(SetND, initial, SetRQ, (unbound ready)) .
. . .
-- Many similar definitions of invariants.
-- 3 invariants are defined using predefined predicates.
-- 9 invariants are defined using problem specific predicates.
. . .
pred inv : State
-- wfs-*:
ceq inv(S) = false if not wfs-uniqND(S) .
-- Similar fourteen definitions for wfs-*.
. . .
-- inv-*:
ceq inv(S) = false if not inv-ifNDInitialThenRQUnboundReady(S) .
. . .
```

```
-- Similar eleven definitions for inv-*.
```

Step 0-5: Prepare for using the Cyclic Dependency Lemma.

For the CloudFormation example, the Cyclic Dependency Lemma is required to use for only one transition rule, R01. For the TOSCA example, however, there are two transition rules, R01 and R02 which cause cyclic situations in the verification. Thus, we need to define two lemmas in advance. One of them means that there is a contradiction when DDS_C of the specified initial resources. Another means that there is a contradiction when DDS_C of the specified created resource includes any created resources. They are defined as the following two conditional equations:

```
ceq [CycleR01 :nonexec]:
    true = false
    if someNDInStates(DDSC(node(T:NDType,I:NDID,initial),S:State),initial) .
ceq [CycleR02 :nonexec]:
    true = false
    if someNDInStates(DDSC(node(T:NDType,I:NDID,created),S:State),created) .
```

Step 0-6: Prepare proof constants.

}

```
ops idND idND' idND1 idND2 idND3 : -> NDIDLt
ops idCP idCP' idCP1 idCP2 idCP3 : -> CPIDLt
ops idRQ idRQ' idRQ1 idRQ2 idRQ3 : -> RQIDLt
ops idRL idRL' idRL1 idRL2 idRL3 : -> RLIDLt
ops sND sND' sND'' sND''' : -> SetOfNode
ops sCP sCP' sCP'' sCP''' : -> SetOfCapability
ops sRQ sRQ' sRQ'' sRQ''' : -> SetOfRequirement
ops sRL sRL' sRL'' sRL''' : -> SetOfRelationship
ops tnd tnd' tnd'' tnd''' : -> NDType
ops trl trl' trl'' : -> RLType
ops snd snd' snd'' : -> NDState
ops scp scp' scp'' : -> CPState
ops srq srq' srq'' : -> RQState
op stND : -> SetOfNDState
op stCP : -> SetOfCPState
op stRQ : -> SetOfRQState
ops mp mp' : -> PoolOfMsg
op msg : -> Msg
```

7.3.2 Lemmas for Using Cyclic Dependency Lemma

As described in Section 6.6, it is wise to define lemmas for using the Cyclic Dependency Lemma and use them in the similar cases. For this TOSCA example, two similar lemmas are required. One lemma claims that if there is an initial node in a reachable global state then there exists a transition rule applicable to the global state. Here we refer to it as the *initial-cont* lemma. It

can be proved as follows:

Step 1-0: Define a predicate to be proved.

Module ProofInitialCont defines the predicate as invcont. Note that we can only consider the case where inv(S) holds because S is a reachable global state.

```
module! ProofInitialCont {
  protecting(ProofBase)
  vars B1 B2 : Bool
  pred (_when _) : Bool Bool { prec: 64 r-assoc }
  eq (B1 when B2)
      = B2 implies B1 .
  var S: State
  pred invcont : State
  eq invcont(S)
      = cont(S) = true
     when inv(S) .
}
```

Step 1-1: Begin with the most general case.

```
select ProofInitialCont .
:goal {
   eq invcont(< (node(tnd, idND, initial) sND), sCP, sRQ, sRL, mp >)
        = true .
}
```

Step 1-2: Consider which rule can be applied to the global state in the current case. The applicable rule may be R01 because the global state includes an initial node.

Step 1-3: Split the current case into cases which collectively cover the current case and one of which matches to LHS of the current rule.

The global state already matches to LHS of R01.

Step 1-4: Split the current case into cases where the condition of the current rule does or does not hold.

```
:csp {
    eq allHostedOnRQOfNDInStates(sRQ,idND,ready) = true .
    eq sRQ = (req(hostedOn,idRQ,unbound,idND) sRQ') .
    eq sRQ = (req(hostedOn,idRQ,waiting,idND) sRQ') .
}
-- Case 1: When all of the hostedOn requirements are ready:
:apply (rd) -- 1
-- Case 2: When there is an unbound hostedOn requirement of the node:
... -- More consideration needed.
-- Case 3: When there is a waiting hostedOn requirement of the node:
:apply (rd) -- 3
```

Only Case 2 remains unproved and it then becomes the current case.

Step 1-2: Consider which rule can be applied to the global state in the current case. The applicable rule may be R04 because the global state in Case 2 includes an unbound hostedOn requirement.

Step 1-5: When there is a dangling link, split the case into cases where the linked object does or does not exist.

```
-- Case 2: When there is an unbound hostedOn requirement of the node:
:csp {
 eq onlyOneRLOfRQ(sRL,idRQ) = false .
 eq sRL = (rel(hostedOn,idRL,idCP,idRQ) sRL') .
}
-- Case 2-1: When the relationship of requirement idRQ does not exist:
:apply (rd) -- 2-1
-- Case 2-2: When the relationship of requirement idRQ exists:
:csp {
 eq existCP(sCP,idCP) = false .
 eq sCP = (cap(hostedOn,idCP,scp,idND') sCP') .
}
-- Case 2-2-1: When the capability of the relationship does not exist:
:apply (rd) -- 2-2-1
-- Case 2-2-2: When the capability of the relationship exists:
:ctf {
 eq idND' = idND .
}
-- Case 2-2-2-1: When the node of capability idCP is
                                the same of requiement idRQ:
:apply (rd) -- 2-2-2-1
-- Case 2-2-2-2: When the node of capability idCP is not
                                the same of requiement idRQ:
... -- More consideration needed.
```

Only Case 2-2-2-2 remains unproved.

Step 1-3: Split the current case into cases which collectively cover the current case and one of which matches to LHS of the current rule.

```
-- Case 2-2-2-2: When the node of capability idCP is not
-- the same of requiement idRQ:
:csp {
  eq scp = closed .
  eq scp = open .
  eq scp = available .
}
-- Case 2-2-2-2-1: When the capability of idCP is closed:
... -- More consideration needed.
-- Case 2-2-2-2-2: When the capability of idCP is open:
:apply (rd) -- 2-2-2-2
-- Case 2-2-2-2: When the capability of idCP is avialable:
```

:apply (rd) -- 2-2-2-3

Only Case 2-2-2-1 remains unproved.

Step 1-2: Consider which rule can be applied to the global state in the current case. The applicable rule may be R03 because the global state in Case 2-2-2-1 includes an unbound hostedOn requirement.

Step 1-5: When there is a dangling link, split the case into cases where the linked object does or does not exist.

```
-- Case 2-2-2-2-1: When the capability of idCP is closed:
:csp {
  eq existND(sND,idND') = false .
  eq sND = (node(tnd',idND',snd') sND') .
}
-- Case 2-2-2-2-1-1: When the node of the capability of idCP does not exist:
:apply (rd) -- 2-2-2-2-1-1
-- Case 2-2-2-2-1-2: When the node of the capability of idCP exists:
... -- More consideration needed.
```

Only Case 2-2-2-1-2 remains unproved.

Step 1-4: Split the current case into cases where the condition of the current rule does or does not hold.

```
-- Case 2-2-2-1-1: When the node of the capability of idCP does not exist:
:csp {
  eq snd' = initial .
  eq snd' = created .
  eq snd' = started .
}
-- Case 2-2-2-2-1-2-1: When the node of idND' is initial:
... -- More consideration needed.
-- Case 2-2-2-2-1-2-2: When the node of idND' is created:
:apply (rd) -- 2-2-2-2-1-2-2
-- Case 2-2-2-2-1-2-3: When the node of idND' is started:
:apply (rd) -- 2-2-2-2-1-2-3
```

Only Case 2-2-2-1-2-1 remains unproved.

Step 1-6: When falling in a cyclic situation, use the Cyclic Dependency Lemma.

```
-- Case 2-2-2-2-1-2-1: When the node of idND' is initial:
:init [CycleR01] by {
   T:NDType <- tnd;
   I:NDID <- idND;
   S:State <- < (node(tnd,idND,initial) sND), sCP, sRQ, sRL, mp >;
}
:apply (rd) -- 2-2-2-1-2-1
```

Thus, all of the cases are successfully proved and we can assume that cont(S) holds for any reachable global state *S* which include an initial node.

Another similar lemma claims that if there is a **created** node in a global state then there exists a transition rule applicable to the global state. Here we refer to it as the *created-cont* lemma. It can be proved as follows:

Step 1-0: Define a predicate to be proved.

Module ProofCreatedCont imports predicate invcont from module ProofInitialCont and additionally introduces the initial-cont lemma proved just above because the proof of this lemma uses it. Note that the when clause is omitted from the initial-cont lemma because inv(S) holds for any reachable global state S.

Step 1-1: Begin with the most general case.

```
select ProofCreatedCont .
:goal {
   eq invcont(< (node(tnd, idND, created) sND), sCP, sRQ, sRL, mp >)
        = true .
}
```

Step 1-2: Consider which rule can be applied to the global state in the current case. The applicable rule may be R02 because the global state includes a created node.

Step 1-3: Split the current case into cases which collectively cover the current case and one of which matches to LHS of the current rule.

The global state already matches to LHS of RO2.

Step 1-4: Split the current case into cases where the condition of the current rule does or does not hold.

```
:csp {
    eq allRQOfNDInStates(sRQ,idND,ready) = true .
    eq sRQ = (req(trl,idRQ,unbound,idND) sRQ') .
    eq sRQ = (req(trl,idRQ,waiting,idND) sRQ') .
}
-- Case 1: When all of the requirements are ready:
```

```
:apply (rd) -- 1
-- Case 2: When there is an unbound requirement of node idND:
... -- More consideration needed.
-- Case 3: When there is a waiting requirement of node idND:
... -- More consideration needed.
```

Both Case 2 and 3 remain unproved. Let Case 2 be the current state.

Step 1-2: Consider which rule can be applied to the global state in the current case. The applicable rule may be R04, R07, or R11 because the global state in Case 2 includes an unbound requirement and the applicable rule depends on its type.

Step 1-3: Split the current case into cases which collectively cover the current case and one of which matches to LHS of the current rule.

```
-- Case 2: When there is an unbound requirement of node idND:
:csp {
  eq trl = hostedOn .
  eq trl = dependsOn .
  eq trl = connectsTo .
}
-- Case 2-1: When the type of requirement idRQ is hostedOn:
:apply (rd) -- 2-1
-- Case 2-2: When the type of requirement idRQ is dependsOn:
... -- More consideration needed.
-- Case 2-3: When the type of requirement idRQ is connectsTo:
... -- More consideration needed.
```

Case 2-1 is not a reachable global state because a node never becomes **created** when one of its **hostedOn** requirement is **unbound**, which makes **inv(S)** reduce to false. Thus, Case 2-2 and 2-3 remains unproved. Let Case 2-2 be the current case.

Step 1-5: When there is a dangling link, split the case into cases where the linked object does or does not exist.

```
-- Case 2-2: When the type of requirement idRQ is dependsOn:
:csp {
  eq onlyOneRLOfRQ(sRL,idRQ) = false .
  eq sRL = (rel(dependsOn,idRL,idCP,idRQ) sRL') .
}
-- Case 2-2-1: When the relationship of requirement idRQ does not exist:
:apply (rd) -- 2-2-1
-- Case 2-2-2: When the relationship of requirement idRQ exists:
:csp {
  eq existCP(sCP,idCP) = false .
  eq sCP = (cap(dependsOn,idCP,scp,idND') sCP') .
}
-- Case 2-2-2-1: When the capability of the relationship does not exist:
:apply (rd) -- 2-2-1
-- Case 2-2-2-2: When the capability of the relationship exists:
```

```
:ctf {
    eq idND' = idND .
}
-- Case 2-2-2-2-1: When the node of capability idCP is
-- the same of requiement idRQ:
:apply (rd) -- 2-2-2-2-1
-- Case 2-2-2-2-2: When the node of capability idCP is not
-- the same of requiement idRQ:
... -- More consideration needed.
```

Step 1-3: Split the current case into cases which collectively cover the current case and one of which matches to LHS of the current rule.

```
-- Case 2-2-2-2-2: When the node of capability idCP is not
-- the same of requiement idRQ:
:csp {
  eq scp = closed .
  eq scp = open .
  eq scp = available .
}
-- Case 2-2-2-2-2-1: When capability idCP is closed:
... -- More consideration needed.
-- Case 2-2-2-2-2-2: When capability idCP is open:
:apply (rd) -- 2-2-2-2-2
-- Case 2-2-2-2-3: When capability idCP is available:
:apply (rd) -- 2-2-2-2-3
```

Case 2-2-2-2-2 and 2-2-2-2-2 are proved because R07 is applicable. Thus, only Case 2-2-2-2-1 remains unproved.

Step 1-2: Consider which rule can be applied to the global state in the current case. The applicable rule may be R05 because the global state in Case 2-2-2-2-1 includes an closed dependsOn capability.

Step 1-5: When there is a dangling link, split the case into cases where the linked object does or does not exist.

```
-- Case 2-2-2-2-1: When capability idCP is closed:
:csp {
  eq existND(sND,idND') = false .
  eq sND = (node(tnd',idND',snd') sND') .
}
-- Case 2-2-2-2-2-1-1: When the node of capability idCP does not exist:
:apply (rd) -- 2-2-2-2-1-1
-- Case 2-2-2-2-2-1-2: When the node of capability idCP exists:
... -- More consideration needed.
```

```
Case 2-2-2-2-1-2 remains unproved.
```

Step 1-4: Split the current case into cases where the condition of the current rule does or does not hold.

```
-- Case 2-2-2-2-2-1-2: When the node of capability idCP exists:
:csp {
    eq snd' = initial .
    eq snd' = created .
    eq snd' = started .
}
-- Case 2-2-2-2-2-1-2-1: When node idND' is initial:
:apply (rd) -- 2-2-2-2-1-2-1
-- Case 2-2-2-2-2-1-2-2: When node idND' is created:
:apply (rd) -- 2-2-2-2-1-2-2
-- Case 2-2-2-2-1-2-3: When node idND' is started:
:apply (rd) -- 2-2-2-2-1-2-3
```

Note that Case 2-2-2-2-1-2-1 is proved by the initial-cont lemma, Case 2-2-2-2-1-2-2 and 2-2-2-2-1-2-3 are proved because R05 is applicable. Thus, Case 2-2 is proved and Case 2-3 reminds unprove. Case 2-3 is split into totally 21 cases all of which are proved similarly as split cases of Case 2-2.

Similarly Case 3 is split into totally 33 cases two of which require to use the Cyclic Dependency Lemma for rule R02. One of them is the following Case 3-2-2-2-2-2-2:

```
-- Case 3: When there is a waiting requirement of node idND:
. . .
-- Case splitting proceeds similarly as Case 2.
. . .
-- Case 3-2-2-2-2-2-2: When the node of idND' is created:
-- The global state in this case is
-- < (node(tnd,idND,created) node(tnd',idND',created) sND'),</pre>
     (cap(dependsOn,idCP,open,idND') sCP'),
_ _
     (req(dependsOn,idRQ,waiting,idND) sRQ'),
_ _
     (rel(dependsOn,idRL,idCP,idRQ) sRL'),
___
___
    mp >
:init [CycleR02] by {
 T:NDType <- tnd;
 I:NDID <- idND;
 S:State <- < (node(tnd,idND,created) sND), sCP, sRQ, sRL, mp >;
}
:apply (rd) -- 3-2-2-2-2-2-2
. . .
```

In this case, node idND is created and directly depends on node idND' which is also created. The Cyclic Dependency Lemma claims this global state is not reachable and this case is proved.

Another case is very similar to one above; the relationship type is not dependsOn but connectsTo as follows:

```
-- Case 3-3-2-1-2-2-2-2: When the node of idND' is created:
-- The global state in this case is
-- < (node(tnd, idND, created) node(tnd', idND', created) sND'),
-- (cap(connectsTo, idCP, open, idND') sCP'),
-- (req(connectsTo, idRQ, waiting, idND) sRQ'),
-- (rel(connectsTo, idRL, idCP, idRQ) sRL'),
-- mp >
```

```
:init [CycleR02] by {
   T:NDType <- tnd;
   I:NDID <- idND;
   S:State <- < (node(tnd,idND,created) sND), sCP, sRQ, sRL, mp >;
}
:apply (rd) -- 3-3-2-1-2-2-2-2.
...
```

All other cases are successfully proved and we can assume that cont(S) holds for any reachable global state S which include a created node.

7.3.3 Proof of Sufficient Condition (1)

Step 1-0: Define a predicate to be proved. The proof of condition (1) requires to use the initial-cont lemma:

```
module! ProofInitCont {
  protecting(ProofBase)
  var S : State
  var T : NDType
  var I : NDID
  var SetND : SetOfNode
  var SetCP : SetOfCapability
  var SetRQ : SetOfRequirement
  var SetRL : SetOfRelationship
  var M : PoolOfMsg
  -- Predicate to be proved.
  pred initcont : State .
  eq initcont(S) = init(S) implies cont(S) .
  -- initial-cont lemma:
  eq cont(< (node(T, I, initial) SetND),</pre>
             SetCP, SetRQ, SetRL, M >) = true .
}
```

Step 1-1: Begin with the most general case.

select ProofInitCont .
:goal {eq initcont(< sND, sCP, sRQ, sRL, mp >) = true .}

Step 1-2: Consider which rule can be applied to the global state in the current case. The first rule is R01.

Step 1-3: Split the current case into cases which collectively cover the current case and one of which matches to LHS of the current rule.

Since LHS of rule R01 requires the global state to have at least one initial node, the case is split into four more cases, i.e. no node, at least one initial, created, or started node.

```
:csp {
    eq sND = empND .
```

```
eq sND = (node(tnd,idND,snd) sND') .
}
-- Case 1: When there is no node:
:apply (rd) -- 1
-- Case 2: When there is a node:
-- The state of the node is initial, created, or started.
:csp {
    eq snd = initial .
    eq snd = created .
    eq snd = started .
}
:apply (rd) -- 2-1
:apply (rd) -- 2-2
:apply (rd) -- 2-3
```

Case 2-1 is proved by the initial-cont lemma. In other cases, init(S) does not hold for the global state S. Thus, sufficient condition (1) is proved.

7.3.4 **Proof of Sufficient Condition (2)**

Step 2-0: Define a predicate to be proved.

The proof of condition (2) requires to use both of the initial-cont lemma and the created-cont lemma:

```
module! ProofContCont {
  protecting(ProofBase)
  vars S SS : State
  var CC : Bool
  var T : NDType
  var I : NDID
  var SetND : SetOfNode
  var SetCP : SetOfCapability
  var SetRQ : SetOfRequirement
  var SetRL : SetOfRelationship
  var M : PoolOfMsg
  -- Predicate to be proved.
  pred ccont : State State
  pred contcont : State
  eq ccont(S,SS)
     = inv(S) and not final(S) implies cont(SS) or final(SS) .
  eq contcont(S)
     = not (S =(*,1)=>+ SS if CC suchThat
            not ((CC implies ccont(S,SS)) == true)
         { true }) .
  -- initial-cont lemma:
  eq cont(< (node(T, I, initial) SetND),</pre>
     SetCP, SetRQ, SetRL, M >)
     = true .
```

```
-- created-cont lemma:
eq cont(< (node(T, I, created) SetND),
        SetCP, SetRQ, SetRL, M >)
        = true .
}
```

Step 2-1: Begin with the cases each of which matches to LHS of each rule. The followings are cases for twelve transition rules:

```
select ProofContCont .
-- Goal of Condition (2) for rule R01
:goal {
 eq contcont(< (node(tnd,idND,initial) sND), sCP, sRQ, sRL, mp >)
     = true .
}
-- Goal of Condition (2) for rule R02
:goal {
 eq contcont(< (node(tnd,idND,created) sND), sCP, sRQ, sRL, mp >)
     = true .
}
-- Goal of Condition (2) for rule R03
:goal {
 eq contcont(< sND, (cap(hostedOn,idCP,closed,idND) sCP), sRQ, sRL, mp >)
     = true .
}
-- Goal of Condition (2) for rule R04
:goal {
 eq contcont(< sND,</pre>
                (cap(hostedOn,idCP,available,idND) sCP),
                (req(hostedOn,idRQ,unbound,idND')
                                                    sRQ),
                (rel(hostedOn,idRL,idCP,idRQ)
                                                    sRL), mp >)
     = true .
}
-- Goal of Condition (2) for rule R05
:goal {
 eq contcont(< sND, (cap(dependsOn,idCP,closed,idND) sCP), sRQ, sRL, mp >)
     = true .
}
-- Goal of Condition (2) for rule R06
:goal {
 eq contcont(< sND, (cap(dependsOn,idCP,open,idND) sCP), sRQ, sRL, mp >)
     = true .
}
-- Goal of Condition (2) for rule R07
:goal {
```

```
eq contcont(< sND,</pre>
                 (cap(dependsOn,idCP,scp,idND)
                                                      sCP),
                 (req(dependsOn,idRQ,unbound,idND') sRQ),
                 (rel(dependsOn,idRL,idCP,idRQ)
                                                      sRL), mp >)
     = true .
}
-- Goal of Condition (2) for rule R08
:goal {
  eq contcont(< sND,</pre>
                 (cap(dependsOn,idCP,available,idND) sCP),
                 (req(dependsOn,idRQ,waiting,idND')
                                                      sRQ),
                 (rel(dependsOn,idRL,idCP,idRQ)
                                                       sRL), mp >)
     = true .
}
-- Goal of Condition (2) for rule R09
:goal {
  eq contcont(< sND, (cap(connectsTo,idCP,closed,idND) sCP), sRQ, sRL, mp >)
     = true .
}
-- Goal of Condition (2) for rule R10
:goal {
  eq contcont(< sND, (cap(connectsTo,idCP,open,idND) sCP), sRQ, sRL, mp >)
     = true .
}
-- Goal of Condition (2) for rule R11
:goal {
  eq contcont(< sND, sCP,</pre>
                 (req(connectsTo,idRQ,unbound,idND) sRQ),
                 (rel(connectsTo,idRL,idCP,idRQ)
                                                      sRL),
                 (opMsg(idCP) mp) >)
     = true .
}
-- Goal of Condition (2) for rule R12
:goal {
  eq contcont(< sND, sCP,</pre>
                 (req(connectsTo,idRQ,waiting,idND) sRQ),
                 (rel(connectsTo,idRL,idCP,idRQ)
                                                      sRL),
                 (avMsg(idCP) mp) >)
     = true .
}
```

The rest of this section describes the proof of condition (2) for rule R06 as an example.

```
select ProofContCont .
-- Goal of Condition (2) for rule R06
:goal {
```

Step 2-7: When there is a dangling link, split the current case into cases where the linked object does or does not exist.

```
:csp {
    eq existND(sND,idND) = false .
    eq sND = (node(tnd,idND,snd) sND') .
}
-- Case 1: The node of capability idCP does not exist:
:apply (rd) -- 1
-- Case 2: The node of capability idCP exists:
```

Step 2-2: Split the current case for a rule into cases where the condition of the rule does or does not hold.

```
:csp {
   eq snd = initial .
   eq snd = created .
   eq snd = started .
}
-- Case 2-1: The node is initial:
:apply (rd) -- 2-1
-- Case 2-2: The node is created:
:apply (rd) -- 2-2
-- Case 2-3: The node is started:
```

Note that Case 2-1 and 2-2 are proved by the initial-cont lemma and the created-cont lemma respectively.

Step 2-3: Split the current case into cases where predicate *final* does or does not hold in the next state.

We know that *final* never holds in the next state of this case.

Step 2-4: Consider which rule can be applied to the next state. Since the next state in Case 2-3 includes an available dependsOn capability with identifier idCP, rule R08 can be applied to it.

Step 2-7: When there is a dangling link, split the current case into cases where the linked object does or does not exist.

```
:csp {
  eq onlyOneRLOfCP(sRL,idCP) = false .
  eq sRL = (rel(trl,idRL,idCP,idRQ) sRL') .
}
-- Case 2-3-1: There is not a corresponding relationship:
:apply (rd) -- 2-3-1
-- Case 2-3-2: There is a corresponding relationship:
```

Step 2-5: Split the current case into cases which collectively cover the current case and the next state of one of the split cases matches to LHS of the current rule.

LHS of rule R08 requires the type of the corresponding relationship to be dependsOn.

```
:csp {
  eq trl = hostedOn .
  eq trl = dependsOn .
  eq trl = connectsTo .
}
-- Case 2-3-2-1: The relationship is hostedOn:
:apply (rd) -- 2-3-2-1
-- Case 2-3-2-2: The relationship is dependsOn:
... -- More consideration needed.
-- Case 2-3-2-3: The relationship is connectsTo:
:apply (rd) -- 2-3-2-3
```

Only Case 2-3-2-2 remains unproved.

Step 2-7: When there is a dangling link, split the current case into cases where the linked object does or does not exist.

```
-- Case 2-3-2-2: The relationship is dependsOn:
:csp {
  eq existRQ(sRQ,idRQ) = false .
  eq sRQ = (req(trl',idRQ,srq,idND') sRQ') .
}
-- Case 2-3-2-2-1: There is not a corresponding requirement:
:apply (rd) -- 2-3-2-2-1
-- Case 2-3-2-2-2: There is a corresponding requirement:
... -- More consideration needed.
```

Only Case 2-3-2-2 remains unproved.

Step 2-5: Split the current case into cases which collectively cover the current case and the next state of one of the split cases matches to LHS of the current rule.

LHS of rule R08 requires the type of the corresponding requirement to be dependsOn and the local state of it to be waiting.

```
-- Case 2-3-2-2-2: There is a corresponding requirement:
:csp {
  eq trl' = hostedOn .
  eq trl' = dependsOn .
  eq trl' = connectsTo .
}
-- Case 2-3-2-2-2-1: The requirement is hostedOn:
:apply (rd) -- 2-3-2-2-2-1
-- Case 2-3-2-2-2-2: The requirement is dependsOn:
:csp {
  eq srq = unbound .
  eq srq = waiting .
  eq srq = ready .
}
```

```
-- Case 2-3-2-2-2-1: The requirement is unbound:
... -- More consideration needed.
-- Case 2-3-2-2-2-2: The requirement is waiting:
:apply (rd) -- 2-3-2-2-2-2
-- Case 2-3-2-2-2-3: The requirement is ready:
:apply (rd) -- 2-3-2-2-2-3
-- Case 2-3-2-2-2-3: The requirement is connectsTo:
:apply (rd) -- 2-3-2-2-2-3
```

Only Case 2-3-2-2-2-1 remains unproved.

Step 2-4: Consider which rule can be applied to the next state. Since the next state in Case 2-3-2-2-2-1 includes an unbound dependsOn requirement with identifier idRQ, rule R07 can be applied to it.

Step 2-7: When there is a dangling link, split the current case into cases where the linked object does or does not exist.

```
-- Case 2-3-2-2-2-1: The requirement is unbound:
:csp {
  eq existND(sND',idND') = false .
  eq sND' = (node(tnd',idND',snd') sND'') .
}
-- Case 2-3-2-2-2-2-1-1: The node of requirement idRQ does not exist:
:apply (rd) -- 2-3-2-2-2-1-1
-- Case 2-3-2-2-2-2-1-2: The node of requirement idRQ exists:
... -- More consideration needed.
```

Only Case 2-3-2-2-2-1-2 remains unproved.

Step 2-5: Split the current case into cases which collectively cover the current case and the next state of one of the split cases matches to LHS of the current rule. The global state already matches to LHS of R07.

Step 2-6: Split the current case into cases where the condition of the current rule does or does not hold in the next state.

```
-- Case 2-3-2-2-2-1-2: The node of requirement idRQ exists:
:csp {
    eq snd' = initial .
    eq snd' = created .
    eq snd' = started .
}
-- Case 2-3-2-2-2-2-1-2-1: The node is initial:
:apply (rd) -- 2-3-2-2-2-1-2-1
-- Case 2-3-2-2-2-1-2-2: The node is created:
:apply (rd) -- 2-3-2-2-2-1-2-2
-- Case 2-3-2-2-2-1-2-3: The node is started:
:apply (rd) -- 2-3-2-2-2-1-2-3
```

All of the cases are successfully proved.

7.3.5 **Proof of Sufficient Condition (3)**

Step 3-0: Use natural number axioms.

The framework provides a module, NATAXIOM, which defines several natural number axioms to be used for proof of condition (3). Module ProofMeasure should protecting import NATAXIOM as well as ProofBase:

```
module! ProofMeasure {
    protecting(ProofBase)
    protecting(NATAXIOM)
```

Step 3-1: Define a predicate to be proved.

Step 3-2: Begin with the cases each of which matches to LHS of each rule. Here we show the proof of condition (3) for rule R06 as an example:

```
-- Goal of Condition (3) for rule R06
select ProofMeasure .
:goal {
   eq mesmes(< sND, (cap(dependsOn,idCP,open,idND) sCP), sRQ, sRL, mp >)
        = true .
}
```

Step 3-3: Split the current case for a rule into cases where the condition of the rule does or does not hold.

```
:ctf {
    eq state(getNode(sND,idND)) = started .
}
:apply (rd) -- 1
:apply (rd) -- 2
```

Condition (3) for other rules can be similarly proved.

7.4 Evaluation

Table 7.1 shows the number of proved goals and split cases to verify the liveness property of setup operations of the TOSCA models consisting of four node types, three relationship types,

and twelve transition rules. Condition (1) requires only one goal and 6 cases whereas (2) and (3) require 12 goals each of which is for each of 12 transition rules. Condition (4) also requires 12 goals for each of 12 invariants and (5) requires 144 goals for each combination of 12 invariants and 12 rules. We need 25 problem specific lemmas each of which requires one goal. The verification consists of totally 206 goals which are split into 918 cases.

Table 7.1: Number of goals and cases				
targets	goals	(1 goal for each of ?)	cases	
Condition (1)	1	(condition)	6	
Condition (2)	12	(12 rules)	115	
Condition (3)	12	(12 rules)	30	
Condition (4)	12	(12 invariants)	18	
Condition (5)	144	$(12 \text{ rules} \times 12 \text{ invariants})$	443	
Lemmas	25	(25 lemmas)	306	
Total	206		918	

Rate of Reuse

Table 7.2 shows the reuse rate of entities provided by the framework.

Table 7.2: Reuse rate of entities provided by the framework

entities	total	reused	defined	reuse rate
Sorts	37	37	0	100%
Operators	218	142	76	65%
Lemmas	38	13	25	34%

We need 37 sorts to represent the TOSCA structure models and all of them can be just instantiated and renamed from predefined sorts provided by the framework.

We also need totally 218 predicates/operators not including definitions of proof constants. 104 of them can be just instantiated and renamed form predefined operators. 11 predicates, such as initcont, contcont, and so on, are the same as in proofs of the CloudFormation example and so can be copied from them. 27 state predicates are simple wrappers of other predicates, such as wfs-* and inv-*.

Thereby, 76 operators are problem specific ones. 23 of them are constructors including local state and type literals. 15 operators are selectors such as id, type, state, and ones for links. The framework requires users to define 8 operators, i.e. init, final, wfs, inv, m, invK, getAllNDInState, and DDSC.

Remaining 30 operators are truly problem specific, however almost all of them can be easily defined combining predefined operators and can be written in only several code lines. As described in Section 7.1.1, there are three kinds of them:

• Check the consistency between messages and local states of objects, e.g. if there is an available message then the corresponding capability should be available. Currently, the framework provides no functionality to support messaging mechanisms.

- Check the consistency between capabilities and requirements connected by relationships. The framework provides many operators and lemmas for links but does not provide those for chains of links.
- Check other problem-specific constraints, e.g. every node should be hosted on exactly one VM node.

The proofs of the TOSCA example need 38 lemmas, 13 of which are already proved by the framework in a general level of abstraction. Reminding 25 lemmas are required to prove condition (4) and (5) for invariants about three kinds of problem specific operators described above.

Size of Codes

Table 7.3 shows the number of lines of codes we write to very the leads-to property. The "potential" column shows the potential number of lines if we write proofs not using the framework.

Table 7.3: Lines of Codes						
	written	potential	reduce rate			
Model	598	1784	66%			
Structure	527	1713	69%			
Behavior	71	71	0%			
Proofs	3991	4516	12%			

The representation of the TOSCA model in CafeOBJ consists of about 600 lines of codes not including comment lines. About 530 lines of codes represent the structure model and 70 lines represent twelve rules. We estimate that the size of the structure model representation is 30% compared to when we would code it without using the framework, whereas the size of the behavior model (transition rules) is the same.

The size of codes for proofs is essentially the same as when not using the framework because reusable codes for proofs are 13 proved lemmas provided by the framework.

Consistent Structure of Proof

In addition to promoting reuse of abstract entities and lemmas, time and efforts to develop proofs is radically reduced. Of course, it is mainly because this is our second experience of the same problem, whereas the previous proof scores did not have any unified policies of splitting and so were very difficult to understand even for us. The framework makes the new proof scores become much clear, especially those of conditions (2)(3)(5) which should be proved for each of twelve trans rules.

The recommended module structure also helps to make proof scores easier to understand. We can instantly find the place where something is defined and can instantly imagine which parts of the proof may be affected when something is modified.

Similarly as application frameworks of software development, our framework not only provides reusable entities to reduce the size of codes of proof but also assists users how to design the models and how to systematically think and develop proofs, which brings high productivity by minimizing development efforts and high maintainability by consistent structure of models and proofs.

Chapter 8

Related Work and Conclusion

8.1 Related Work

Reuse of Abstract Proofs

There are very few existing researches on reuse of proofs. Abrial, J. and Hallerstede, S. [1] proposed the generic instantiation approach for reuse of Event-B development. The idea of the generic instantiation is that it is a sufficient condition to prove instantiated axioms in order to reuse proofs of a generic machine and its refined machines. In more detail, let M and C be a generic machine and a context respectively where M sees C. Let s, c, and P(s, c) be collections of sets, constants, and axioms defined by C respectively. Similarly, let N and D be a concrete machine and a context where N sees D. Let t, d, and Q(t, d) be collections of sets, constants, and axioms defined by D respectively. Let M' be a machine instantiated from M where s and c are renamed as S(t, d) and C(t, d). Suppose that M' refines N and sees D. Then, proving $Q(t, d) \rightarrow P(S(t, d), C(t, d))$ is a sufficient condition in order to reuse invariants and theorems of M and also of its refined machines without reproving them.

Silva, R. and Butler, M. J. [29] proposed to use theorem proving to ensure the sufficient condition. Using the functionality to rename elements (Refactory plug-in) and compose machines (Shared Event Composition plug-in) of the Rodin platform, they defined a way of instantiating generic machines and generating the sufficient condition as a theorem of the concrete machine whose proof obligation will be ensured by Rodin's theorem prover.

Tikhonova, U., et al. [32] applied this idea to verify LACE DSL programs for controlling lithography machines. They implemented transformation from LACE programs to Event-B specifications which are composed by instantiated machines from general ones, however, the generated theorems are too large for the automatic provers of Rodin to discharge. They say that they do not expect their average user to prove these theorems using interactive provers, as it requires knowledge of propositional calculus and understanding of proof strategies. Instead of theorem proving, they employed evaluation of structural properties predicates in the animation plug-in of Rodin.

Although reusing abstract entities by renaming and composing is a similar approach to our framework, Silva, R. and Butler, M. J. did not provide any actually reusable entities whereas our framework provides general templates, libraries, lemmas, and a procedure reusable in a specific domain. Tikhonova, U., et al. applied the idea to the domain of the lithography machine control, however, they did not reuse generally proved properties to prove the instantiated specifications.

Formal Approach for Cloud Orchestration

Salaün, G., et al. [9, 27, 28] designed a system setup protocol and demonstrated to verify a liveness property of the protocol using their model checking method. Although their setup protocol is essentially the same as the behavior model of our TOSCA example in this dissertation, there are four main differences.

Firstly, they proved one specific protocol whereas this dissertation proposes a general way to specify, represent, and verify behavior of cloud orchestration and also shows that it can be effectively applied to a model of standard specification language as a non-trivial case study.

Secondly, their protocol is based on a specific implementation which challenges distributed management of cloud resources while current popular implementations, e.g. CloudFormation, use centralized management. On the other hand, our model is rather abstract without assuming distributed or centralized implementations.

Thirdly, they used model checking while we use theorem proving. They checked about 150 different models of system including from four to fifteen components in which from 1.4 thousand to 1.4 million transitions are generated and checked. They found a bug of their specification because checked models fortunately included error cases. The model checking method can verify correctness of checked models and so they should include all of the boundary cases. In our formalization, the specification itself is verified by interactive theorem proving in which all of the boundary cases are necessary in consideration in a systematic way. It achieves structural and deep understanding that is required to develop trusted systems.

Finally, they called a function to check the acyclicness of resource dependency whenever a transition occurs whereas our framework provides formalization, a template module, and lemmas to prove the invariant property of the acyclicness.

Dependency Management between Internal Resources

CloudFormation and OpenStack Heat can manage resources on the IaaS layer, however, they support to manage dependencies between resources in VMs. For example, suppose a software component (SC₁) on a VM (VM₁) can be activated only after waiting for activation of another component (SC₂) on another VM (VM₂), CloudFormation requires a pair of special purpose resources, namely, WaitCondition and WaitConditionHandle. VM1 should be declared to depend on the WaitCondition resource. The corresponding WaitConditionHandle resource provides a URL that should be passed to the script for initializing VM₂. When SC₂ is successfully activated, the script sends a success signal to the URL, which causes the WaitCondition become active and then creation of dependent VM₁ starts. This style of management includes several problems. Firstly, it forces complicated and troublesome coding of operations. Secondly, although only SC₁ should wait for SC₂, all the other components on VM₁ are also forced to wait. This causes unnecessary slowdown of system creation. Thirdly, it tends to make cyclic dependencies. Suppose SC₂ should also wait for another component SC₃ on VM₁. Although the dependency among components, SC₁, SC₂, and SC₃ is acyclic, the dependency between VMs is cyclic. This may be solved by splitting VM_1 to two VMs, one is for SC_1 and another is for SC_3 , but it causes increased cost and delayed creation. Our formalization can manage any types of resources and solve this kind of problems in a smarter way because it can manage finer grained dependencies, which is shown as invocation rules described in Section 7.2.

Next Version of OASIS TOSCA

OASIS TOSCA TC currently discusses the next version (v1.1) to define a standard set of nodes, relationships, and operations [22]. It is planned to use state machines to describe behavior of the standard operations, which is a similar approach as ours. However, the usage is limited to clarify the descriptions of the standard and the way for type architects to define behavior of their own types is out of the scope of standardization. We provide a way to specify behavior of types and show that it can be used for verification.

8.2 Future Issues

While more than six seventh of operators and one third of lemmas for the TOSCA example can be easily defined using predefined operators and proved lemmas, several extensions of our framework are desired to further reduce problem specific coding and proving. The general formalization for messaging mechanism and chains of links is required.

CloudFormation provides a default roll back mechanism when an operation failure occurs but it requires manual operations when the roll back also fails. On the other hand, the current version of TOSCA does not manage operation failures and it focuses on declaratively defining expected configurations of cloud systems. A possible future extension of TOSCA may be to define alternative configurations in failure cases, which our formalization can be extended to handle.

In this dissertation, we explain our framework using examples of system setup operations of cloud systems because cloud orchestration tools currently focus on them. However, TOSCA is designed to be used for any types of system operations such as scale-out and scale-in. One of the main difficulties to specify scaling operations is that they dynamically change the structure of cloud systems, for which our framework should be extended from two points of view. Firstly, some additional guidance is required to design state measuring functions, especially for the case of scale-out where the number of resources in the system will increase. Secondly, while the user of our framework is left responsible for proving the invariant property of $noCycle_C$, it may be not a trivial work as to dynamic structure. Some constraint should be introduced in the cloud system structure to keep acyclicness of dependency. One possible solution is to assume a partial order of types of objects and to allow transition rules to produce dependency only in the descending order. Two techniques to prove the invariant property of $noCycle_C$ described in Section 5.3.3 will be also effective for the solution.

Although the framework focuses on leads-to properties, which is one of the main contribution of this dissertation, safety properties are of another category of important properties that automated system operations should have. The framework also supports to verify invariant properties which may represent various safety properties of cloud orchestration, however, the proof procedure of the framework should be extended to guide verification of typical safety properties of this domain.

Finally, the case study shows the high reuse rate of the abstract entities and proved lemmas provided by the framework, however, its high productivity and maintainability is based on the subjective evaluation of the author. An objective bench marking by novice proof engineers is necessary.

8.3 Conclusion

A general formalization of declarative cloud orchestration is proposed and a framework is provided for interactive developing proof scores. The framework provides (1) a general way to formalize specifications of different kinds of cloud orchestration tools and (2) a procedure for how to verifying leads-to properties, as well as invariant properties, of formalized specifications. It also provides (3) general templates and libraries of formal descriptions for specifying orchestration of cloud systems and (4) proved lemmas for general predicates of the libraries to be used for verification.

The framework has been applied to the verification of specifications of AWS CloudFormation and also of OASIS TOSCA. The provided procedure systematically assists the verification process and makes its generic part be routine work whose efforts are reduced by the provided logic templates and predicate libraries. As a result, a verification engineer can concentrate on the work specific to the individual problem, which brings high productivity by minimizing development efforts and high maintainability by consistent structure of models and proofs.

A related work applied their model checking method to a typical problem in the domain of cloud orchestration, in which many of finite-state systems were checked. Our framework is more general to be applied to different kinds of models in the domain and to be used for interactive theorem proving which can verify systems of arbitrary many number of states in a significantly systematic way.

An example of usage of our formalization shows a general way to manage dependencies of cloud resources which is a smarter one than that of the most popular tool, AWS CloudFormation.

It is also demonstrated that the framework can be used to specify, represent, and verify the behavior models of the standard specification language, OASIS TOSCA, of cloud orchestration where the standard has not yet provided any ways to do so.

The major contributions of this dissertation are that (1) it introduces the idea of frameworks from software development to proof development which results in high productivity and high maintainability of proofs and (2) it shows that the framework can be effectively applied to a non-trivial problem, that is, to specify, represent, and verify the behavior models of the standard specification language of cloud orchestration.

All of the CafeOBJ codes of the framework and example proof scores in this dissertation can be downloaded at https://github.com/yuki-yoshida/JAIST.

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