

Title	On Anonymity Metrics for Practical Anonymous Communication Protocols
Author(s)	Kitazawa, Shigeki; Soshi, Masakazu; Miyaji, Atsuko
Citation	情報処理学会論文誌, 45(8): 1887-1897
Issue Date	2004-08
Type	Journal Article
Text version	publisher
URL	http://hdl.handle.net/10119/4380
Rights	<p>社団法人 情報処理学会, Shigeki Kitazawa / Masakazu Soshi / Atsuko Miyaji, 情報処理学会論文誌, 45(8), 2004, 1887-1897. ここに掲載した著作物の利用に関する注意: 本著作物の著作権は(社)情報処理学会に帰属します。本著作物は著作権者である情報処理学会の許可のもとに掲載するものです。ご利用に当たっては「著作権法」ならびに「情報処理学会倫理綱領」に従うことをお願いいたします。</p> <p>Notice for the use of this material: The copyright of this material is retained by the Information Processing Society of Japan (IPSJ). This material is published on this web site with the agreement of the author (s) and the IPSJ. Please be complied with Copyright Law of Japan and the Code of Ethics of the IPSJ if any users wish to reproduce, make derivative work, distribute or make available to the public any part or whole thereof. All Rights Reserved, Copyright (C) Information Processing Society of Japan.</p>
Description	

On Anonymity Metrics for Practical Anonymous Communication Protocols

SHIGEKI KITAZAWA,[†] MASAKAZU SOSHI^{††} and ATSUKO MIYAJI^{††}

Anonymous communication protocols are indispensable to protect users' privacy in open networks such as the Internet. Therefore they have wide application, e.g., electronic voting, and enormous research has been conducted on them. However, since it is difficult to devise general 'anonymity metrics' for practical anonymous protocols such as Crowds, few attempts have been made so far to establish such measures. Therefore, toward anonymity evaluation of practical anonymous networks, first we propose and formalize two novel anonymity metrics for practical anonymous communication networks. Next we shall discuss whether or not deterministic protocols can provide anonymity efficiently in terms of computational complexity. Unfortunately, we can show that it is difficult to build efficient anonymous networks only by means of deterministic approaches. We also run simulation experiments and discuss the results.

1. Introduction

Anonymous communication networks are indispensable to protect privacy of users in open networks such as the Internet. Therefore they have wide application, e.g., electronic voting, and enormous research has been conducted on them^{1)~5),12),15)~19),22)}. The simplest way of establishing anonymous networks is given as follows. When Alice sends a message to Bob anonymously, she first dispatches it to a trusted *proxy* (or anonymizer) and then the proxy forwards the message to Bob. Consequently Bob cannot know who originally injected the message into the network and thus anonymous communication is achieved. This is essentially the same as what Anonymizer does²⁾. In this paper, an entity which initiates anonymous communication is called an *initiator*, and an entity for which messages of the initiator are destined is called a *responder*. Furthermore, we use the terms 'proxy' and 'node' interchangeably in this paper.

Anonymous networks, however, could not be useful unless we can evaluate anonymity properties provided by them. Unfortunately, although we can analyze anonymity of some anonymous protocols in a rigorous manner^{1),4),5)}, from a practical point of view, such protocols would often degrade efficiency or incur some cost. For example, Ref. 5) requires a

lot of servers and Ref. 4) is quite ineffective.

On the other hand, with respect to practical anonymous networks^{2),12),15),18),19)}, it is difficult to evaluate anonymity attained in the networks. This is mainly due to the lack of *anonymity metrics* for practical anonymous networks.

However, since it is difficult to devise general anonymity metrics for practical anonymous networks such as Crowds¹⁹⁾, although several attempts for them have been made so far^{6),19),21),23),25)}, none is considered to be perfect.

For example, let us consider *the degrees of anonymity* discussed by Reiter and Rubin¹⁹⁾. They are general and useful, although, at the same time they are informal as Reiter and Rubin themselves mentioned. Furthermore, unfortunately, Díaz, et al.⁶⁾ suggested that the anonymity degrees do not take into consideration situations where an attacker can determine an appropriate probability distribution for the initiator of a message within the anonymity set and thus she is distinguishable by the attacker.

Therefore, toward anonymity evaluation of practical anonymous networks, first we propose two novel anonymity metrics for practical anonymous communication networks .

However, to be fair, we also point out that a quite effective and robust MIX network is proposed by Jakobsson and Juels¹⁴⁾.

Our work was in part inspired by Reiter and Stubblebine²⁰⁾, although it discusses authentication metrics. They argued that the notion of path independence can be regarded as authentication

[†] Mitsubishi Electric Corporation Information Technology R&D Center

^{††} School of Information Science, Japan Advanced Institute of Science and Technology

Anonymity metrics proposed in this paper are based on the following observations:

- (1) Generally speaking, anonymous networks have several intermediate proxies en route from an initiator to a responder. In such a case, as the number of the intermediate proxies increases, i.e., the path that messages in anonymous communication follows becomes longer, anonymity provided by the anonymous protocols becomes higher^{3),(18),(19),(22)}. On the other hand, communication costs, which can be represented by communication paths, cannot be infinitely high. Due to performance reasons, constraints by network architectures, and so on, the costs are under restriction to some degree.
- (2) As discussed above, the most primitive form of anonymous communication is via one or more proxies. Hence, if an initiator wants to communicate with several *distinct* responders anonymously and she can always choose an intermediate trusted proxy on the path to every responder, then such anonymous networks can afford desirable anonymity.

Later in this paper, from the viewpoints as discussed above, we formalize the anonymity metrics for practical anonymous networks.

Next we shall discuss whether or not deterministic anonymous networks can provide anonymity efficiently in terms of computational complexity. Unfortunately, we can show that we have little hope of efficient anonymous networks only by means of deterministic approaches.

As a result we need to invent practical anonymous networks by probabilistic or heuristic means. Hence we consider several possible (practical) anonymous protocols, run simulation experiments for them, and discuss the re-

metrics. Then they formalized the problems of locating maximum set of independent authentication paths as *Bounded Disjoint Paths* and *Bounded Connective Paths* and showed that the two problems are not solvable in polynomial-time. Hence heuristic approaches are required, so that they ran some simulation experiments and demonstrated the effectiveness of their work.

Note that this situation is *different* from the one where the initiator dynamically chooses different paths to a *single* designated responder. The latter case could be vulnerable to a *predecessor attack*²⁵⁾ (a similar situation is discussed in Ref. 19)), but the former is not what the predecessor attack supposes. This is further discussed in Section 2.2.

sults. Simulation results show that we can enhance anonymity only by taking into consideration the neighborhood nodes. Especially, anonymous protocols considered in the experiments suggest some possible extensions to the famous Crowds anonymous system.

The rest of the paper is organized as follows. In Section 2 we propose novel anonymous metrics and discuss various aspects of them. In Section 3 we run simulation experiments to investigate heuristic approaches. Finally, we conclude this paper in Section 4.

2. Proposed Anonymity Metrics and Evaluation

In this section, we propose and discuss two anonymity metrics for practical anonymous networks.

As stated in Section 1, our proposed metrics are briefly summarized as follows:

- (1) anonymity properties with respect to communication paths, and
- (2) anonymity properties with respect to the possibility of selecting trusted proxies.

In this section, we first present the background of each anonymity metrics and then formalize the two metrics. Next we discuss whether or not deterministic protocols can provide anonymity efficiently in terms of computational complexity. Unfortunately, we can show that we have little hope of efficient anonymous networks only by means of deterministic approaches.

2.1 Anonymity Metric (1)

2.1.1 Background

- (1) Generally speaking, as the number of the intermediate proxies on anonymous communication path increases, anonymity provided by the anonymous network becomes higher.
- (2) On the other hand, communication costs cannot be infinitely high. Due to performance reasons, constraints by network architectures, and so on, the costs are under restriction to some length.

Issues of increasing anonymous communication paths to enhance anonymity (or security) have been discussed so far by many researchers. For example, Chaum addressed the issue of *cascading MIXes* in his seminal work³⁾ for the first time. Furthermore, Goldschlag et al. discussed a loose routing scheme in Onion routing, which adds more hops to Onion chains to increase security¹⁰⁾.

However, it is Reiter and Rubin that have discussed in further details the trade-off laid between the increase of anonymity and performance degradation due to the increase of path lengths¹⁹⁾. This is summarized as follows. Let p_f be the forwarding probability of messages by jondos in Crowds. In order to evaluate anonymity provided by Crowds, they calculated the probability that the initiator is the immediate predecessor of a collaborator (attacker) on the path. It is given by $\frac{n-p_f(n-c-1)}{n}$, where n and c are the numbers of the crowd and the collaborators, respectively. From this expression we can immediately see that as p_f increases, the probability that the initiator is exposed decreases (i.e., anonymity enhances). However, note that the increase of the forwarding probability p_f also implies the increase of path lengths. A simple calculation can yield that the expected length of a path in Crowds is $\frac{p_f}{1-p_f} + 2$ (you can find its derivation in Ref. 19)). Again we can easily see that as p_f increases, the average path lengths also increase. Reiter and Rubin concluded that "... multiple types of crowds should exist: those employing a small p_f for better performance but less resilience to collaborating jondos ..., and those using a large p_f to increase security with a cost of performance." For more details on the trade-off between anonymity and performance due to the increase of path lengths, consult Ref. 19).

Now we are in a position to model anonymity properties just discussed. First, in order to develop an abstract model for evaluating anonymity from the viewpoint of the item (1) above, assume that some value is assigned to each node in the network. Moreover, assume that anonymity afforded by anonymous communication can be estimated by adding the value of each node on the path. In other words, a larger value of the sum indicates a higher level of anonymity. Henceforth we suppose that we are given a function which assigns the value to each node and we call the function *privacy function*. The assigned values are called *privacy values*.

On the other hand, communication costs are usually constrained from the viewpoint of the item (2). To express such a situation, let us assume that some value, which is apart from the privacy value of the node, is assigned to each node. Then as the sum of the values on a path becomes larger, the cost of the path becomes

larger. Henceforth we suppose that we are given a function which assigns the value to each node and we call the function *cost function*. The assigned values are called *cost values*.

Given a network system, it would be straightforward to define cost functions. With respect to privacy functions, we can consider various ways of deriving them. For instance, in the simplest case, we can assign one to each node as its privacy value. Then the sum of the privacy values of the nodes on an anonymous communication path exactly means the hop count and it well expresses a situation where the degree of anonymity becomes higher as the path gets longer.

We can consider a bit more elaborate example. Note that ISO defines the international standard for security system evaluation, i.e., ISO 15408¹³⁾. In the standard, 'Security Functional Requirements' prescribes several privacy conditions (Class FPR: Privacy), that is, FPR_AANO Anonymity, FPR_PSE Pseudonymity, FPR_UNO Unobservability, and FPR_UNL Unlinkability, some of which are further divided into a few levels. Now let us take a look at FPR_AANO Anonymity, which has two levels. Moreover, let us suppose that we assign some privacy value to each system, according to its level of FPR_AANO, i.e., (i) no FPR_AANO rating, (ii) FPR_AANO.1, or (iii) FPR_AANO.2. In such a case, the sum of the privacy values indicates the level of anonymity of the anonymous path with respect to FPR_AANO Anonymity.

Finally, we can take advantage of various available rating methods such as those used in reputation systems^{7),8)}.

In summary, privacy and cost functions provide abstraction for anonymity properties as mentioned above. In the rest of this paper, we suppose that these two functions are given in advance. However, as shown later, it is shown that even if such functions are available, effective anonymous communication networks can hardly be built only by means of deterministic methods.

2.1.2 Formalization and Evaluation

In this section, we formalize the anonymity metric discussed in Section 2.1.1.

First, a network is supposed to be represented

Alternatively, we can assign a cost value to a communication link. However, for simplicity, in this paper we model it as is given above.

by a directed graph $G = (V, E)$. Here V is a set of nodes (proxies) and E is a set of directed edges. In general $E \subseteq V \times V$ holds.

Hereinafter in this paper we denote an initiator and a responder by s and d ($\in V$), respectively, unless explicitly stated. Moreover, as discussed in Section 2.1.1, we assume that privacy function $\mathcal{P} : V \rightarrow N$ and cost function $\mathcal{C} : V \rightarrow N$ are given. Here N is a set of non-negative integers.

Now we are ready to define the anonymity metric as follows:

Definition 1 In a directed graph G , with respect to a path $v_1 (= s), v_2, \dots, v_n (= d)$, if $\sum_{i=1}^n \mathcal{P}(v_i) \geq p$ and $\sum_{i=1}^n \mathcal{C}(v_i) \leq c$, then we call the path (p, c) -anonymous.

Next we shall discuss whether or not deterministic protocols can efficiently provide anonymity in terms of the metric. For that purpose, we define a decision problem corresponding to the anonymity metric as follows:

Problem 1 $((p, c)$ -anonymity)
[INSTANCE] A directed graph $G = (V, E)$, $s, d \in V$, and privacy function $\mathcal{P} : V \rightarrow N$ and cost function $\mathcal{C} : V \rightarrow N$.

[QUESTION] Is there a (p, c) -anonymous path from s to d ?

Now we can prove Theorem 1.

Theorem 1 (p, c) -anonymity is NP complete.

Proof: Given G , privacy function \mathcal{P} , cost function \mathcal{C} , and a path $v_1 (= s), v_2, \dots, v_n (= d)$, it should be obvious that in polynomial time we can determine whether or not the path is (p, c) -anonymous. Thus we can construct a non-deterministic algorithm to solve (p, c) -anonymity in polynomial time and consequently (p, c) -anonymity is in NP.

Now we show that “PARTITION”, which is known to be NP-complete, is polynomially reducible to (p, c) -anonymity. PARTITION is defined as follows⁹⁾:

Problem 2 (PARTITION)
[INSTANCE] A finite set $A = \{a_1, a_2, \dots, a_n\}$ and a size function $w : A \rightarrow N$.
[QUESTION] Is there a subset $A' \subseteq A$ such that $\sum_{a \in A'} w(a) = \sum_{a \in A - A'} w(a)$?

When we are given an arbitrary instance of PARTITION, we construct the following graph

$G = (V, E)$, and define privacy function \mathcal{P} , cost function \mathcal{C} , and the privacy and cost values p and c respectively.

$$V = \{a_{1,0}, a_{2,0}, \dots, a_{n,0}, a_{(n+1),0}\} \cup \left(\bigcup_{i=1}^n \{a_{i,1}, a_{i,2}\} \right)$$

$$E = \left(\bigcup_{i=1}^n \{(a_{i,0}, a_{i,1})\} \right) \cup \left(\bigcup_{i=1}^n \{(a_{i,0}, a_{i,2})\} \right) \cup \left(\bigcup_{i=1}^n \{(a_{i,1}, a_{(i+1),0})\} \right) \cup \left(\bigcup_{i=1}^n \{(a_{i,2}, a_{(i+1),0})\} \right)$$

$$\mathcal{P}(a_{i,1}) = \mathcal{C}(a_{i,1}) = w(a_i) \quad (i = 1, \dots, n)$$

$$\mathcal{P}(a_{i,2}) = \mathcal{C}(a_{i,2}) = 0 \quad (i = 1, \dots, n)$$

$$\mathcal{P}(a_{i,0}) = \mathcal{C}(a_{i,0}) = 0 \quad (i = 1, \dots, n + 1)$$

$$p = c = \frac{1}{2} \sum_{i=1}^n w(a_i)$$

where $a_{i,0} = s$ and $a_{(n+1),0} = d$.

To illustrate the above reduction, for example we depict in Fig. 1 the reduction where the instance of PARTITION is $A = \{a_1, a_2, a_3\}$, $w(a_1) = 3, w(a_2) = 5, w(a_3) = 2$.

Let us now suppose that PARTITION has a solution $A' = \{a_{i_1}, a_{i_2}, \dots, a_{i_j}\}$. Without loss of generality, assume that $i_1 < i_2 \dots < i_j$. In such a case we define a function δ as follows:

$$\delta(k) = \begin{cases} 1 & \text{if } k = i_l \text{ for some } l \\ 2 & \text{otherwise} \end{cases}$$

By using function δ , consider a path $P = a_{1,0}, a_{1,\delta(1)}, a_{2,0}, a_{2,\delta(2)}, \dots, a_{n,\delta(n)}, a_{(n+1),0}$. We can readily see that P is (p, c) -anonymous in G . This is because $\sum_{a \in P} \mathcal{P}(a) = \sum_{a \in P} \mathcal{C}(a) = \frac{1}{2} \sum_{i=1}^n w(a_i)$ ($= p = c$). For example, in Fig. 1, the path corresponds to $a_{1,0}, a_{1,1}, a_{2,0}, a_{2,2}, a_{3,0}, a_{3,1}, a_{4,0}$.

Conversely, assume that graph G has a (p, c) -anonymous path. Let us further assume that $a_{i_1,1}, a_{i_2,1}, \dots, a_{i_j,1}$ are all nodes such that the second subscript is one. It is now clear that $\{a_{i_1}, a_{i_2}, \dots, a_{i_j}\} (= A')$ is a solution of PARTITION. \square

It is well-known that in some NP-complete problems there exist algorithms to find solutions which are never far from optimal ones by more than some specific bounds. They are called *approximation algorithms*⁹⁾. Unfortunately, (p, c) -anonymity is so difficult that there does not exist such an approximation al-

Here we model a network in a traditional way. However, we have run simulation experiments while we take into consideration network topologies that conform the topology of the Internet as much as possible. See Section 3.

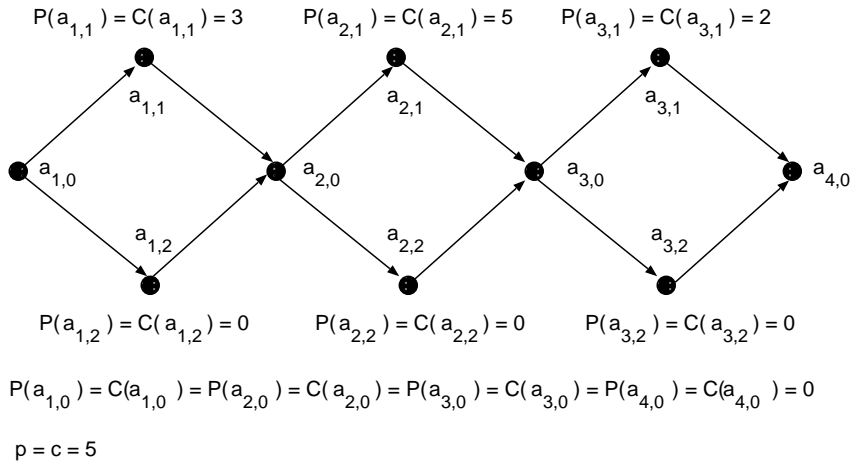


Fig. 1 Reduction from PARTITION.

gorithm. This will be shown below.

We denote by I an instance of (p, c) -anonymity with some fixed c . Furthermore, a solution by an optimization algorithm that maximizes $\sum_{i=1}^n \mathcal{P}(v_i)$ of I is denoted by $OPT(I)$ (such problems are called *optimization problems*). Obviously (p, c) -anonymity is no more difficult than a problem to find $OPT(I)$ and the latter problem is thus NP-hard.

Now we can prove Theorem 2.

Theorem 2 If $P \neq NP$, then there does not exist a deterministic polynomial algorithm (approximation algorithm) A which can guarantee $|OPT(I) - A(I)| \leq p'$ for a fixed p' and all instances I of the optimization problems for (p, c) -anonymity.

Proof: We prove this theorem by contradiction. Without loss of generality, assume that p' is a positive integer.

Suppose that there is an A in Theorem 2. In such a case, by using A , we can construct a deterministic polynomial algorithm B which can solve (p, c) -anonymity, which contradicts the assumption $P \neq NP$.

B is actually constructed as follows. First we denote by I' a new instance where privacy function \mathcal{P} is replaced by \mathcal{P}' , which is defined as $\mathcal{P}'(v) = (p' + 1)\mathcal{P}(v)$.

Then candidate solutions for I' are clearly the same as those for I and the privacy value of a solution for I' is $(p' + 1)$ times the corresponding value for I . Now note that every solution for I' is a multiple of $p' + 1$ and that $|OPT(I') - A(I')| \leq p'$ holds. So it must hold that $|OPT(I') - A(I')| = 0$ and finally we can conclude that $|OPT(I) - B(I)| = |OPT(I') -$

$A(I')|/(p' + 1) = 0$. However, the fact also means that we can find $OPT(I)$ in polynomial time. This is a contradiction. \square

2.2 Anonymity Metric (2)

In this section we propose and discuss another anonymity metric.

2.2.1 Background

As discussed in Section 1, the most primitive form of anonymous communication is via one or more proxies. However, in practical anonymous communication networks, it is not always possible to select a trusted proxy when an initiator anonymously sends messages to a responder because of the network topology or the locations of the initiator or responder. Moreover, we cannot trust all proxies in the network.

Hence, if an initiator wants to communicate with several *distinct* responders anonymously and she can always choose an intermediate trusted proxy on the path to every responder, then such anonymous networks can afford desirable anonymity.

Note that this situation is *different* from the one where the initiator dynamically chooses different paths to a *single* designated responder. The latter case, especially when the attackers can identify the anonymous communication stream in the paths, could be vulnerable to a *predecessor attack*²⁵⁾ (a similar situation is discussed in Ref. 19)). On the other hand, notice that we are now supposing the situation where an initiator wants to communicate with *multiple and different* responders. Then the initiator tries to choose an intermediate trusted proxy on the path to each responder. In this case the anonymous communication streams are differ-

ent and the attackers can not always identify them. In summary, this case is not what the predecessor attack supposes.

Now we can consider anonymity metric whether or not we can arrange trusted proxies in the anonymous network in such a way as stated above.

2.2.2 Formalization and Evaluation

Here we formalize anonymity metric discussed in Section 2.2.1.

First, as in Section 2.1.2, we regard a network as a directed graph $G = (V, E)$. Moreover, let $s \in V$ and a set of nodes $\{d_1, d_2, \dots, d_j\} \subseteq V$ be an initiator and a set of responders, respectively.

Now we can formalize anonymity metric discussed in Section 2.2.1 as follows:

Definition 2 Suppose that we are given a directed graph $G = (V, E)$, $s \in V$, and a set of nodes $\{d_1, d_2, \dots, d_j\} \subseteq V$. In such a case, if for a fixed positive value t ($\leq |V|$) there exist a subset $T \subseteq V$, $|T| \leq t$ such that we can always find some $n \in T$ on paths from s to every $d \in \{d_1, \dots, d_j\}$, then we call G is t -locatable with respect to s and $\{d_1, \dots, d_j\}$.

Next we shall discuss whether or not deterministic protocols can efficiently provide anonymity in terms of the metric. For that purpose, we define a decision problem corresponding to the anonymity metric as follows:

Problem 3 (t -locatability)

[INSTANCE] A directed graph $G = (V, E)$, $s \in V$, a responder set $\{d_1, d_2, \dots, d_j\} \subseteq V$, and a positive value t ($\leq |V|$).

[QUESTION] Is a graph G t -locatable with respect to initiator s and a responder set $\{d_1, d_2, \dots, d_j\}$?

Based on the above definitions, we can now prove Theorem 3.

Theorem 3 t -locatability is NP-complete.

Proof: t -locatability is in NP. This is because we can construct a non-deterministic polynomial algorithm which arbitrarily chooses a subset of V and determines whether or not the subset satisfies the condition of t -locatability.

Next we show that an NP-complete problem, "VERTEX COVER", is in polynomial time reduced to t -locatability. VERTEX COVER is defined below⁹⁾:

Problem 4 (VERTEX COVER)

[INSTANCE] Graph $G = (V, E)$, positive integer $K \leq |V|$.

[QUESTION] Is there a vertex cover of size K or less for G , i.e., a subset $V' \subseteq V$ with

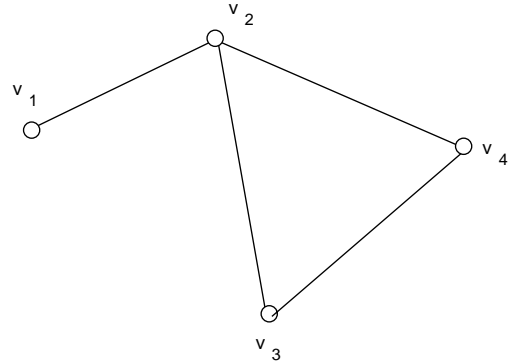


Fig. 2 An Instance of VERTEX COVER.

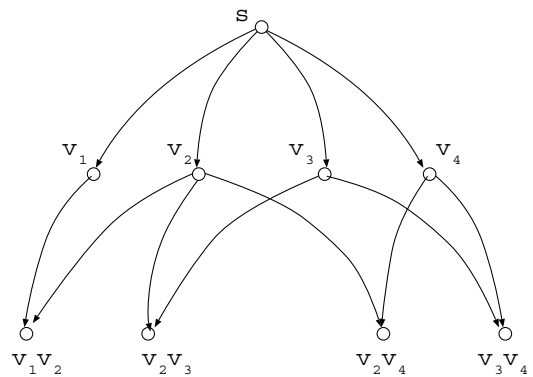


Fig. 3 Reduction from VERTEX COVER.

$|V'| \leq K$ such that for each edge $\{u, v\} \in E$ at least one of u and v belongs to V' ?

where G is an undirected graph.

Given an instance of VERTEX COVER, we transform it into an instance of t -locatability, which is defined as follows:

- Graph $G'' = (V'', E'')$, where $V'' = \{s\} \cup V \cup \{v_1v_2 \mid (v_1, v_2) \in E\}$ and $E'' = \{(s, v) \mid v \in V\} \cup \{(v_1, v_1v_2), (v_2, v_1v_2) \mid (v_1, v_2) \in E\}$.
- initiator = s ,
- responder set = $\{v_1v_2 \mid (v_1, v_2) \in E\}$
- $t = K$

Note that in the above reduction, v_1v_2 ($(v_1, v_2) \in E$) represents a single node in G'' .

To demonstrate an example of the reduction, we pay attention to an instance of VERTEX COVER as shown in Fig. 2. The instance is reduced to the instance of t -locatability depicted in Fig. 3.

Below we show that the reduction given above is actually polynomial time reduction from VERTEX COVER to t -locatability.

First let us suppose that VERTEX COVER

has a solution $V' = \{v_{i_1}, v_{i_2}, \dots, v_{i_j}\}$ ($j \leq K$). In such a case $T = V'$ ($\subseteq V''$) is a solution for the corresponding instance of t -locatability. The reason is as follows. Let $R = \{v_1v_2 \mid (v_1, v_2) \in E\}$ be a responder set of G'' . Then a path from s to a responder $v_1v_2 \in R$ is either $s \rightarrow v_1 \rightarrow v_1v_2$ or $s \rightarrow v_2 \rightarrow v_1v_2$. Keeping in mind that $(v_1, v_2) \in E$ and V' is a solution of VERTEX COVER, we can see that either $v_1 \in V'$ ($= T$) or $v_2 \in V'$ ($= T$) holds. Consequently all we have to do is to place a proxy on v_1 ($\in V''$) or v_2 ($\in V''$), respectively in the former case or the latter.

Conversely, if an instance of t -locatability given above has a solution $T = \{v_{i_1}, v_{i_2}, \dots, v_{i_j}\}$, then we can conclude that $V' = T$ in a similar manner.

At this stage it should be clear that the above reduction can be done in polynomial time. \square

Now we consider an approximation algorithm to the optimization problem for t -locatability. In a similar way as in the case of (p, c) -anonymity, given an instance I of the optimization problem for t -locatability, we denote by $OPT(I)$ a solution found by an optimization algorithm of the problem that minimizes t . Then we can show that it is difficult to even find a solution approximate to the optimal one.

Theorem 4 If $P \neq NP$, then no polynomial time approximation algorithm A for t -locatability can guarantee $|OPT(I) - A(I)| \leq t'$ for a fixed constant t' .

Proof: We can show this theorem again by contradiction as Theorem 2. Without loss of generality, we assume that t' is a positive integer.

Suppose that A is actually such an approximate algorithm in Theorem 4. Then by using A we can construct a deterministic polynomial time algorithm B which can solve t -locatability.

B is constructed as follows. First we consider a new instance I' of t -locatability, where graph G is replaced by a new graph $G' = (V', E')$. G' has the same s as I and consists of $(t' + 1)$ graphs, each of which is isomorphic to G .

More precisely, G' is defined as follows:

$$\begin{aligned} V' &= \{s\} \cup \{v[i] \mid v \in V, 1 \leq i \leq t' + 1\} \\ &\quad \cup \{v_1[i]v_2[i] \mid \\ &\quad \quad v_1v_2 \in V, 1 \leq i \leq t' + 1\} \\ E' &= \{(s, v[i]) \mid v \in V, 1 \leq i \leq t' + 1\} \\ &\quad \cup \{(v_1[i], v_1[i]v_2[i]) \mid \\ &\quad \quad v_1v_2 \in V, 1 \leq i \leq t' + 1\} \end{aligned}$$

$$\begin{aligned} &\cup \{(v_2[i], v_1[i]v_2[i]) \mid \\ &\quad v_1v_2 \in V, 1 \leq i \leq t' + 1\} \end{aligned}$$

Then the corresponding nodes in G to candidate solutions for I' are clearly the candidate solutions for I and the number of proxies of a solution for I' is $(t' + 1)$ times the corresponding value for I . Now note that every solution for I' is a multiple of $t' + 1$ and that $|OPT(I') - A(I')| \leq t'$ holds. So it must hold that $|OPT(I') - A(I')| = 0$ and finally we can conclude that $|OPT(I) - B(I)| = |OPT(I') - A(I')| / (t' + 1) = 0$. However, the fact also means that we can find $OPT(I)$ in polynomial time. Contradiction. \square

2.3 Discussion

So far we have proposed and thoroughly discussed two new anonymity metrics for practical anonymous networks ((p, c) -anonymity, t -locatability). It is also possible to develop other anonymity metrics. In this section we take into consideration some anonymity metrics other than (p, c) -anonymity and t -locatability.

For example, as mentioned before, it is the most intuitive to adopt anonymity metric which considers anonymity properties where the level of anonymity becomes higher as the path which anonymous communication follows becomes longer. Generally speaking, this can be formalized by a decision problem "LONGEST PATH"⁹⁾.

Problem 5 (LONGEST PATH)

[INSTANCE] Graph $G = (V, E)$, length $l(e) \in Z^+$ for each $e \in E$, positive integer K , specified vertices $s, t \in V$.

[QUESTION] Is there a simple path in G from s to t of length K or more, i.e., whose edge lengths sum to at least K ?

LONGEST PATH is also known to be NP-complete⁹⁾.

Let us consider another anonymity metric. When an initiator sends many messages to a responder anonymously, as the number of paths the messages follow becomes larger, it becomes more difficult for attackers to gather information about the initiator and the responder and thus more anonymity would be provided.

Anonymity metric for the case just mentioned can be formalized by (bounded) disjoint paths⁹⁾. Bounded disjoint paths are a set of paths whose lengths are limited by some bound and no pair of which have a node in common. More formally, the problem is defined as follows.

Problem 6 (MAXIMUM LENGTH-BOUNDED DISJOINT PATHS)

[**INSTANCE**] Graph $G = (V, E)$, specified vertices s and t , positive integers $J, K \leq |V|$.

[**QUESTION**] Does G contain J or more mutually vertex disjoint paths from s to t , none involving more than K edges?

MAXIMUM LENGTH-BOUNDED DISJOINT PATHS is NP-complete⁹⁾.

We also considered other anonymity metrics, which are omitted from this paper due to the lack of space, most of which are in NP-complete. Needless to say, it is strongly believed that it is almost impossible to solve NP-complete problems efficiently (i.e., in polynomial time). This implies that $NP \neq P$. As a consequence we have succeeded in showing some theoretical limits of deterministic approaches.

Therefore based on the discussion so far, generally speaking, it is difficult to establish effective practical anonymous networks only by means of deterministic approaches. Hence practical anonymous networks should be built with probabilistic or heuristic approaches.

3. Heuristic Approaches and Simulation Experiments

Based on the discussion in the previous section, we can consider several heuristic approaches for practical anonymous protocols. In this section we shall present the approaches, conduct simulation experiments to investigate how they work, and finally discuss several aspects of them. Especially, anonymous protocols considered in the experiments suggest some possible extensions to the famous Crowds anonymous system. Furthermore, we show that if we monitor only the neighbors and assign appropriate privacy and cost values to the nodes, then we can get significant effects.

3.1 Descriptions of Simulations

In this section we discuss the background for our simulation experiments.

In order to conduct network simulation, first we have to generate network topologies which conform to the existing networks. Therefore in these years many researches have been done on such network generators. In our simulation ex-

periments, we have used *Inet* topology generator developed in Michigan University²⁴⁾.

Next we focus our attention on privacy and cost functions. Although we can suppose various privacy and cost functions, in the simulation we define the functions according to the following policies:

N1 Privacy and cost values are generated at random.

N2 Larger cost and smaller privacy values are assigned to articulation nodes. Intuitively speaking, articulation nodes are the points where various paths join and so the attacks to such nodes can pose a serious threat to anonymity properties. In other words, N2 is one example scenario in favor of attackers.

In our simulation, we assign every articulation node and its adjacent node (i.e., connected through an edge) to more than 0.8 times the maximum cost value with probability 0.8. Furthermore, with probability 0.8, we assign every articulation node and its adjacent node to less than 0.2 times the maximum privacy value.

Furthermore, in our simulation we implement the following anonymous communication protocols.

P1 Crowds protocol¹⁹⁾

P2 Crowds protocol with a strategy to choose a node with the smallest cost value when forwarding messages.

P3 Crowds protocol with a strategy to choose a node with the largest anonymity value when forwarding messages.

P4 protocol to choose a path with the smallest sum of the cost values of the nodes on the path.

P5 shortest path (just for comparison)

P6 A single trusted proxy

3.2 Evaluation

As stated in Section 3.1, there are two ways of network conditions (N1 and N2) and five ways of protocols (P1, P2, P3, P4, P5, and P6). Thus we combinedly have twelve ways of simulation experiments. Henceforth we call each of them P1+N1, P1+N2, P2+N1, P2+N2, P3+N1, P3+N2, P4+N1, P4+N2, P5+N1, P5+N2, P6+N1, and P6+N2, respectively.

The network topology used in our simulation

In some systems^{2)~4),18)}, anonymous communication paths are fixed or determined in advance. However, except for a few systems such as anonymizer and simple broadcast type ones, most of them use encryption or random numbers and hence have undeterministic features.

Articulation nodes are what increase the number of connected components of the graph if they are removed¹¹⁾.

Table 1 Simulation results (N1).

	P1+N1	P2+N1	P3+N1	P4+N1	P5+N1	P6+N1
length	5.68	5.55	5.86	3.93	3.86	6.48
cost	2968.53	2390.54	3112.20	1790.56	2174.50	2954.33
privacy	3119.67	2973.76	3818.19	2259.76	2232.12	3910.45

Table 2 Simulation results (N2).

	P1+N2	P2+N2	P3+N2	P4+N2	P5+N2	P6+N2
length	5.51	5.71	5.59	3.77	3.88	6.55
cost	5392.66	4893.18	5132.26	3670.01	4019.74	6028.06
privacy	1125.10	1512.52	1751.69	1039.15	843.36	1710.71

was generated by Inet and the number of the nodes is 3037. Privacy and cost values are integers from 0 to 1000. The forwarding probability of Crowds is 2/3. Finally, initiators and responders were chosen randomly and each experiment was run 1000 times. We show the averages of the simulation experiments in **Table 1** and **Table 2**.

In the following evaluation, we regard P1+N1, i.e., Crowds protocol on a network with random privacy and cost values, as the base for comparison.

First consider the case in Table 1. In comparison of P2+N1 with P1+N1, since P2 selects a node with the smallest cost value, the average of the value decreases by 19.5%. At the same time, the average privacy value also decreases by 4.7%. However, the rate of decrease of the cost value is greater than that of the privacy and consequently it shows the effectiveness of P2.

Similarly, in comparison of P3+N1 with P1+N1, since P3 selects a node with the largest privacy value, the average of the value increases by 22.4%. On the other hand, the average cost value also increases, but only by 4.8%. Hence we can see that P3 is also a promising heuristic.

With respect to P4+N1, since P4 selects a path with the smallest sum of the cost values of the nodes on the path, the rate of decrease of cost values is the largest (39.7% decrease in comparison with P1+N1). However, the rate of decrease of the privacy values is also large (27.6% decrease in comparison with P1+N1). This is partly because paths with smaller cost values are often shorter and hence privacy values also become smaller.

This consideration is supported by the comparison of P5+N1 with P1+N1. That is, generally speaking, as a path becomes shorter, the sums of privacy and cost values on the path also become smaller. Consequently it is not obvious

whether or not P4 and P5 are useful.

Now we discuss P6+N1. This shows some increase with respect to path length (14.1% in comparison with P1+N1). This is due to the constraint where messages must go through a trusted proxy. Although costs are almost the same in both cases, the privacy values of P6+N1 increases by 25.3% in the average because of the increases of the path lengths.

In the case in Table 2, we can evaluate the experiments in a similar way as in Table 1. However, in Table 2, we can immediately see that cost and privacy ratios of P2+N2, P3+N2 and P4+N2 with respect to P1+N2 are better than those of P2+N1, P3+N1 and P4+N1 with respect to P1+N1, respectively. This is because N2 is a scenario in favor of attackers and we can obtain greater effects from anonymous protocols which try to enhance anonymity. On the other hand, it is not clear whether or not P5+N2 and P6+N2 are more effective than P5+N1 and P6+N1, respectively.

Note that P1 (Crowds), P2, and P3 do not need information about a whole network, but only about the neighborhood nodes. In other words, from the simulation experiments, we can see that if we monitor only the neighbors and assign appropriate privacy and cost values to the nodes, then we can get significant effects. In particular, since Crowds does not take into consideration such cases, if we slightly modify it as P2 or P3, then we can get more effective version of Crowds anonymous communication protocols.

4. Conclusion

Anonymous communication networks are indispensable to protect users' privacy in open networks such as the Internet. In the paper we have evaluated various aspects of anonymity properties afforded by practical anonymous communication networks.

In this paper we proposed two novel anonymity metrics for practical anonymous communication networks. Furthermore we discussed whether or not deterministic protocols can provide anonymity efficiently in terms of computational complexity. Unfortunately, we can show that we have little hope of efficient anonymous networks only by means of deterministic approaches.

Finally we run simulation experiments and discussed the results. Simulation results show that we can enhance anonymity only by taking into consideration the neighborhood nodes. Especially, anonymous protocols considered in the experiments suggest some possible extensions to the famous Crowds anonymous system.

Acknowledgments The authors would like to thank the anonymous referees for valuable and helpful comments on this paper.

References

- 1) Abe, M.: Universally Verifiable Mix-net with Verification Work Independent of the Number of Mix-servers, *IEICE Transaction on Fundamentals*, Vol.E83-A, No.7, pp.1431–1440 (2000).
- 2) Anonymizer: <http://www.anonymizer.com/>.
- 3) Chaum, D.: Untraceable Electronic Mail, Return Addresses, and Digital Pseudonyms, *Comm. ACM*, Vol.24, No.2, pp.84–88 (1981).
- 4) Chaum, D.: The Dining Cryptographers Problem: Unconditional Sender and Recipient Untraceability, *Journal of Cryptography*, Vol.1, No.1, pp.65–75 (1988).
- 5) Desmedt, Y. and Kurosawa, K.: How to Break a Practical MIX and Design a New One, *Advances in Cryptography—EUROCRYPT 2000*, Preneel, B.(Ed.), Lecture Notes in Computer Science, Vol.1807, pp.557–572, Springer-Verlag (2000).
- 6) Díaz, C., Seys, S., Claessens, J. and Preneel, B.: Towards Measuring Anonymity, *Privacy Enhancing Technologies (PET)*, Dingledine, R. and Syverson, P.F.(Eds.), Lecture Notes in Computer Science, Vol.2482, pp.54–68, Springer-Verlag (2002).
- 7) Dingledine, R., Freedman, M.J., Hopwood, D. and Molnar, D.: A Reputation System to Increase MIX-Net Reliability, *Information Hiding: 4th International Workshop, IHW 2001*, Moskowitz, I.S.(Ed.), Lecture Notes in Computer Science, Vol.2137, pp.126–140 (2001).
- 8) Dingledine, R. and Syverson, P.: Reliable MIX Cascade Networks through Reputation, *Sixth International Financial Cryptography Conference (FC 2002)* (2002).
- 9) Garey, M.R. and Johnson, D.S.: *Computers and Intractability—A Guide to the Theory of NP-completeness*, W.H. Freeman and Co. (1979).
- 10) Goldschlag, D.M., Reed, M.G. and Syverson, P.F.: Hiding Routing Information, *Information Hiding*, Anderson, R.(Ed.), Lecture Notes in Computer Science, Vol.1174, pp.137–150, Springer-Verlag (1996).
- 11) Harary, F.: *Graph Theory*, Perseus Publishing (1995).
- 12) Inoue, D. and Matsumoto, T.: Rivulet: An Anonymous Communication Method Based on Group Communication, *IEICE Transactions on Fundamentals of Electronics, Communications and Computer Sciences*, Vol.E85-A, No.1, pp.94–101 (2002).
- 13) International Organization of Standardization (ISO): International Standard ISO/IEC 15408 (1999). Technically identical to Common Criteria version 2.1.
- 14) Jakobsson, M. and Juels, A.: An Optimally Robust Hybrid MIX Network, *Proc. 20th Annual ACM Symposium on Principles of Distributed Computing (PODC)*, pp.284–292 (2001).
- 15) Kitazawa, S., Nagano, S., Soshi, M. and Miyaji, A.: Anonymous Communication with Elementary Cyclic Routes, *IPSJ Journal*, Vol.41, No.8, pp.2148–2160 (2000). (In Japanese).
- 16) Kitazawa, S., Soshi, M. and Miyaji, A.: An Agent-Based Model of Anonymous Communication Protocols, *Proc. 10th IEEE International Workshops on Enabling Technologies: Infrastructure for Collaborative Enterprise (WET-ICE 2001)*, pp.177–182 (2001).
- 17) Kitazawa, S., Soshi, M. and Miyaji, A.: Evaluation of Anonymity of Practical Anonymous Communication Networks, *8th Australasian Conference on Information Security and Privacy—ACISP 2003*, Safavi-Naini, R. and Seberry, J.(Eds.), Lecture Notes in Computer Science, Vol.2727, pp.13–26, Springer-Verlag (2003).
- 18) Pfitzmann, A.: A Switched/Broadcast ISDN to Decrease User Observability, *Proc. 1984 International Zurich Seminar on Digital Communications, Applications of Coding, Channel Coding and Secrecy Coding*, pp.183–190 (1984).
- 19) Reiter, M.K. and Rubin, A.D.: Crowds: anonymity for Web transactions, *ACM Transactions on Information and System Security*, Vol.1, No.1, pp.66–92 (1998).
- 20) Reiter, M.K. and Stubblebine, S.G.: Path Independence for Authentication in Large-Scale Systems, *ACM Conference on Computer and*

Communications Security, pp.57–66 (1997).

- 21) Serjantov, A. and Danezis, G.: Towards an Information Theoretic Metric for Anonymity, *Privacy Enhancing Technologies (PET)*, Dingledine, R. and Syverson, P.F.(Eds.), Lecture Notes in Computer Science, Vol.2482, pp.41–53, Springer-Verlag (2002).
- 22) Syverson, P.F., Goldschlag, D.M. and Reed, M.G.: Anonymous Connections and Onion Routing, *Proc. IEEE Symposium on Security and Privacy*, pp.44–54 (1997).
- 23) Syverson, P.F., Tsudik, G., Reed, M.G. and Landwehr, C.E.: Towards an Analysis of Onion Routing Security, *Workshop on Design Issues in Anonymity and Unobservability* (2000).
- 24) Winick, J. and Jamin, S.: Inet-3.0: Internet Topology Generator, Technical Report CSE-TR-456-02, University of Michigan (2002).
- 25) Wright, M., Adler, M., Levine, B.N. and Shields, C.: An Analysis of the Degradation of Anonymous Protocols, *Network and Distributed System Security Symposium* (2002).

(Received December 5, 2003)

(Accepted June 8, 2004)



Shigeki Kitazawa received the M.E. and D.E. degrees in information science from Japan Advanced Institute of Science and Technology, Japan, in 1998 and in 2001, respectively. Since joining Mitsubishi Electric Corp. in 2001, he has been working in the field of network security. He is currently a research engineer of Information Technology R&D Center in Mitsubishi Electric Corp. His interests include IP traceback, intrusion detection, anomaly detection, and log analysis.



Masakazu Soshi received his B.E. and M.S. degrees from the University of Tokyo in 1991 and in 1993, respectively, and his Ph.D. degree from the University of Electro-Communications in 1999. He worked as an associate for the University of Electro-Communications from 1997 to 1998 and for the Japan Advanced Institute of Science and Technology (JAIST) from 1999 to January 2003. Since February 2003, he has been a research associate professor of JAIST. His research interests include access matrix models, mobile agent security, anonymous communication, software obfuscation, quantum cryptography, and IP traceback.



Atsuko Miyaji received the B. Sc., the M. Sc., and Dr. Sci. degrees in mathematics from Osaka University, Osaka, Japan in 1988, 1990, and 1997 respectively. She joined Matsushita Electric Industrial Co., LTD from 1990 to 1998 and engaged in research and development for secure communication. She has been an associate professor at JAIST (Japan Advanced Institute of Science and Technology) since 1998. She has joined the computer science department of University of California, Davis since 2002. Her research interests include the application of projective varieties theory into cryptography and information security. She received IPSJ Sakai Special Researcher Award in 2002 and the Standardization Contribution Award in 2003. She is a member of the International Association for Cryptologic Research, the Institute of Electronics, Information and Communication Engineers and the Information Processing Society of Japan.