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<th>Theoretical Assessment of FePt Nanoparticles as Heating Elements for Magnetic Hyperthermia</th>
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<td>Author(s)</td>
<td>Maenosono, Shinya; Saita, Soichiro</td>
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FePt magnetic nanoparticles (MNPs) are expected to be a high-performance nanoheater for magnetic hyperthermia because of their high Curie temperature, high saturation magnetization, and high chemical stability. Here, we present a theoretical performance assessment of chemically disordered fcc-phase FePt MNPs. We calculate heat generation and heat transfer in the tissue when an MNP-loaded tumor is placed on an external alternating magnetic field. For comparison, we estimate the performances of magnetite, maghemite, FeCo, and L10-phase FePt MNPs. We find that an fcc FePt MNP has a superior ability in magnetic hyperthermia.

Index Terms—Bioheat transfer equation, cancer treatment, hyperthermia, iron-platinum nanoparticle.

I. INTRODUCTION

Hyperthermia is one of many techniques used in oncology, based on heating tumors for therapeutic purposes, and usually used as an additive therapy with standard treatments, such as radiotherapy and chemotherapy. The principle of cancer treatment is to eliminate only cancer cells distinguishing from normal cells. They are distinguished by visual inspection in surgical procedure. However, cellular discrimination is difficult. Although various efforts have been made to attain tumor-selective radiotherapy and chemotherapy, there remains considerable difficulty in these techniques. Hyperthermia is superior to other therapeutic techniques on this point. The blood flow is insufficient in tumors and the inadequate blood flow makes tumors more acidic due to the lactic acid buildup in the tumor tissues from lack of oxygen. In general, cells are easy to die when the environment becomes acidic, because temperature-sensitivity of cell increases. Additionally, the temperature will rise easily when the blood flow is insufficient. Moreover, cancer cells have a lower thermal resistance than normal cells. In consequence, one can eliminate cancer cells selectively by rising the local temperature at the site of tumor.

The magneto-thermo-cytolysis (or the magneto-thermoablation) is a promising technique thanks to the development of precise methods for synthesizing functionalized magnetic nanoparticles (MNPs) [1]. MNPs with functionalized surfaces, which have high specificity to a tumor tissue, are used as heating elements for hyperthermia. The process involved in the magnetic hyperthermia is based on the energy dissipation when a ferromagnetic material is placed on an external alternating magnetic field. The energy dissipation of MNPs consists of the following two effects: the Néel relaxation and the Brownian relaxation. For efficient magnetic hyperthermia, the MNPs are required to have low toxicity and a high saturation magnetization in order to minimize the doses needed for temperature increase.

In this context, iron-platinum (FePt) nanoparticle is a promising candidate because presents a high Curie temperature, high saturation magnetization, and high chemical stability [2]. Recently, a colloid-chemical synthesis technique of FePt MNPs has been developed and the FePt MNPs are regarded as one of the most likely candidates for ultrahigh-density nano-sized magnetic recording materials [2][3]. The colloid-chemically synthesized FePt MNPs have chemically disordered face-centered cubic (fcc) structure in which Fe and Pt atoms are randomly arranged and are superparamagnetic. Post-synthesis thermal annealing at a temperature over 580 °C transforms the crystalline structure from fcc to chemically ordered L10 phase. L10-phase FePt MNPs have a large magnetcrystalline anisotropy \( K = 7 \times 10^6 \text{J/m}^3 \) [4], and thus exhibit large coercivity at room temperature, even when their size is as small as several nanometers. For bio applications such as heating elements for hyperthermia, however, a superparamagnetic fcc-phase FePt MNP is also an attractive material. For this purpose, it is important to know the targeted value of MNP size, because the mean size control attaining desirable average composition and uniformity of FePt MNPs is still a big challenge. Chen et al. have synthesized FePt MNPs of average diameter with a size of up to 9 nm by precisely controlling reaction conditions, such as the kind of solvent used, the amount of capping agents, temperature, temperature rising rate, and reaction time [5]. However, in general, it is difficult to synthesize FePt MNPs of average diameter that are larger than 5 nm with uniform size and composition distributions. Here, we theoretically considered an applicability of FePt MNPs to magnetic hyperthermia comparing with iron oxide and permeon-dur MNPs, and clarified the requirements for the synthesis of FePt MNPs when one applies FePt MNPs as heating elements for hyperthermia.

II. THEORY

The energy dissipation of MNPs in an alternating magnetic field is described as [6]

\[
P = \pi \mu_0 \chi_0 H_0^2 f \frac{2\pi f \tau}{1 + (2\pi f \tau)^2}
\]

where \( \mu_0 \) is the permeability of free space, \( 4\pi \times 10^{-7} \text{T·m/A} \); \( \chi_0 \) is the equilibrium susceptibility; \( H_0 \) and \( f \) are the amplitude and
the frequency of alternating magnetic field; and $\tau$ is the effective relaxation time given by

$$\tau^{-1} = \tau_N^{-1} + \tau_B^{-1} \quad (2)$$

where $\tau_N$ and $\tau_B$ are the Néel relaxation and the Brownian relaxation time, respectively. $\tau_N$ and $\tau_B$ are written as

$$\tau_N = \frac{\sqrt{\pi}}{2} \frac{\tau_0}{\sqrt{T}} \quad (3)$$

$$\tau_B = \frac{3\eta V_H}{kT} \quad (4)$$

where $\tau_0$ is the average relaxation time in response to a thermal fluctuation; $\eta$ is the viscosity of medium; $V_H$ is the hydrodynamic volume of MNP; $k$ is the Boltzmann constant, $1.38 \times 10^{-23} \text{ J/K}$; $T$ is the temperature. Here, $\Gamma = KV_M/kT$ and $V_M$ is the volume of MNP. The MNP volume $V_M$ and the hydrodynamic volume including the ligand layer $V_H$ are written as

$$V_M = \frac{\pi D^3}{6} \quad (5)$$

$$V_H = \frac{\pi (D + 2\delta)^3}{6} \quad (6)$$

where $D$ is the diameter of MNP; $\delta$ is the ligand layer thickness. The equilibrium susceptibility $\chi_0$ is assumed to be the chord susceptibility corresponding to the Langevin equation, and expressed as

$$\chi_0 = \chi_0 \left( \coth \xi - \frac{1}{\xi} \right) \quad (7)$$

where $\xi = \mu_0 M_0 H V_M/kT$; $M_0 = \mu_0 M_0$; $H = H_0 \cos 2\pi ft$; and $\mu$ is the volume fraction of MNPs. Here, $M_0$ and $M_0$ are the domain and saturation magnetization, respectively. The initial susceptibility is given by $\chi_I = \mu_0 \mu_0 M_0 V_M/3kT$. The temperature rise is calculated as $\Delta T = P \Delta t / \rho c_p$ where $P$ and $c_p$ are the effective density and the effective specific heat calculated as $P = \phi p_1 + (1 - \phi) p_2$ and $c_p = \phi c_p + (1 - \phi) c_{p2}$, where subscripts 1 and 2 represent the MNPs and the medium, respectively.

### III. HEATING RATE OF AQUEOUS DISPERSIONS OF MNPS

Based on the above-mentioned theory, we calculated the rate of temperature rise for aqueous dispersion of monodispersed equiatomic fcc-phase FePt MNPs varying the diameter of MNP ($D$) in adiabatic condition. For comparison, we also estimated the rates of temperature rise for magnetite ($\text{Fe}_3\text{O}_4$), maghemite ($\gamma$-Fe$_2$O$_3$), permendur (FeCo) and $\text{Li}_0$-phase FePt MNPs. In Table I, physical properties of each magnetic material are shown. The magnetocrystalline anisotropy constant ($K$) of fcc-phase FePt MNPs is estimated by using the relation $K = 25kT_B V_M$, where $T_B$ denotes the blocking temperature [7]. The temperature-dependent magnetization measurements of 4-nm fcc-phase FePt particles indicated that superparamagnetic behavior was blocked at 20 to 30 K [2]. Hence, we estimated as $K \approx 2.06 \times 10^5 \text{ J/m}^3$ for fcc-phase FePt MNPs by setting $T_B = 20 \text{ K}$. The domain magnetization $M_0$ of FePt [8] and FeCo [9] MNPs are estimated by using bulk values of $M_0$. The surface dead layer effect [10] and polydispersity of MNPs are not considered in our calculations. In practice, the magnetic anisotropy may vary considerably due to the shape contributions of MNPs. For simplicity, however, the shape effect is not taken into account in the present model. It has been pointed out that hysteresis losses are important especially for magnetic single domain particles with high magnetocrystalline anisotropy [11]. However, the hysteresis losses are not considered, because we assume MNPs are superparamagnetic in this study.

Fig. 1 shows comparative heating rates for aqueous monodisperse dispersions of the various MNPs listed in Table I, assuming $\tau_0 = 10^{-9} \text{ s}$ and $\phi = 0.1$. Amplitude and frequency of applied magnetic field were fixed at 50 mT and 300 kHz. The carrier liquid is pure water in all cases. Surface ligand layer thickness is assumed to be $\delta = 1 \text{ nm}$. On these conditions, fcc- and $\text{Li}_0$-phase FePt MNPs yield the largest heating rates in the size range of $D < 20 \text{ nm}$. Most operative sizes of each MNPs, $D_{\text{max}}$, which give a maximum heating rate, are 9 nm for fcc- and $\text{Li}_0$-phase

<table>
<thead>
<tr>
<th>Material</th>
<th>$M_0$ (kA/m)</th>
<th>$K$ (kJ/m$^3$)</th>
<th>$c_p$ (J/kg°C)</th>
<th>$\rho$ (kg/m$^3$)</th>
<th>$D_{\text{max}}$ (nm)</th>
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<tbody>
<tr>
<td>Magnetite</td>
<td>446</td>
<td>9</td>
<td>670</td>
<td>5180</td>
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<tr>
<td>Maghemite</td>
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<td>746</td>
<td>6600</td>
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</tr>
<tr>
<td>FeCo</td>
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<td>1.5</td>
<td>172</td>
<td>8140</td>
<td>34</td>
</tr>
<tr>
<td>fcc-FePt</td>
<td>1140</td>
<td>206</td>
<td>327</td>
<td>15200</td>
<td>9</td>
</tr>
<tr>
<td>$\text{Li}_0$-FePt</td>
<td>1140</td>
<td>7000</td>
<td>295</td>
<td>15200</td>
<td>9</td>
</tr>
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</table>

*Estimated by $K=25kT_BV_M$, $\text{[4]}$, $\text{[15]}$, $\text{[16]}$. $^H_T0=50 \text{ mT}$ and $f=300 \text{ kHz}$.\n
FIG. 1. Comparative heating rates as a function of particle diameter for various MNPs. Filled squares and open circles represent fcc- and $\text{Li}_0$-phase FePt, respectively. Open squares and filled triangles are magnetite and maghemite, respectively. Filled circles represent FeCo MNPs. $H_0 = 50 \text{ mT}$ and $f = 300 \text{ kHz}$.\n
TABLE I

<table>
<thead>
<tr>
<th>Physical Properties and Most Operative Sizes</th>
<th>$\text{Fe}_3\text{O}_4$</th>
<th>$\gamma$-Fe$_2$O$_3$</th>
<th>FeCo</th>
<th>FePt</th>
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<td>$M_0$ (kA/m)</td>
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<td>414</td>
<td>1790</td>
<td>1140</td>
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<td>$K$ (kJ/m$^3$)</td>
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<td>$c_p$ (J/kg°C)</td>
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<td>$\rho$ (kg/m$^3$)</td>
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<tr>
<td>$D_{\text{max}}$ (nm)</td>
<td>19</td>
<td>23.5</td>
<td>34</td>
<td>9</td>
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</table>
FePt MNPs, 19 nm for magnetite, 23.5 nm for maghemite, and 34 nm for FeCo MNPs (Table I). The FeCo MNPs have the highest heating rates as shown in Fig. 1. The maghemite MNPs also have large heating rates as well as magnetite MNPs. However, the size ranges of FeCo and maghemite, where the heating is possible, are much larger than the typical size ranges of standard ferrofluids ($D = 8-10$ nm). In general, the stability of magnetic colloid becomes impaired when $D > 20$ nm due to the spontaneous magnetization. On the other hand, it is difficult to obtain independently isolated L10-phase FePt MNPs at this moment. Considering above-mentioned problems and other things such as chemical stability, we will focus on fcc FePt and magnetite MNPs hereafter.

Fig. 2(a) shows the dependence of heating rates on amplitude of applied magnetic field fixing $f = 300$ kHz. Note that $H_0$ is varied as 25, 50, and 75 mT, and only the cases of fcc FePt and magnetite MNPs are plotted. The heating rates simply increase with increasing $H_0$. In the case of fcc FePt MNPs, the increase in the heating rates is more prominent than that in the case of magnetite MNPs when $H_0$ increases. No change in $D_{\text{max}}$ is observed for both MNPs. Fig. 2(b) shows the dependence of heating rates on $f$ fixing $H_0 = 50$ mT. Note that $f$ is varied as 100, 300, and 500 kHz. The heating rates increase with increasing $f$. Unlike in the case of Fig. 2(a), the heating rates of magnetite MNPs increase with increasing $f$ much faster than those of fcc FePt MNPs. The gradual decrease in $D_{\text{max}}$ with increasing $f$ is also observed for both MNPs.

In Fig. 3, the dependences of the maximum heating rates (MHR) and $D_{\text{max}}$ plotted as a function of $f$. Filled and open squares represent MHR of fcc FePt and magnetite, respectively. Filled and open circles are $D_{\text{max}}$ of fcc FePt and magnetite, respectively.

**IV. BIOHEAT TRANSFER MODEL**

Several attempts to estimate the spatial temperature distribution in localized magnetic hyperthermia using MNPs have been reported. For example, András et al. calculated the spatial temperature distribution in breast carcinomas containing magnetic particles under external alternating magnetic field by modified heat conduction equations [17]. They compared the calculated results with in vitro measurements with muscle tissue, and found a good agreement between the calculation and the experimental
results. To estimate the temperature rise behavior in vivo, we solved the Pennes bioheat transfer equation [18] given by

$$\rho C_p \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + \rho_0 c_p \omega_0 (T_a - T) + Q_{\text{mnp}} + P \quad (8)$$

where $k \rho$ is the thermal conductivity of tissue, 0.502 W/(m·K) [19], $\rho_0$ is the density of blood, 1000 kg/m$^3$ [21]–[24]; $c_p \omega_0$ is the specific heat of blood, 4180 J/(kg·K) [21]–[24]; $\omega_0$ is the blood perfusion rate, 6.4 $\times$ 10$^{-3}$ s$^{-1}$ [21]; $T_a$ is the temperature of arterial blood, 310 K; and $Q_{\text{mnp}}$ is the metabolic heat generation, 540 W/m$^3$. The effective density $\rho$ and the effective specific heat $c_p$ of the MNP-loaded tumor are given as the volume average as mentioned above, setting $\phi = 2 \times 10^{-5}$, $\rho_2 = 1060$ kg/m$^3$ [19], [22]–[24], and $\rho_2 c_2 = 3600$ J/(kg·K) [19], [22]–[24]. By assuming a spherical tumor of 1 cm in diameter existing in the body core, we solved the one-dimensional form of (8) with the Neuman boundary conditions.

Fig. 4(a) shows the time evolution of temperature at the center of the tumor ($x = 0$) in the cases of 9-nm fcc FePt and 19-nm magnetite MNPs ($H_0 = 50$ mT and $f = 300$ kHz). The energy dissipation is $P = 3.97 \times 10^5$ W/m$^3$ for fcc FePt MNPs and $P = 1.95 \times 10^5$ W/m$^3$ for magnetite MNPs. In general, cancer cells have a higher chance of dying when the temperature is above 42.5 °C, and the rate of death drastically increases with increasing temperature [25]. Hence, fcc FePt MNPs work well while magnetite MNPs do not in these conditions. This result indicates that one can significantly reduce the doses of MNPs producing the same effect. In practice, the MNPs in tumor tissue are considered to be immobilized in cell plasma or sticking on cell membranes. Therefore, the Brown relaxation pathway is thought to be nearly irrelevant. To consider this effect, we increased the medium viscosity $\eta$ from the viscosity of water, and checked the changes in $P$ for both MNPs. In the case of magnetite MNPs, $P$ is independent of $\eta$, because the Néel relaxation dominates the relaxation process originally. On the other hand, $P$ decreases with increasing $\eta$ in the case of fcc FePt MNPs. However, $P$ becomes to be independent of $\eta$ when $\eta$ increases more than 10 times the water viscosity. In such case, the value of $P$ is 7% of original value. Even in this situation, the energy dissipation of fcc FePt MNPs is larger than that of magnetite MNPs.

Fig. 4(b) shows the steady-state temperature distributions after applying external alternating magnetic field of $H_0 = 50$ mT and $f = 300$ kHz for 600 s. The distance from the center of the tumor is represented as $x$. The interface between the tumor and normal tissue is located at $x = 5$ mm. As seen in Fig. 4(b), the range where the temperature is higher than 42.5 °C is $0 \leq x \leq 6$ mm. This indicates that the magnetic hyperthermia is highly selective for cancer treatments. Although the biocompatibility and cytotoxicity of FePt MNPs are still unclear at this moment, they are known to strongly depend on the kinds of surface capping molecules [26]. Hence, we do not elaborate on the biocompatibility and toxicity of FePt MNPs in the present paper.

V. CONCLUSION

Theoretical assessment of chemically disordered fcc-phase FePt MNPs as heating elements for magnetic hyperthermia is carried out by combining the heat generation model and the bioheat transfer equation. In consequence, fcc FePt MNPs are found to have a superior heating capability compared with other MNPs such as magnetite. Thus, significant reduction of the doses of MNPs is expected. However, one needs to synthesize larger FePt MNPs than 6 nm for their use in hyperthermia.

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REFERENCES


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