<table>
<thead>
<tr>
<th><strong>Title</strong></th>
<th>Estimation of fundamental frequency of reverberant speech by utilizing complex cepstrum analysis</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Author(s)</strong></td>
<td>Unoki, Masashi; Hosorogiya, Toshihiro</td>
</tr>
<tr>
<td><strong>Citation</strong></td>
<td>Journal of Signal Processing, 12(1): 31-44</td>
</tr>
<tr>
<td><strong>Issue Date</strong></td>
<td>2008-01</td>
</tr>
<tr>
<td><strong>Type</strong></td>
<td>Journal Article</td>
</tr>
<tr>
<td><strong>URL</strong></td>
<td><a href="http://hdl.handle.net/10119/7755">http://hdl.handle.net/10119/7755</a></td>
</tr>
<tr>
<td><strong>Description</strong></td>
<td>信号処理学会が著作権を有する。一部に対して著作権者が著作権を有するものも存在し、一部には著作権者の許可なく利用することはできません。</td>
</tr>
</tbody>
</table>
Estimation of fundamental frequency of reverberant speech by utilizing complex cepstrum analysis

Masashi Unoki and Toshihiro Hosorogiya

School of Information Science, Japan Advanced Institute of Science and Technology
1-1 Asahidai, Nomi, Ishikawa 923-1292, Japan
E-mail: {unoki, t-hosoro}@jaist.ac.jp

Abstract This paper reports comparative evaluations of twelve typical methods of estimating fundamental frequency ($F_0$) over huge speech-sound datasets in artificial reverberant environments. They involve several classic algorithms such as Cepstrum, AMDF, LPC, and modified autocorrelation algorithms. Other methods involve a few modern instantaneous amplitude- and/or frequency-based algorithms, such as STRAIGHT-TEMPO, IFHC, and PHIA. The comparative results revealed that the percentage of correct rates and SNRs of the estimated $F_0$s were reduced drastically as reverberation time increased. They also demonstrated that homomorphic (complex cepstrum) analysis and the concept of the source-filter model were relatively effective for estimating $F_0$ from reverberant speech. This paper thus proposes a new method of robustly and accurately estimating $F_0$s in reverberant environments, by utilizing the modulation transfer function (MTF) concept and the source-filter model in complex cepstrum analysis. The MTF concept is used in this method to eliminate dominant reverberant characteristics from observed reverberant speech. The source-filter model (liftering) is used to extract source information from the processed cepstrum. Finally, $F_0$s are estimated from them by using the comb-filtering method. Additive-comparative evaluation was carried out on the new approach with other typical methods. The results demonstrated that it was better than the previously reported techniques in terms of robustness and providing accurate $F_0$ estimates in reverberant environments.

Keywords: $F_0$ estimation, reverberant speech, complex cepstrum analysis, MTF concept, source-filter model

1. Introduction

The fundamental frequency ($F_0$) as well as the fundamental period ($T_0$) of speech can be utilized as significant features to represent the source information (glottal waveform or vocal-fold vibrations) of speech sounds in various speech-signal processes. These are, for example, in speech analysis/synthesis systems, automatic speech recognition (ASR) systems, and speech emphasis methods. In particular, robust and accurate $F_0$ can generally be used as a powerful cue to reduce the noise component in noisy speech and/or to remove the reverberation effect in reverberant speech. Therefore, robustly and accurately estimating the $F_0$ of target speech in real environments, which is the same as extracting the $F_0$ of noiseless speech, is a particularly important issue in these applications.

Many studies on extracting or estimating the $F_0$ of target speech have been done in the literature on speech-signal processing, and numerous methods have been proposed [1, 2, 3] over the last half-century. The traditional extraction/estimation methods can be divided into processing in the time and frequency domains, or both domains. Most of these have made use of the periodic features of speech in the time domain (zero-cross [4, 5], periodgram [6], peak-picking [4, 7], autocorrelation [4, 8], the amplitude magnitude difference function (AMDF) [9], and maximum likelihood [10]), or harmonic features in the frequency domain (comb filtering [11, 12], autocorrelation [13], sub-harmonic summation (SHS) [14], and cepstrum [15]).

The aim of all these methods has been to extract the periodicity or harmonicity of source information from observed speech. However, this still seems to be incompletely resolved because three main issues remain, i.e., (1) observability: the observed speech is an emitted sound passing through the mouth/nose so
that it is impossible to directly observe glottal vibrations from it without eliminating the effects of the vocal tract. (2) flexibility and irregularity: glottal vibrations are not complete periodic signals and the range of variations in the periods is relatively wide, and (3) robustness: the observed speech signals are affected by noise and reverberation so that the significant features for estimating $F_0$ are also smeared.

Most studies have focused on the first two issues so that they have implicitly assumed all speech signals are observed in clean environments or all observations are only noiseless speech sounds. Various methods of estimating $F_0$ have been proposed under this assumption to solve the first issue by suppressing the effects of filter characteristics (vocal tract), based on the source-filter model, from the observed speech sounds. For example, typical approaches based on this idea have been homomorphic methods of analysis [15, 16] and linear prediction (LP)-based methods [17, 18, 19]. A few examples of inverse filtering methods are lag-windowing [20] and simplified inverse filter tracking (SIFT) [21]. Center-clipping, band-limitation [22, 23], and multi-windowing [24] techniques have also been used in approaches based on the autocorrelation function.

A few approaches to precisely estimate the $F_0$ of target noiseless speech have been established (e.g., STRAIGHT-TEMPO [25] and YIN [26]) by comparing electro-glottal-graph (EGG) information. The stability of the instantaneous frequency of speech has also been used in the STRAIGHT-TEMPO method (referred to as “TEMPO” after this) to accurately estimate $F_0$s as significant features to resolve the first two issues. This method plays an important role in controlling “pitch” related features in STRAIGHT analysis/synthesis tools [27]. YIN has also been proposed which combines autocorrelation functions and AMDF to resolve these. It has been reported that both methods can be used to estimate the $F_0$ of target noiseless speech extremely precisely so that the first two issues seem to be have been resolved. However, it has not yet been clarified whether these methods can precisely estimate $F_0$ in real environments. Hence, we need to investigate the last issue for realistic applications.

It is generally known that the method of estimating $F_0$ using periodic and/or harmonic features (e.g., autocorrelation functions and comb filtering) is relatively robust against background noise, but the estimated $F_0$ is not relatively accurate [2, 28, 29]. It has also been reported that the comb-filtering-based method is more robust against background noise than the autocorrelation-based approach [29]. The cepstrum-based method is not as robust against background noise as either of these because it is composed of homomorphic analysis so that noise components are not clearly separated in the quefrency domain [29].

The time-frequency representation of speech obtained by time-frequency analysis can also adequately represent the periodic/harmonic components of speech. The instantaneous amplitude (IA) of speech signals has fine harmonic features that are robust against background noise so that the comb-filtering of instantaneous amplitude has been proposed [30] to construct a sound-segregation model. The instantaneous frequency (IF) of speech has also been used to accurately estimate $F_0$s but their stability as used in TEMPO is sensitive to noise. More robust methods using instantaneous frequency have been proposed by using bandwidth equations related to instantaneous amplitude and frequency with harmonicity [28, 31]. Other robust techniques using instantaneous amplitude and frequency-related approaches have been proposed by using periodicity and harmonicity [29]. It has been reported that these are more robust than TEMPO and can precisely estimate the $F_0$ in noisy environments.

All these methods have focused on noiseless to noisy conditions to estimate sufficiently accurate $F_0$s of target speech. Thus, methods using instantaneous amplitude and frequency or those with robust features against noise such as periodicity and harmonicity have been regarded as accurately being able to estimate $F_0$s from noisy speech. The last issue seems to be have been solved at this time; however, there have been no studies on robustness in reverberant environments.

It can easily be predicted that no typical methods will work as well and their percentage correct rates for $F_0$s will drastically be reduced as reverberation time increases. If our prediction is correct, the last issue has not yet been completely solved and needs to be considered in reverberant environments and in noisy reverberant environments. We evaluated traditional methods of estimating $F_0$ in terms of robustness and accuracy in reverberant environments to investigate this issue and discuss them in this paper. We then propose a method of estimating $F_0$ from reverberant speech without measuring impulse response in room acoustics (i.e., blind method of estimating $F_0$) by taking the characteristics of reverberation into consideration.

This paper is organized as follows. Section 2 describes the mathematical setup and then defines the problem of estimating $F_0$ from reverberant speech. We discuss our evaluations of most typical methods of estimating $F_0$ in reverberant environments in Section 3 and investigations into what the best model is. Section 4 introduces complex cepstrum analysis and investigates what the significant features for robust estimates are. We then introduce the model concept (complex cepstrum analysis, the modulation transfer function (MTF) concept, and source-filter model). We finally propose a method of estimating $F_0$ in reverberant environments. We discuss our evaluations of the proposed method in Section 5 by comparing it with
other methods using the same simulations. Section 6 gives our conclusions and perspective regarding future work.

2. Mathematical setup

2.1 Signal representation and STFT

A time-varying harmonic signal, $x(t)$, can be represented as the analytic signal:

$$x(t) = \sum_{k \in K} a_k(t) \exp(j\omega_k(t)t + \theta_k(t))$$

(1)

where $a_k(t)$ is the instantaneous amplitude and $\theta_k(t)$ is the phase. Here, $k$ denotes the harmonic index and $K$ is the number of harmonics so that $\omega_k(t)$ can be expressed as $2\pi k F_0(t)$. Fundamental frequency $F_0(t)$ is an instantaneous frequency so that this should be extracted from $x(t)$ using instantaneous cues.

The short-term Fourier transform (STFT) is usually used [32] to analyze $x(t)$ in any given short-term segment (windowing processing): 

$$X(\omega, \tau) = \int x(t)w(t-\tau)e^{-j\omega t}dt$$

(2)

$$A(\omega, \tau) = |X(\omega, \tau)|$$

(3)

$$\phi(\omega, \tau) = \text{arctan} \left( \frac{\text{Im}[X(\omega, \tau)]}{\text{Re}[X(\omega, \tau)]} \right)$$

(4)

where $w(t)$ is a window function and a short-term signal, $x(t, \tau)$, is defined as $w(t-\tau)x(t)$ for mathematical convenience. $A(\omega, \tau)$ is the amplitude spectrum and $\phi(\omega, \tau)$ is the phase spectrum of $X(\omega, \tau)$.

The task of extracting/estimating fundamental frequency $F_0(t)$ in this formulation is, therefore, to estimate the $F_0$ in each short-term segment using the harmonicity of $X(\omega, \tau)$ or to estimate segmental $T_0 = 1/F_0$ by using the periodicity of $x(t, \tau)$. Thus, traditional methods based on waveform processing (e.g., zero-cross [4, 5], periodograms [6], peak-picking [4, 7], autocorrelation [4, 8], AMDF [9], maximum likelihood [10], STFT-based processes, and sub-harmonic summation (SHS) [14]) estimate $F_0(t)$ from $x(t, \tau)$ or $X(\omega, \tau)$ by using periodicity or harmonicity.

2.2 Source-filter model

The source-filter model is a well-known concept to separately represent the glottal (source information) and vocal-tract (filter information) characteristics for speech production. Based on this concept, the observed clean speech signal, $x(t)$, can be represented as

$$x(t) = e(t) * v_r(t)$$

(6)

where $e(t)$ is the source signal related to glottal information and $v_r(t)$ is the impulse response of the filter related to the vocal tract at time $\tau$. The asterisk “*” denotes convolution. Note that the emission effect has been omitted from this formulation. Thus, Eq. (2) can also be represented as

$$X(\omega, \tau) = S(\omega, \tau) \cdot V(\omega, \tau)$$

(7)

where $S(\omega, \tau)$ is the STFT of $s(t, \tau) = w(t-\tau)e(t)$ and $V(\omega, \tau)$ is that of $v(t, \tau) = v_r(t)$. $V(\omega, \tau)$ represents filter characteristics so that the separation effect of $V(\omega, \tau)$ is usually used to estimate $F_0(t)$ from $X(\omega, \tau)$. Some traditional methods of estimation are inverse filtering $V^{-1}(\omega, \tau)$ [21], whitening of $X(\omega, \tau)$ using $|V(\omega, \tau)|$ (or lag windowing) [20], and subtraction on logarithmic processing $\log X(\omega, \tau) = \log S(\omega, \tau) + \log V(\omega, \tau)$ [22, 23].

The linear prediction (LP) method is also one of the most powerful techniques of analyzing speech signals. LP coefficients have filter characteristics (all-pole type) and the LP residue has source information. The LP coefficients of $x(t, \tau)$ can thus be used as inverse filtering $V^{-1}(\omega, \tau)$ in the source-filter model [17, 21]. The LP residue can also be used as a short-term signal $s(t, \tau)$ [19]. Waveform processing and AMDF have also been incorporated [18].

2.3 Cepstrum representation

Cepstrum is also a well-known method of homomorphic analysis. The complex cepstrum of $X(\omega, \tau)$ in Eq. (2) can be represented as

$$C(q, \tau) = F^{-1}[\log \{|X(\omega, \tau)| \exp(j\phi(\omega, \tau))\}]$$

$$= F^{-1}[\log A(\omega, \tau)] + F^{-1}[j\phi(\omega, \tau)]$$

$$= C_A(q, \tau) + C_\phi(q, \tau)$$

(8)

where $F^{-1}[\cdot]$ is the Fourier inverse transform, $C_A(q, \tau)$ is the amplitude cepstrum, $C_\phi(q, \tau)$ is the phase cepstrum of $C(q, \tau)$, and $q$ denotes the quefrency (time domain). The complex cepstrum of $X(\omega, \tau)$ in Eq. (7)
can also be represented as

\[
C(q, \tau) = F^{-1} \log S(\omega, \tau) + F^{-1} \log V(\omega, \tau)
\]

\[
= C_{src}(q, \tau) + C_{flt}(q, \tau)
\]

where \(C_{src}(q, \tau)\) is the complex cepstrum of source signal \(S(\omega, \tau)\) and \(C_{flt}(q, \tau)\) is that of filter \(V(\omega, \tau)\).

The amplitude cepstrum, \(C_A(q, \tau)\), is generally used in the traditional method so that \(C_{A,src}(q, \tau)\) and \(C_{A,flt}(q, \tau)\) are separately used for estimating \(F_0(t)\) from \(C_A(q, \tau)\). Figure 1 outlines the concept underlying the source-filter model in the quefrency domain. \(C_{A,flt}(q, \tau)\) represents the dominant spectrum envelope of \(X(\omega, \tau)\) (lower Fourier component in quefrency domain) so that they are compactly located in the lower quefrency. In contrast, \(C_{A,src}(q, \tau)\) represents the dominant fine structure of \(X(\omega, \tau)\) so that they are compactly located in the higher quefrency domain. Therefore, the task of estimating \(F_0\) with this concept is to find the dominant quefrency from \(C_{A,src}(q, \tau)\) or to detect periodicity or harmonicity from \(C_{A,src}(q, \tau)\) by eliminating \(C_{A,flt}(q, \tau)\) from \(C_A(q, \tau)\). The last processing is referred to as “lifting”. Typical approaches are Noll’s original method \([15]\) and his clip-processing \([16]\).

2.4 Problem with estimating \(F_0\)

The task of estimating \(F_0\) in reverberant environments is to extract \(F_0(t)\) from reverberant speech signal \(y(t)\) or respective STFT \(Y(\omega, \tau)\):

\[
y(t) = x(t) * h(t) = e(t) * v_r(t) * h(t)
\]

\[
Y(\omega, \tau) = S(\omega, \tau)V(\omega, \tau)H(\omega, \tau)
\]

where \(h(t)\) is the impulse response and \(H(\omega, \tau)\) is the STFT of \(h(t)\) in room acoustics (reverberation). Note that, \(H(\omega, \tau)\) is actually required to present all characteristics \(H(\omega) = H(\omega, \tau)\) by using a long-term Fourier transform (LTFT) so that the length of analysis (at each \(\tau\)) should be more than the reverberation time.

The task of estimating \(F_0\) in reverberant environments is thus to select periodicity and harmonicity from the convolved source signal, \(e(t)\), while that in noisy environments is to select them from the noisy (additive) source signal, \(e(t)\). If \(h(t)\) is simplified echo or a minimum phase impulse response, the cepstrum-based method can be used to adequately estimate \(F_0\) from the reverberant speech signal, \(y(t)\), because homomorphic analysis is a powerful tool for dealing with simplified echoes. Realistic impulse responses in room acoustics generally have non-minimum phase characteristics and we therefore predicted that estimating \(F_0\) robustly and accurately would be more difficult than in noisy environments.

3. Evaluation of typical methods

3.1 Typical methods of estimating \(F_0\)

Many methods of estimating \(F_0\) have been proposed in the literature on speech signal processing, as described in Section 1. The most comprehensive review remains that by Hess (1983) \([1]\) and more recent reviews are those by Hess (1992) and Cheveigne and Kawahara (2001) \([2, 3]\). A few examples of recent approaches are instantaneous-amplitude \([30]\), instantaneous-frequency \([28, 31]\), and fundamental wave-filtering \([33]\). There are also comparative evaluations in Atake et al.’s (2000), Ishimoto et al.’s (2001), and Nakatani and Iriyo (2004) \([2, 3, 28, 29, 31]\).

We evaluated twelve typical methods to investigate how robust estimates of \(F_0\) were in reverberant environments: ACMWL (AutoCorrelation through Multiple Window-Length) \([24]\), AMDF \([9]\), STFT-ACorrLog (AutoCorrelation of Log-amplitude spectrum on STFT) \([22, 23, 13]\), STFT-ACorrLag (Lag-windowing on STFT) \([20]\), STFT-Comb (Comb filtering on STFT) \([11, 12]\), SHS \([14]\), Cepstrum \([15]\), LPC-residue \([19]\), VFHFF (Voice Fundamental Wave Filtering (Feed-forward type)) \([33]\), TEMPO \([25]\), IFHC (Instantaneous Frequency of Harmonic Components) \([28]\), and PHIA (Periodicity/Harmonicity using Instantaneous Amplitude) \([29]\). Although other methods have been proposed, we choose these twelve because they are commonly used in comparative evaluations and the others are just modifications or heavy revisions of them.

The characteristics, parameters, and detailed conditions on these algorithms that we used in this comparative evaluation are listed in Table 1. TEMPO was used as a complete original version. As the other methods implemented by the researchers were based on their original research, they were the first or original versions. Several parameters were set to obtain appropriate results based on preliminary simulations. For more detailed information on their technical implementations and skill levels, please refer to their original papers.

3.2 Sound dataset and evaluation measures

The sound dataset we used in this evaluation was the speech database on simultaneous recordings of speech and EGG by Atake et al. \([28]\). This dataset consisted of 30 short Japanese sentences uttered by 14 males and 14 females with voiced-unvoiced labels (total of 840 utterances, sampling frequency of 16 kHz, and quantization of 16-bits).

The reverberant speech sentences we used were created by convolving the original signals, \(x(t)\), with the following reverberant impulse responses, \(h(t)\), as a
function of the reverberation time.

\[ h(t) = a \exp \left( \frac{-6.9t}{T_R} \right) n(t) \]  

(12)

where the "a" is a gain factor as the normalized power of \( h(t) \), \( T_R \) is reverberation time, and \( n(t) \) is white noise. This is the well-known stochastic-approximated impulse response in room acoustics reported by Schroeder [34, 35], in which the response has an envelope of exponential decay and is a white noise carrier. This formulation for the impulse response has been used in the study of speech intelligibility in room acoustics [36] as general artificial reverberation and thus has non-minimum phase components [34, 35]. Six reverberation conditions (\( T_R = 0.0, 0.1, 0.3, 0.5, 1.0, \) and 2.0 s) were used in this study. There were a total of 5,040 stimuli.

Fine \( F_0 \) error and gross \( F_0 \) error within the voiced section have been used as measures for some comparative evaluations in noisy environments [2, 28, 29, 31]. These have concentrated on error analysis. Since we concentrated on evaluating robustness and the accuracy of \( F_0 \) estimates, we used two similar measures for evaluation but not the same measures. The first was the percent correct rate (\( \% \)) and the second was SNR (in dB).

\[ \text{Correct rate}_E = \frac{N_{F_0,\text{Est}}(E)}{N_{F_0,\text{Ref}}} \times 100 \]  

(14)

\[ \text{SNR} = 20 \log_{10} \frac{\int (F_{0,\text{Ref}}(t) - F_{0,\text{Est}}(t))^2 dt}{\int F_{0,\text{Ref}}(t)^2 dt} \]  

(15)

where \( F_{0,\text{Ref}}(t) \) and \( F_{0,\text{Est}}(t) \) are reference \( F_0 \) and estimated \( F_0 \), and this integral is done in the voiced section (\( t \)). \( N_{F_0,\text{Est}}(E) \) is the size of the correct region that satisfies

\[ \frac{|F_{0,\text{Ref}}(t) - F_{0,\text{Est}}(t)|}{F_{0,\text{Ref}}(t)} \leq E \]  

(\( \% \))

within voiced section (\( t \)) where \( E \) is the error margin (\( \% \)). \( N_{F_0,\text{Ref}}(E) \) is the size of region \( F_{0,\text{Ref}}(t) \) in the voiced section at the error margin \( E \). In this paper, the \( F_0 \) estimated by TEMPO from the EGG signal is used as the correct \( F_0 \) (reference \( F_0 \), \( F_{0,\text{Ref}}(t) \)). \( F_{0,\text{Est}}(t) \) was used to estimate \( F_0 \) with the twelve methods from reverberant speech signals. Two values for \( E \) (error margins of 5% and 10%) were used in the percent correct rate.

Since gross \( F_0 \) error is the ratio of the number of frames giving “incorrect” \( F_0 \) values to the total number of frames, the percent correct rate approximately indicates gross \( F_0 \) error. Since fine \( F_0 \) error is the normalized room mean square error between \( F_{0,\text{Ref}}(t) \) and \( F_{0,\text{Est}}(t) \), SNR indicates a similar measure in dB.

3.3 Results

Figure 2 plots the results of comparative evaluations for the twelve typical methods of estimating \( F_0 \) from reverberant speech as a function of the reverberation time, \( T_R \). The left panels (a), (c), and (e) plot the results for the first six methods and the right panels (b), (d), and (f) plot them for the last six. The top panel plots the percent correct rates (expressed as percentages) for \( F_0 \) estimates within an error margin of 5% and the middle panel plots these within

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>domain</th>
<th>Features</th>
<th>Parameter setting</th>
</tr>
</thead>
<tbody>
<tr>
<td>ACSWLP [24]</td>
<td>time</td>
<td>( x(t, \tau) )</td>
<td>Window candidates of nine (15 to 60-ms in 5-ms steps)</td>
</tr>
<tr>
<td>AMDF [9]</td>
<td>time</td>
<td>( x(t, \tau) )</td>
<td>40-ms window, 2-ms shift</td>
</tr>
<tr>
<td>STFT</td>
<td>freq.</td>
<td>( \log</td>
<td>X(\omega, \tau)</td>
</tr>
<tr>
<td>auto-corr. [22, 23, 13]</td>
<td>freq.</td>
<td>(</td>
<td>S(\omega, \tau)</td>
</tr>
<tr>
<td>Lag windowing [20]</td>
<td>freq.</td>
<td>(</td>
<td>X(\omega, \tau)</td>
</tr>
<tr>
<td>Comb filtering [11, 12]</td>
<td>freq.</td>
<td>( \log</td>
<td>X(\omega, \tau)</td>
</tr>
<tr>
<td>SHS [14]</td>
<td>freq.</td>
<td>( C_A(q, \tau) )</td>
<td>40-ms window length, 5-ms shift, 3-ms liftering,</td>
</tr>
<tr>
<td>Cepstrum [15]</td>
<td>quef.</td>
<td>( \text{Instant. Amp. (IA)} )</td>
<td>40-ms window, 2-ms shift, 3-ms liftering,</td>
</tr>
<tr>
<td>LPC Residue [19]</td>
<td>time</td>
<td>( s(t, \tau) )</td>
<td>Noll’s method (( h_w = 0.54 + 0.46 \cos(2\pi f/600) ))</td>
</tr>
<tr>
<td>( F_0 ) filtering [33]</td>
<td>time</td>
<td>( s(t, \tau) )</td>
<td>40-ms window, 2-ms shift, LP order of 12, 1/4 down-sampling</td>
</tr>
<tr>
<td>TEMPO [25]</td>
<td>freq.</td>
<td>( \text{Harmonicity of IFs} )</td>
<td>80-ms window, 2-ms shift, 1/4 down-sampling, averaged-clipping,</td>
</tr>
<tr>
<td>IFHC [28]</td>
<td>freq.</td>
<td>Fixed point analysis on Instant. freq. (IF)</td>
<td>1.5 kHz band-limitation, “Non-selfsupport mode”,</td>
</tr>
<tr>
<td>PHIA [29]</td>
<td>time/ freq.</td>
<td>( \text{Instant. Amp. (IA)} ) &amp; ( \text{Cepstrum and Dempster’s law} )</td>
<td>1-ms ( F_0 ) shift length, ( \text{nev} = 24 ), Heuristic factor: “on”</td>
</tr>
</tbody>
</table>

(1) Hanning windowing function was used in STFT-based processing.
(2) Lower limits of estimated \( F_0 \) were set at 60 Hz and higher were set at 800 Hz.
Fig. 2  Estimation results: (a)–(b) percent correct rate within error margin of 5 %, (c)–(d) percent correct rate within error margin of 10 %, and (e)–(f) SNR (s: original, n: error between original and estimated $F_0$) of $F_0$ estimates from reverberant speech using twelve typical methods as function of reverberation time, $T_R$. 
an error margin of 10%. The bottom panel plots the SNRs. The correct rates and SNRs of all 12 methods are drastically reduced as the reverberation time increases. The correct rates within the 5% error margin for all methods were less than 50% and the SNRs were less than about 15 dB, especially when reverberation time $T_R$ was 2.0 s. Moreover, the correct rates within the 10% error margin as an approximate evaluation were also less than 70%. We hence concluded that none of these methods worked as well as robust and accurate $F_0$ estimates and they had drawbacks in estimating $F_0$ from reverberant speech.

However, we found a few clues in doing this evaluation for improving these methods. We can see from Fig. 2 that the cepstrum method is the most accurate excluding the clean condition ($T_R = 0.0$). Cepstrum analysis is homomorphic and this can deal with convolution processing as additive (subtractive) processing. Although the impulse responses we used in evaluations were not minimum-phase characteristics, the cepstrum method seemed to reduce the effect of reverberation for estimating $F_0$ since this can treat a direct sound and a reflected sound as the same signal. Therefore, the cepstrum method has the possibility of estimating $F_0$ from reverberant speech if it is not affected too much by reverberation. The comb-filtering method is slightly more robust against reverberation as we can see from Figs. 2(c) and (e). Maximization method is slightly more robust against reverberation.

We did a preliminary investigation into which component, $C_{H,\text{min}}(q, \tau)$ or $C_{H,\text{all}}(q, \tau)$, most affected dealing with $C_{\text{src}}(q, \tau)$ for estimating $F_0$, using Eq. (19). Figure 3 shows the process of estimating one of the reverberant speech signals (/Tokushima-To-Iebara-Awa-Odori-Ga-Yuumei-Desu/, female speaker, reverberation time $T_R$ of 2.0 s) we used in the evaluations. Speech signals ($x(t)$ and reverberant $y(t)$) are shown in Figs. 3(a) and (b). The reference $F_0$ ($F_{0,\text{Ref}}(t)$) by TEMPO from the EGG signal) and the $F_0$ ($F_{0,\text{Est}}(t)$) estimated by the cepstrum method from $y(t)$ correspond to the dashed and solid lines in Fig. 3(c). Note that $F_{0,\text{Ref}}(t)$ obtained by TEMPO are completely within the voiced part because TEMPO has an Unvoiced/Voiced (U/V) decision. As can be seen, the estimated $F_0$ was not close to the reference in the voiced part. This method, however, can be used to accurately estimate $F_0$ from $y(t)$ by eliminating the effect of $h(t)$ from $y(t)$ on the complex cepstrum in the long-term Fourier transform, as plotted in Fig. 3(d). At the same time, two comparative $F_0$s were obtained as plotted in Figs. 3(e) and (f) by estimating $F_0$ from $y(t)$ by eliminating minimum phase or the all-pass phase component from $y(t)$.

The all-pass phase component of the reverberant with periodicity/harmonicity of source information as a filter and the reverberation characteristics are eliminated. It is too difficult only to deal with $C_{\text{src}}(q, \tau)$ in this estimation task, without measuring $h(t)$ or $C_H(q, \tau)$ (i.e., blind $F_0$ estimation). In addition, long-term $C_H(q, \tau)$, in which the length of analysis is more than the reverberation time, is needed to accurately extract $C_{\text{src}}(q, \tau)$.

Let us overview the results in Subsection 3.3 by reconsidering the complex cepstrum representation of reverberant speech $y(t)$. From Eqs. (9)-(11), the complex cepstrum of $y(t)$ can be represented as

$$C_H(q, \tau) = C_{\text{src}}(q, \tau) + C_{\text{flt}}(q, \tau) + C_{\text{H}}(q, \tau)$$

(16)

where $C_{\text{H}}(q, \tau)$ is the complex cepstrum of the reverberant impulse response, $h(t)$. These cepstra can also be represented as all amplitude and phase cepstra (denoted by subscripts “A” and “φ”).

Complex cepstrum analysis, on the other hand, is usually used to separate minimum and non-minimum phase characteristics. The complex cepstrum, $C(q, \tau)$, can also be separately represented as

$$C(q, \tau) = C_{\text{min}}(\omega, \tau) + C_{\text{all}}(\omega, \tau)$$

$$= C_{\text{A, min}}(q, \tau) + C_{\text{φ, min}}(q, \tau)$$

$$+ C_{\text{A, all}}(q, \tau) + C_{\text{φ, all}}(q, \tau)$$

(17)

where the subscripts “min” and “all” indicate minimum and non-minimum phase characteristics. Here, respective spectra can be represented as

$$X(\omega, \tau) = X_{\text{min}}(\omega, \tau) \cdot X_{\text{all}}(\omega, \tau)$$

$$= |X_{\text{min}}(\omega, \tau)| \exp(j\phi_{\text{min}}(\omega, \tau))$$

$$\times |X_{\text{all}}(\omega, \tau)| \exp(j\phi_{\text{all}}(\omega, \tau))$$

(18)

where $|X_{\text{all}}(\omega, \tau)| = 1$ and $C_{\text{A, all}}(q, \tau) = 0$. Hence, $C_Y(q, \tau)$ can be separately represented as

$$C_{Y,\text{A, min}}(q, \tau) + C_{Y,\text{φ, min}}(q, \tau) + C_{Y,\text{φ, all}}(q, \tau)$$

$$= C_{\text{src},\text{A, min}}(q, \tau) + C_{\text{src,φ, min}}(q, \tau) + C_{\text{src,φ, all}}(q, \tau)$$

$$+ C_{\text{flt, A, min}}(q, \tau) + C_{\text{flt, φ, min}}(q, \tau) + C_{\text{flt, φ, all}}(q, \tau)$$

$$+ C_{\text{H, A, min}}(q, \tau) + C_{\text{H,φ, min}}(q, \tau) + C_{\text{H,φ, all}}(q, \tau)$$

(19)

Note that the amplitude cepstrum of all-pass phase characteristics has been omitted from this equation.
paper, the same trends were observed. Hence, we concluded that eliminating the all-pass phase characteristics of \( h(t) \) would enable effective estimates of \( F_0 \) from reverberant speech \( y(t) \). In addition, the cepstrum method with the all-pass component eliminated raised the possibility of achieving robust and accurate estimates of \( F_0 \) since we knew homomorphic analysis could easily deal with minimum phase characteristics such as simplified echoes.

4.2 Estimates of \( h(t) \) based on MTF concept

The MTF concept was proposed by Houtgast and Steeneken [36] to account for the relation between the transfer function of frequency in an enclosure in terms of the envelopes of input and output signals (\( x(t) \) and \( y(t) \)), and characteristics of the enclosure such as reverberation. This concept was introduced as a measure in room acoustics to assess what effect enclosure had on the intelligibility of speech [36]. The complex modulation transfer function, \( m(\omega) \), is defined as

\[
m(\omega) = \frac{\int_0^\infty h(t)^2 \exp(j\omega t) dt}{\int_0^\infty h(t)^2 dt}
\]  

where \( h(t) \) is the impulse response of the room acoustics and \( \omega \) is the radian frequency. This equation means the Fourier transform of the squared impulse response is divided by its total energy.

When reverberant impulse response \( h(t) \) as defined in Eq. (12) is substituted into the equation above, the MTF, \( m(\omega) \), can be obtained as

\[
m(\omega) = |m(\omega)| = \left[ 1 + \left( \frac{\omega T_R}{13.8} \right)^2 \right]^{-1/2}
\]  

where \( T_R \) is the reverberation time, i.e., the time required for the power of \( h(t) \) to decay by 60 dB [36]. Figure 4 plots the MTF, \( m(\omega) \), as a function of the modulation frequency, \( F_m \), (i.e., the dominant frequency in the temporal envelope). These theoretical curves were calculated by substituting five reverberation times (\( T_R = 0.1, 0.3, 0.5, 1.0, \) and 2.0 s) and \( \omega = 2\pi F_m \) into Eq. (21). Here, \( m(\omega) \) can also be regarded as the modulation index with respect to \( F_m \). These curves reveal how much the modulation index of the envelope will be reduced from 1.0 to 0.0 depending on \( T_R \) at a specific \( F_m \). In other words, \( T_R \) can be predicted from a specific \( m(2\pi F_m) \) at a specific \( F_m \). Therefore, the temporal envelope of the reverberant impulse response, \( a\exp(-6.9t/T_R) \), can also be predicted using \( T_R \) and the “a” in Eq. (13).

Based on the MTF concept, we can establish how much reverberation affects a reduction in \( m(\omega) \) and we can then predict the characteristics of room acoustics (\( T_R \)) using inverse MTF. MTF-based power-envelope inverse-filtering methods, which have aimed at restoring the reduced MTF in the temporal envelope of the
signals, have been proposed by the present authors [37, 38]. A technique of predicting $T_R$ using the inverse MTF from the temporal envelope of observed signal $y(t)$ has also been proposed [37, 38]; this was used as a constraint for deriving the optimal restoration of the power envelope for the original signal. This is because the MTFs of a timing point where the negative area is determined from a timing point where the negative area becomes a cepstral shape of exponential decay with respect to qu frency (dominant at lower frequencies).

In contrast, although it is difficult to obtain a complete value with regard to phase cepstrum $C_{H,\phi}(q, \tau)$, long-term $C_{H,\phi,\text{all}}(q, \tau)$ can be estimated from them by using Eqs. (17) and (19). As explained in Sec. 4.1, using estimated $C_{H,\phi,\text{all}}(q, \tau)$ from $h(t)$ to eliminate the all-pass phase component from reverberant speech $\hat{y}(t)$ on the basis of LTFT should be done to estimate $F_0$. Although the estimated $C_{H,\text{A,\text{min}}}(q, \tau)$ can also be canceled out in Eq. (19) on LTFT, the elimination of minimum-phase characteristics in Eq. (19) on LTFT is not as effective for eliminating all-pass phase characteristics so that this has not been used in this paper. The short-term $C_{H,\text{A,\text{min}}}(q, \tau)$ and $C_{H,\phi,\text{min}}(q, \tau)$ to be canceled out in Eq. (19) on STFT will be considered in the next section.

4.3 Lifting on complex cepstrum

$C_{H,\phi,\text{all}}(q, \tau)$ is canceled out in Eq. (19) on LTFT as explained in the previous section, so that the remaining terms are $C_{\text{Hf}}(q, \tau)$ and $C_{H,\text{min}}(q, \tau)$ to extract $C_{\text{src}}(q, \tau)$. Complex cepstrum analysis and the source-filter model are used to cancel out the remaining terms in Eq. (19) on STFT to take the best advantage of homomorphic processing.

There is a Hilbert transform relationship between $C_{\text{A,\text{min}}}(q, \tau)$ and $C_{\phi,\text{min}}(q, \tau)$, and the latter has the same characteristics in the positive qu frency domain based on the minimum phase characteristics. However, short-term $C_{H,\text{A,\text{min}}}(q, \tau)$ and $C_{H,\phi,\text{min}}(q, \tau)$ are not the same as the long-term versions when STFT analysis is shorter than the reverberation time. However, amplitude cepstrum $C_{H,\text{min}}(q, \tau)$ in the lower qu frency parts is generally larger than that in the higher parts and this exponentially attenuates as the qu frency increases. Therefore, the minimum phase characteristics, $C_{H,\text{min}}(q, \tau)$, can be assumed to concentrate on the lower qu frency parts.

The cepstrum components of the source characteristics are separately concentrated on the higher qu frency parts and those of the filter are separately concentrated on the lower based on the advantages of the source-filter model, as shown in Fig. 1. Therefore, if a component on the low qu frency part can only be removed by lifting, the filter characteristics as well as the dominant components of the minimum-phase characteristics of reverberation can be canceled out in Eq. (19). Thus, the following lifter, $l(q)$, is used in this paper to cancel them out in Eq. (19).

$$l(q) = \begin{cases} 0, & q \leq q_{\text{if}} \\ 1, & q > q_{\text{if}} \end{cases}$$

where $q_{\text{if}} = 1.25$ ms. This means the upper limit for estimated $F_0$ is 800 Hz.
Liftering based on source-filter model

Elimination $C_{\text{src}}(q)$ from $C_{\text{r}}(q)$

LTFT $\log X_{\text{src}}(\omega, t)$

Sort-term Fourier transform (STFT)

CCA

Comb filtering

F0 estimation

Fundamental frequency

Reverberant speech $y(t)$

Long-term Fourier transform (LTFT)

$Y(\omega)$

$T_R$ estimation

Estimation of MTF based imp. response

Inversed LTFT

$C_{\text{r}}(q)$

$C_{\text{r}}(q)$

Fig. 5 Algorithm for proposed method

4.4 Proposed method of estimating $F_0$

The algorithm for estimating $F_0$ based on complex cepstrum analysis, the MTF concept, and the source-filter model are explained by Fig. 5. This method is composed of three main processes: (1) estimating the MTF-based reverberation impulse responses and eliminating them from reverberant speech, (2) extracting $X_{\text{src}}(\omega, \tau)$ from the processed reverberant speech by using liftering on the complex cepstrum based on the source-filter model, and (3) estimating $F_0$ from them by using a final decision block.

Comb filtering was employed in the final two blocks in Fig. 5. As these are commonly used in classical methods of estimation, such as in comb-filtering and autocorrelation functions, they can be replaced by the autocorrelation function. In addition, since the proposed method treats a complex cepstrum, the restored short-term waveform $s(t, \tau)$ from $C_{\text{src}}(q, \tau)$ can be used to estimate $F_0$ with the autocorrelation function and/or AMDF. As the aim of this paper was to propose a model concept for robustly estimating $F_0$ in reverberant environments, these kinds of considerations with regard to modifications in processing are beyond the scope of this paper.

5. Evaluation of proposed method

5.1 Method

We evaluated the proposed method with (labeled “Proposed(Est)”) and without (labeled “Proposed(Org)”) $T_R$ estimates by using the same procedure and sound dataset described in Section 3. With and without comparisons of the proposed method were done to find out how accurate the $T_R$ estimates were. We compared them with TEMPO, the cepstrum method, and a modified complex cepstrum method based on the source-filter model (labeled “SrcFlt”). The SrcFlt method was used to find out how effectively $C_{R,0,\text{all}}(q, \tau)$ was eliminated on the LTFT with the proposed method.

5.2 Results and discussion

Figure 6 plots the results for the comparative evaluations. The correct rates within error margins of 5 % and 10 % for the proposed and the other methods are plotted in Figs. 6(a) and (b). Their SNRs are plotted in Fig. 6(c). The results for the cepstrum method indicate the baselines in the evaluations while those for TEMPO (dashed-line) indicate the lower limits.

Although the overall accuracy of $F_0$ estimates tended to be reduced as reverberation time increased, about a 10 % improvement in the correct rates and about a 5 dB improvement in the SNR could be obtained with the new method. There are fewer differences in the results for both the proposed methods with and without $T_R$ estimates. This means the $T_R$ estimates can work as well. Since a correct rate of 60 % within an error margin of 5 %, a correct rate of 75 % within an error margin of 10 %, and an SNR of 17 dB at $T_R = 2.0$ s were achieved with the method we propose, we concluded that MTF-based impulse responses can be precisely estimated by utilizing $T_R$ estimates. For example, the results for extracting $F_0$ at $T_R = 2.0$ with the proposed method, with and without $T_R$ estimates, from the same reverberant speech (Fig. 3(b)) are plotted in Figs. 6(d) and (e).

The SrcFlt method results indicate a slight improvement (about 3 % in the correct rate) to that with the cepstrum method. In contrast, there were about 7 % and 5 dB improvements in the percent correct rate and in the SNR by using the new method. We
concluded that the use of complex cepstrum analysis with regard to non-minimum phase characteristics effectively enabled $F_0$ to be estimated in reverberant environments.

As shown in Figs. 3(b), 6(d), and 6(e), most $F_0$-estimation methods including the proposed method, which does not have the U/V decision output of redundant information in the unvoiced and silent sections, while TEMPO does. An important issue is how to determine the U/V decision rules for applications of speech-signal processing in our next stage of research. This issue should be able to be resolved by incorporating power discrimination such as that used in TEMPO with the U/V decision rules, but this is beyond the scope of this paper.

6. Conclusion and Future Perspectives

We evaluated the robustness and accuracy of twelve typical methods of estimating $F_0$ (i.e., classic ACMWL, AMDF, STFT-based, cepstrum, LPC, and SHS algorithms, and modern IFHC, PHIA, and TEMPO algorithms) in artificial reverberant environments using huge speech datasets. The results revealed that none of these methods could accurately estimate $F_0$ in reverberant environments and that their accuracies drastically decreased as reverberation time increased. The results also demonstrated that the best method was cepstrum-based and that the worst was the instantaneous frequency-based model. We found that periodicity and/or harmonicity on the complex cepstrum effectively enabled $F_0$ to be estimated in reverberant environments.

We proposed a robust and accurate method of estimating $F_0$ that was based on the source-filter model concept and the MTF concept in complex cepstrum analysis. This method included (1) eliminating the dominant reverberation effect from observed speech by estimating MTF-based reverberant impulse responses and (2) extracting source information from them by subtracting the remaining cepstrum related to filter characteristics and the remaining reverberation through liftering. We demonstrated that our new method is robust against reverberation and can accurately estimate $F_0$ from observed reverberant speech, using the same comparative evaluations.

Additional improvements may be possible by modifying the $F_0$ determination block. Further evaluations using real reverberant impulse responses in room acoustics are required for real applications. Extensional improvements may be possible by incorporating the proposed method into the U/V decision rules and by considering the robustness of the new method in both noisy and reverberant environments, but these are beyond the scope of this paper.

In future work, we hope to incorporate our new robust and accurate approach to estimate $F_0$ into the MTF-based process of speech dereverberation [39, 40] and then to improve them so that they can become a more complete blind-dereverberation method. This is because the current method, which consists of MTF-based power-envelope inverse filtering and carrier restoration using $F_0$ information can dereverberate reverberant speech in power envelopes as well as in resynthesized waveforms, assuming that $F_0$ can be accurately estimated. As mentioned in the Introduction, robust and accurate $F_0$ is a significant feature of our new method so that it should be able to contribute to resolving the problems we previously experienced with speech dereverberation [39, 40].

7. Acknowledgments

This work was supported by a Grant-in-Aid for Scientific Research from the Ministry of Education, Culture, Sports, Science, and Technology of Japan (No. 18680017). It was also partially supported by the Strategic Information and Communications R&D Promotion ProgrammE (SCOPE) (071705001) of the Ministry of Internal Affairs and Communications (MIC), Japan.

References

Fig. 6 Evaluation results: (a) percent correct rate within error margin of 5%, (b) percent correct rate within error margin of 10%, (c) SNR of $F_0$ estimates from reverberant speech using proposed method, and examples of extracted $F_0$ using proposed model (d) without $T_R$ estimation and (e) with $T_R$ estimation.


[20] H. Singer and S. Sagayama: Pitch dependent phone mod-
[21] J. D. Markel: The SIFT algorithm for fundamental fre-
[22] N. Kunieda, T. Shimamura and J. Suzuki: Pitch extrac-
tion by using autocorrelation function on the log spec-
[23] H. Kobayashi and T. Shimamura: An extraction method
of fundamental frequency using clipping and band limita-
pitch extraction of speech signal using autocorrelation
functions through multiple window-length, IEICE Trans.
Patterson: Fixed Point analysis of frequency to instan-
taneous frequency mapping for accurate estimation of F0
and periodicity, Proc.Eurospeech99, No. 6, pp. 2781–2784,
[26] A. de Cheveigné and H. Kawahara: Yin, a fundamental
frequency estimator for speech and music, J. Acoust. Soc.
[27] H. Kawahara, I. Masuda-Katsuse and A. de Cheveigné:
Restructuring speech representations using a pitch-
adaptive time-frequency smoothing and an instantaneous-
frequency-based F0 extraction: Possible role of a repeti-
tive structure in sounds, Speech Communication, Vol. 27,
and K. Shikano: Robust fundamental frequency estima-
tion using instantaneous frequencies of harmonic compo-
[29] Y. Ishimoto, M. Unoki and M. Akagi: A Fundamental
Frequency Estimation Method for Noisy Speech Based
on Instantaneous Amplitude and Frequency, Proc. Eu-
tion from Noisy Signal based on Auditory Scene Analysis,
1999.
[31] T. Nakatani and T. Irino: Robust and accurate funda-
mental frequency estimation based on dominant harmonic
[32] P. P. Vaidyanathan: Multirate systems and Filter Banks,
[33] H. Ohmura and K. Tanaka: Fine pitch contour extraction
by voice fundamental wave filtering method, J. Acoust.
[34] M. R. Schroeder: Modulation transfer functions: defini-
tion and measurement, Acustica, Vol. 49, pp. 179–182,
1981.
[35] H. Kuttruff: Room Acoustics, Taylor & Francis, fourth
transfer function in room acoustics as a predictor of speech

Fig. 7 Examples of relationship between power en-
velope of system based on MTF concept: (a) power
envelope $e_x^2(t)$ of (b) original signal $x(t)$, (c) power
envelope $e_h^2(t)$ of (d) impulse response $h(t)$, (e) power
envelope $e_y^2(t)$ derived from $e_x^2(t) * e_h^2(t)$, (f) reverber-
ant signal $y(t)$ derived from $x(t) * h(t)$, and (g) restored
power envelope $e_y^2(t)$

improved method based on the MTF concept for restoring
the power envelope from a reverberant signal, Acoustical
2004.
[38] M. Unoki, K. Sakata, M. Furukawa, and M. Akagi: A
speech dereverberation method based on the MTF con-
cept in power envelope, Acoustical Science and Technol-
[39] M. Unoki, K. Sakata and M. Akagi: A speech derever-
beration method based on the MTF concept, Proc. Eu-
[40] M. Unoki, M. Toi, and M. Akagi: Development of the
MTF-based speech dereverberation method using adapti-
tive time-frequency division, Proc. Forum Acusticum

Appendix MTF-based power envelope inverse
filtering

In the model of inverse-filtering of the power enve-
lope [37], the observed reverberant signal, the original
signal, and the stochastic-idealized impulse response
in room acoustics are denoted as $bfg(y(t))$, $x(t)$, and
$h(t)$, respectively, and are modeled as:

\[
    y(t) = x(t) * h(t)
\]

\[
    x(t) = e_x(t)n_1(t)
\]

\[
    h(t) = e_h(t)n_2(t) = a \exp(-6.9t/T_R)n_2(t)
\]

where the asterisks denote the convolution operation,
$e_x(t)$ and $e_h(t)$ are the envelopes of $x(t)$ and
$h(t)$, and $n_1(t)$ and $n_2(t)$ are the mutually independent respective white noise functions, i.e., $< n_k(t), n_k(t - \tau) > = \delta(\tau)$. The parameters of the impulse response, $a$ and $T_R$, correspond to a constant amplitude term and the reverberation time.

In this model, the power envelope of the reverberant signal, $e_y(t)^2$, can be determined as

$$\langle y^2(t) \rangle = e_x^2(t) + e_h^2(t) = e_y^2(t)$$  \hspace{1cm} (27)

where $< \cdot >$ is the ensemble average operation. This equation shows that there is a significant relationship between the envelopes; i.e., the MTF concept. Based on this result, $e_x^2(t)$ can be recovered by deconvoluting $e_y^2(t)$ with $e_h^2(t)$. Here, the transmission functions of power envelopes $E_x(z)$, $E_h(z)$, and $E_y(z)$ are assumed to correspond to the $z$-transforms of $e_x^2(t)$, $e_h^2(t)$, and $e_y^2(t)$. Thus, the transmission function of the power envelope of the original signal, $E_x(z)$, can be determined from

$$E_x(z) = \frac{E_y(z)}{a^2} \left\{ 1 - \exp \left( -\frac{13.8}{T_R \cdot f_s} \right) z^{-1} \right\}$$  \hspace{1cm} (28)

where $f_s$ is the sampling frequency. Finally, the power envelope, $e_x^2(t)$, can be obtained from the inverse $z$-transform of $E_x(z)$.

Figure 7 shows an example of how power-envelope inverse filtering is related to the MTF concept. Figure 7(a) shows a sinusoidal power envelope as original power envelope $e_x^2(t)$, and a white noise carrier, $n_1(t)$, using Eq. (25). Figure 7(b) shows power envelope $e_h^2(t)$ calculated using Eq. (26) with $T_R = 0.5$ s. Figure 7(d) shows the impulse response, $h(t)$, of Eq. (12), calculated from $e_h^2(t)$ and a white noise carrier, $n_2(t)$. Figures 7(e) and (f) show the power envelope, $e_y^2(t)$, obtained from a convolution of $e_x^2(t) \ast e_h^2(t)$ and the observed reverberant signal, $y(t)$, obtained from a convolution of $x(t)$ with $h(t)$, respectively. The left panels ((a), (c), and (e)) show the power envelopes of the signals and the right panels ((b), (d), and (f)) show the corresponding signals. In this figure, the modulation index decreased from 1.0 (in Fig. 7(a)) to 0.404 (maximum deviation of envelope between the dotted lines in Fig. 7(e) relative to that in Fig. 7(a)). Since the MTF concept shows the modulation index as a function of $F_m$ and $T_R$, it can also be shown that the decreased modulation index is derived from $m(2\pi F_m) = 0.402$ using Eq. (21) by substituting $T_R = 0.5$ s and $F_m = 10$ Hz into Eq. (21). The solid line in Fig. 7(g) indicates the restored power envelope $\hat{e}_y^2(t)$ obtained from reverberant power envelope $e_y^2(t)$ (Fig. 7(e)) using Eq. (28) with $T_R = 0.5$ s. We can see that power-envelope inverse filtering can accurately restore the power envelope from a reverberant signal in terms of shape and magnitude.

**Masashi Unoki** was born in Akita Pref., Japan, in 1969. He received his M.S. and Ph.D. (Information Science) from the Japan Advanced Institute of Science and Technology (JAIST) in 1996 and 1999. His main research interests are auditory-motivated signal processing and the modeling of auditory systems. He was a JSIS research fellow from 1998 to 2001. He was associated with the ATR Human Information Processing Laboratories as a visiting researcher during 1999–2000, and from 2000 to 2001 he was a visiting research associate at CNBH in the Dept. of Physiology at the University of Cambridge. He has been on the faculty of the School of Information Science at JAIST since 2001 and he is now an associate professor. He is a member of the Research Institute of Signal Processing (RISP), the Institute of Electrical and Electronic Engineering (IEEE), the Institute of Electronics, Information and Communication Engineers (IEICE) of Japan, the Acoustical Society of America (ASA), the Acoustical Society of Japan (ASJ), and the International Speech Communication Association (ISCA). Dr. Unoki received the Sato Prize for an Outstanding Paper from the ASJ in 1999 and the Yamashita Taro Prize for Young Researcher from the Yamashita Taro Research Foundation in 2005.

**Toshihiro Hosorogiya** was born in Ishikawa Pref., Japan in 1980. He received his B.E. from Nagoya University in 2005, and his M.S. from the Japan Advanced Institute of Science and Technology in 2007. He is a member of the Research Institute of Signal Processing (RISP) and the Acoustical Society of Japan (ASJ).

(Received June 17, 2007; revised September 11, 2007)